



Muonic Atom of Unstable Nuclei

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Introduction



◆ Physics Motivation

X-RAY SPECTROSCOPY of MUONIC ATOMS !

- ➔ Precision tool to measure the **NUCLEAR CHARGE DISTRIBUTION**.
- ➔ Usefully complement the knowledge obtained from electron scattering and laser spectroscopy.
- ➔ Successfully used since more than 30 years to study **STABLE ISOTOPES** in condensed or gaseous states !

Nuclear Charge Radii of Tin Isotopes from Muonic Atoms

C. Piller et al., Phys. Rev. C **42** (1990) 182,
L.A. Schaller Z. Phys. C **56** (1992) S48.
(Fribourg Univ. / Mainz Univ.; Exp. PSI μ E1)

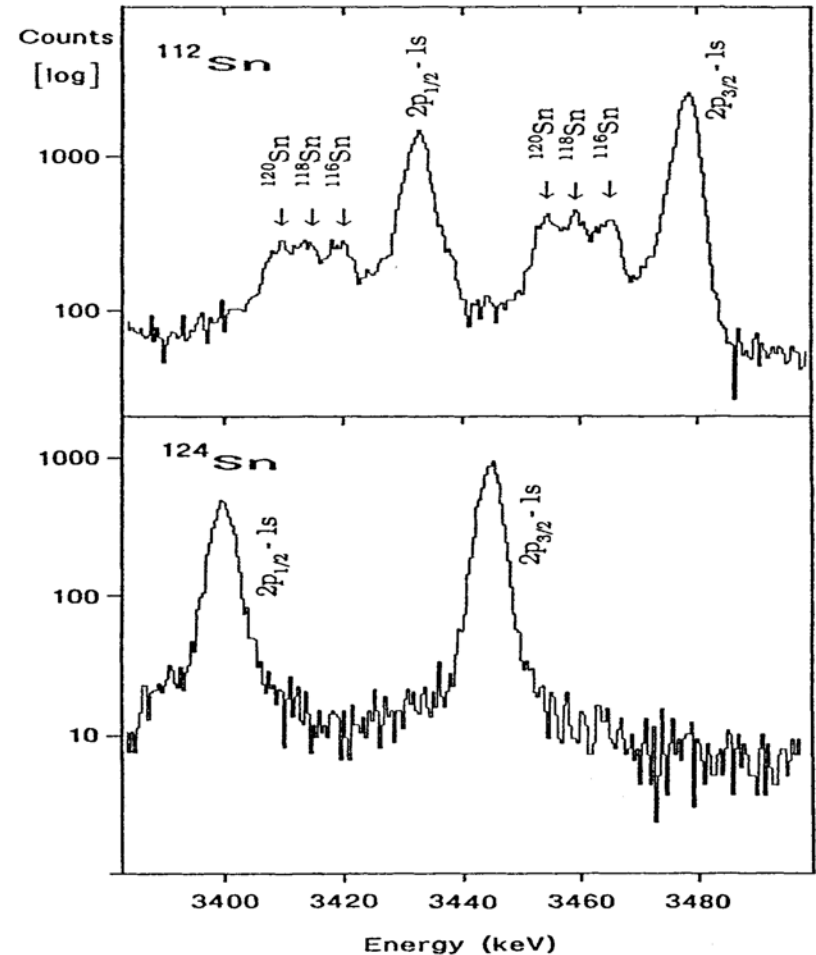


Fig. 3. Prompt muonic x-ray spectra showing the $2p_{1/2} - 1s$ and $2p_{3/2} - 1s$ transitions in the two tin isotopes at the extreme ends of stability, ^{112}Sn and ^{124}Sn (ref.2). The isotopic purity of ^{112}Sn was 68%, which explains the appearance of further tin isotopes in the upper half of this figure.

Towards Radioactive Muonic Atoms ?



◆ Facilities with both RI BEAM PROJECTS and negative muon beams:

- ➔ TRIUMF (ISAC), J-PARC (E-arena), ...
- ➔ RIKEN (RI Beam Factory) if intense μ^- can be produced,
- ➔ and maybe at a NEUTRINO FACTORY PROJECT

RAMA WORKSHOP

◆ In the near Future

- ➔ MUON BEAM of significant higher flux ($10^{12}\mu/s, 55\text{MeV}/c$ PRISM_μ),
- ➔ NEXT GENERATION of RNB facility

◆ Experimental Methods using muons

- ➔ Merging Beams Scenario (M. Lindros, CERN) ,
- ➔ Combined Cyclotron Trap & Penning Trap,
- ➔ **SOLID HYDROGEN & MUON TRANSFER**

◆ Other Methods for Unstable Nuclei

PRESENT: Optical Laser Spectroscopy (ISOLDE, RIKEN, ...)

FUTURE: Electron Scattering with e^- & RI collider Rings (GSI , MUSES at RIKEN, ...)

ECT*
EUROPEAN CENTRE FOR THEORETICAL STUDIES
IN NUCLEAR PHYSICS AND RELATED AREAS
TRENTO, ITALY
Institutional Member of the European Science Foundation Associated Committee NuPECC

RADIOACTIVE MUONIC AND ANTIPROTONIC ATOMS
May 22-26, 2001

MAIN TOPICS:

- Survey of nuclear and general physics background and motivation
- Review of previous muonic and antiprotonic atom research
- Discussion of novel ideas to produce radioactive antiprotonic and muonic atoms
- Comparison with alternate experimental methods
- Identification of key experiments
- Exploration of the possibilities for technical realization
- Impulses to form new international collaborations

SPEAKERS INCLUDE:
N. Aschbach (Trento), J. Deutsch (Lausanne), R. Engler (Garching), M. Hammad (CERN), J. Jankovská (Warsaw), A. S. J. Johansson (Groningen), E. Kolbe (Oak Ridge), K. Langaké (Lund), M. Lindros (CERN), M. Nagamatsu (Oak Ridge), T. Nilsson (Groningen), M. L. Rivas (Groningen), P.-G. Rothard (Groningen), R. Rossignol (Aachen), J. Sakuma (Kyushu), A. Vaché (Trento), M. C. Volpe (Orsay), D. Vretenar (Zagreb), T. Yamazaki (Osaka)

ORGANIZERS OF THE WORKSHOP:
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Klaus Jungmann, KVI Groningen, organizer and group leader (jungmann@kvi.nl)

Director of the ECT*: Prof. Wolfgang Weise (Trento)
Scientific Secretary: Prof. Renato Leonardi (Trento)

The ECT* is sponsored by the "Istituto Trentino di Cultura" in collaboration with the "Associazione alla Cultura" (Provincia Autonoma di Trento), funding agencies of EU Member and Associated States and with the support of the Department of Physics of the University of Trento.

Participation in the ECT* scientific projects led by researchers of the EU Member and Associated States is partially financed by the EU - Human Potential Program to provide access to Major Research Infrastructures (STATE projects); see <http://ect.jcu.eu.org>
Postdoctoral researchers are encouraged to apply to individual EU fellowships; see http://www.cerdl.it/learning/for_hp_mz.htm

Why Radioactive Muonic Atoms ?



◆ Probing Nuclear Charge Distribution

Matter distribution deduced from measured interaction cross sections. Charge distribution needed to get information on proton and neutron distributions in nuclei.

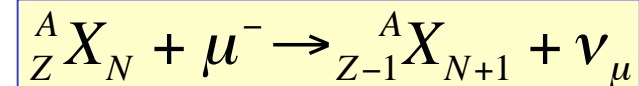
➔ **X-RAY SPECTROSCOPY** of **RADIOACTIVE MUONIC ATOMS !**

◆ Deformation Properties

Quadrupole hyperfine splitting of muonic X-rays yield precise and reliable absolute quadrupole moment values. Measure the deformation properties of nuclei.

➔ **IMPORTANT ROLE** in **ESTABLISHING** and **REFINING NUCLEAR STRUCTURE MODELS !**

◆ Muon Capture



Tools to explore changes in collective excitation modes of neutron-rich nuclei.

Kolbe et al., Eur. Phys. J A **11** (2001) 39; T. Nilsson et al., Nucl. Phys. A 746 (2004) 513c

➔ **IMPORTANT ASTROPHYSICAL IMPLICATIONS !**

◆ Novel nuclear structure effects may exist far off the valley of stability ?

μA^* Technical Feasibility

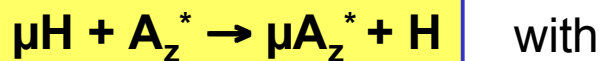


◆ How to produce such exotic μA^* atoms ?

We propose:

➔ **SOLID HYDROGEN FILM** used to stop both simultaneously μ^- and A^* beams.

➔ **μA^* ATOMS** formed through **MUON TRANSFER REACTION** to higher Z nuclei, i.e.,

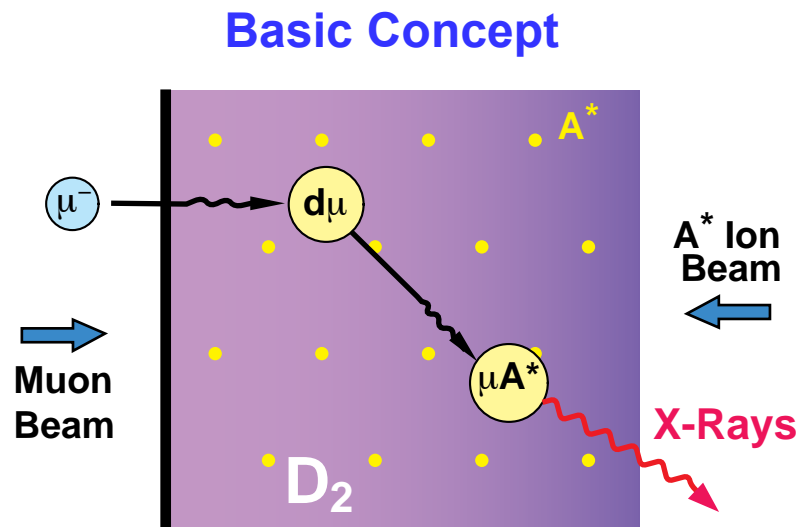


$$\text{TRANSFER RATE: } \lambda_z \approx C_z Z 10^{10} \text{ s}^{-1}$$

HIGH TRANSFER RATE & HIGH EFFICIENCY

e.g., $Z = 50$ and
 $C_z = 1 \text{ ppm } (5 \times 10^{16} \text{ nuclei/cm}^3)$

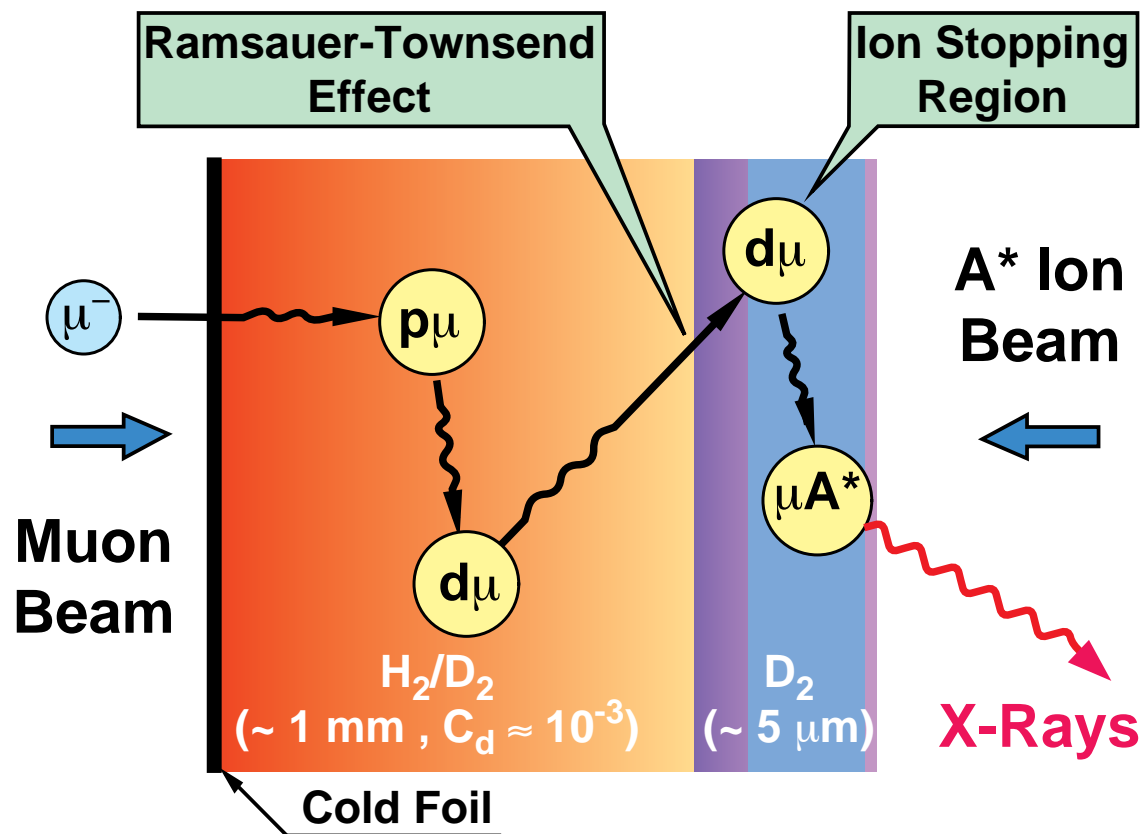
➔ $\lambda_z \approx 5 \times 10^5 \text{ s}^{-1}$



μA^* Technical Feasibility (2)



◆ Basic Concept: Two-Layer Arrangement



Preliminary Transfer Yield Estimation



◆ Transfer Yield Estimation (Two-Layer Arrangement)

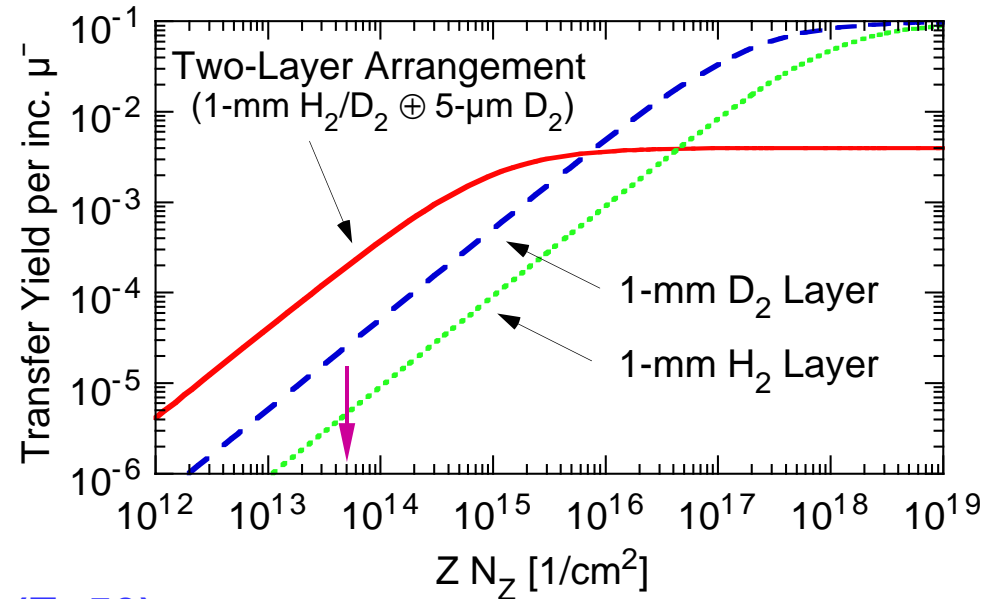
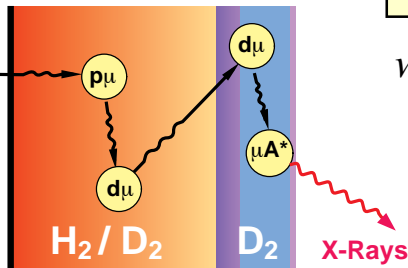
No $d\mu$ atom loss !

$$Y_X = \frac{\phi \lambda_Z}{\lambda_0 + \phi \lambda_Z} Y_{\mu^-} Y_{d\mu}$$

with $\lambda_Z \approx C_Z Z \times 10^{10} \text{ s}^{-1}$,

$$C_Z = N_Z / N_D,$$

$Y_{\mu^-} \approx 0.1$, $Y_{d\mu} \approx 0.04$
 μ^- Stopping $d\mu$ Emission



◆ Preliminary Yield Estimation for Tin (Z=50):

■ Muon Intensity (1 cm ² , 30 MeV/c):	$1 \times 10^8 \text{ [s}^{-1}\text{]}$	21st Century Muon Beam SHC confinement Field
■ Implanted Sn Ions (1 cm ² , uniform):	1×10^{12}	
■ Transfer Yield per incident μ^- :	2×10^{-4}	1-mm D ₂ 2×10^{-5}
■ Muonic Tin Atoms Formed:	$20'000 \text{ [s}^{-1}\text{]}$	$2'000 \text{ [s}^{-1}\text{]}$
■ Total X-Ray Number Detected:	$500 \text{ [hr}^{-1}\text{]}$	$50 \text{ [hr}^{-1}\text{]}$

Assuming for $\mu\text{Sn } 2p \rightarrow 1s$ X-ray detection ($\sim 3.4 \text{ MeV}$) : b.r. ~ 0.7 , $\epsilon \sim 0.005$ and $\Delta\Omega \sim 0.002$.

Practical Considerations



◆ **SIMULTANEOUS** implantation of unstable nuclei and measurement with μ^- .

◆ Ion beam **ENERGY** and **SPREAD** determine the implantation **DEPTH** and **THICKNESS**.

Ion range in solid hydrogen: 1 mm \Leftrightarrow ~ 10 MeV/u
 5 μm \Leftrightarrow ~ 30 keV/u

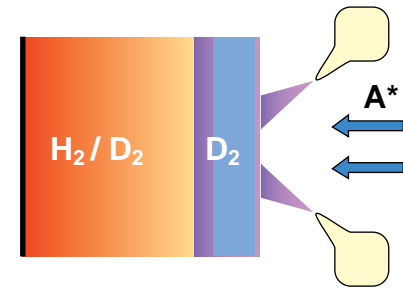
➔ **SWEEPING** Beam Energy

◆ **CONTINUOUS SPUTTERING** of solid hydrogen films.

If proven important,

➔ **SIMULTANEOUS**

Hydrogen Deposition
& Ion Implantation



◆ RI beam **COMPLETELY** stopped in the target!

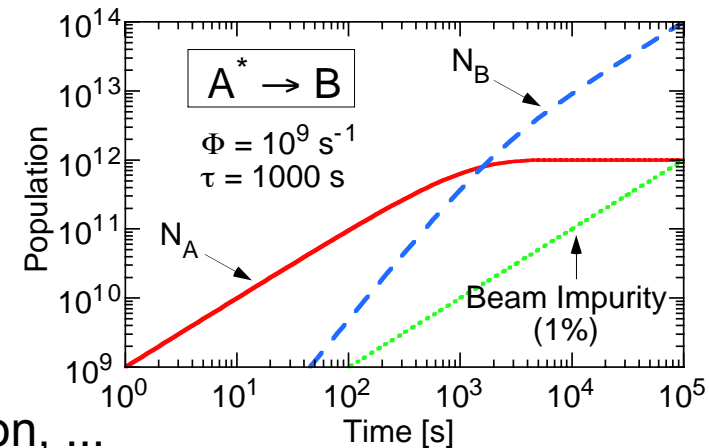
❖ **ACCUMULATION** of **DAUGHTER NUCLEI**

➔ **LIMITATION** (static target): $T_{1/2} > 10$ min.

❖ **ACTIVITY HIGH RADIATION BACKGROUND**

➔ Pulsed Muon Beam

➔ Active BG suppression, Detector segmentation, ...



Using Solid Hydrogen Films



◆ Advantages

- ➔ **WINDOWLESS TARGET** in vacuum
- ➔ **WELL-DEFINED** interaction region
- ➔ **EASY TARGET EVAPORATION** and **REPLACEMENT**
- ➔ **RI BEAM**: Impurities, Emittance, Energy spread, ... ➔ **NOT CRITICAL**
No Cooling Needed!

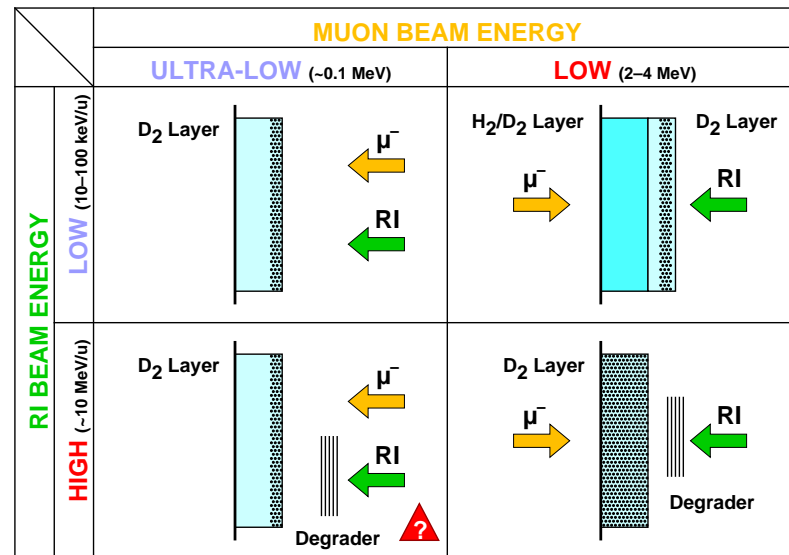
◆ Disadvantages

- ➔ **SPUTTERING**
- ➔ **ACCUMULATION** of **DAUGHTER NUCLEI**
➔ **NEW IDEAS !** e.g., using sputtering vs. daughter nuclei accumulation

◆ Other Considerations

- ➔ Magnetic confinement field
- ➔ Pulsed muon beam

Different μA* Formation Schemes

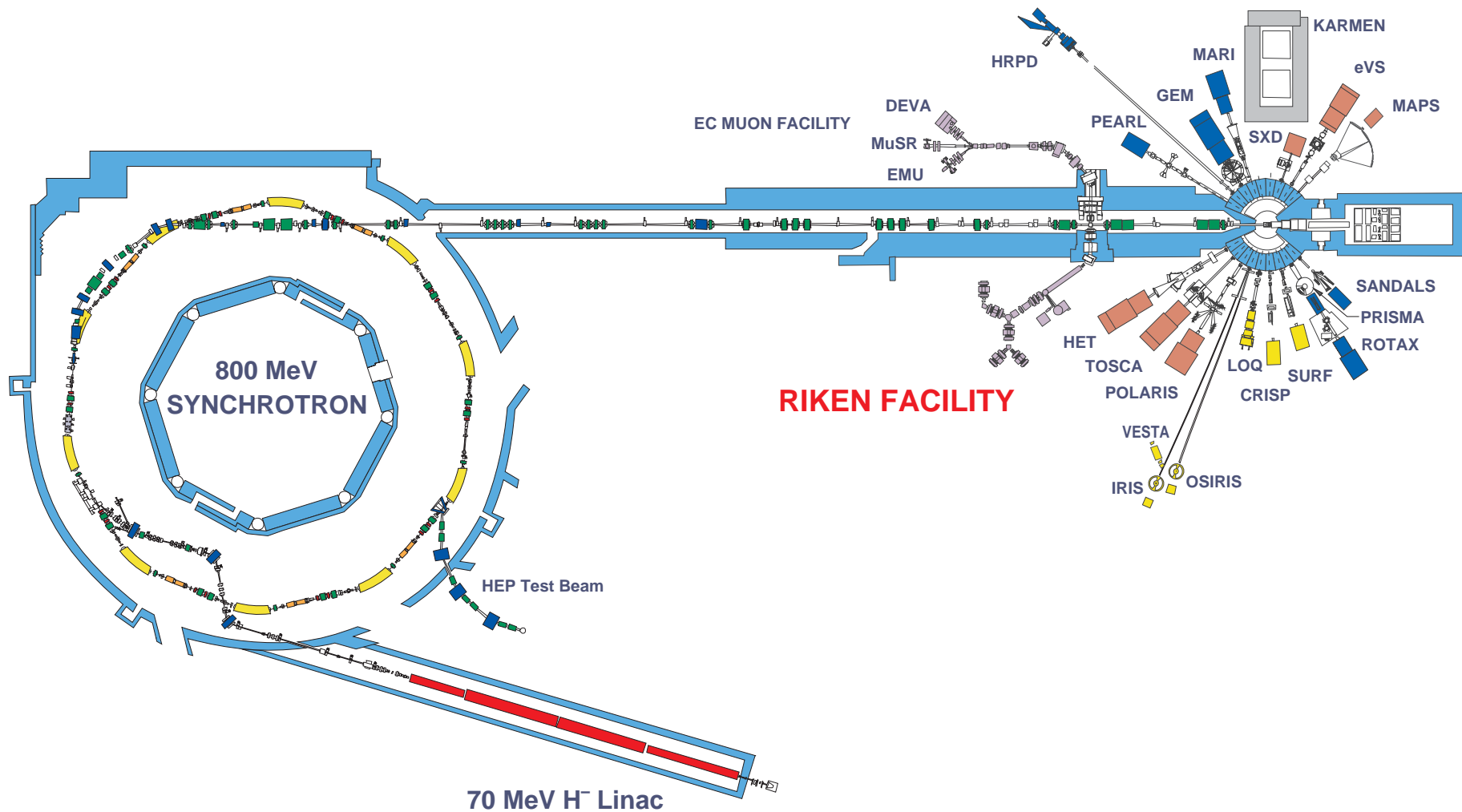


Feasibility Study

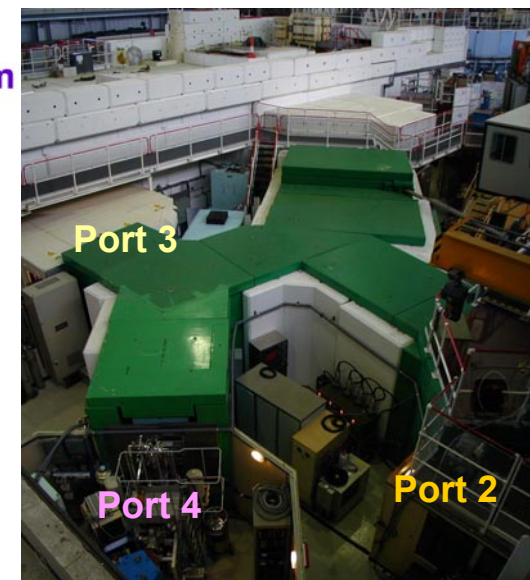
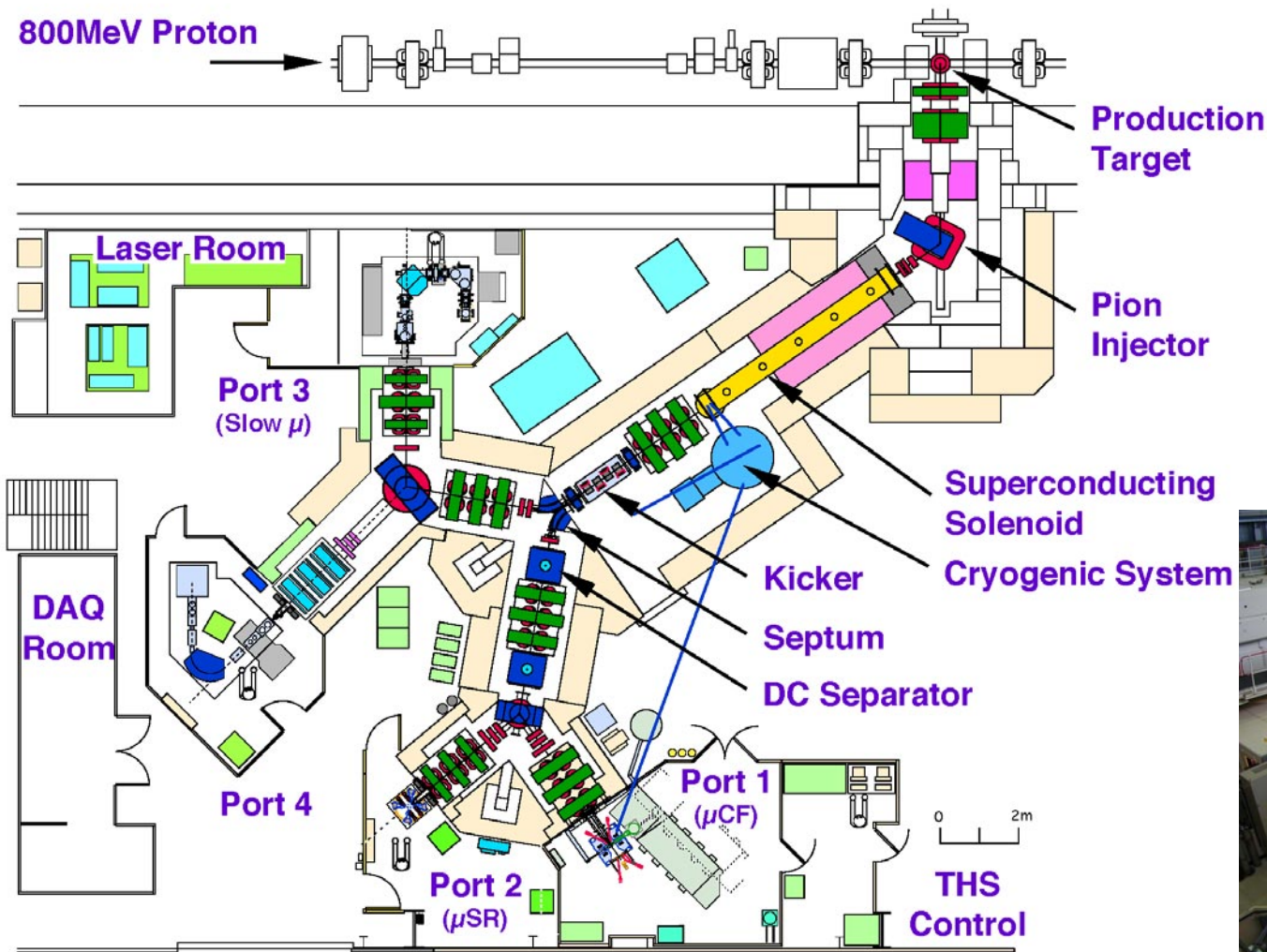


- ◆ **EXPERIMENTAL SETUP** for X-ray spectroscopy of muonic atoms formed from implanted ions in solid hydrogen
- ◆ **TEST EXPERIMENT** at RIKEN-RAL Muon facility.
- ◆ Establish the feasibility of this method by using **STABLE IONS**.
- ◆ **μCF RELATED STUDY**: Helium transfer in Solid Hydrogen Films
- ◆ In the near future, experiment using **LONG-LIVED ISOTOPES**.

ISIS Facility at RAL



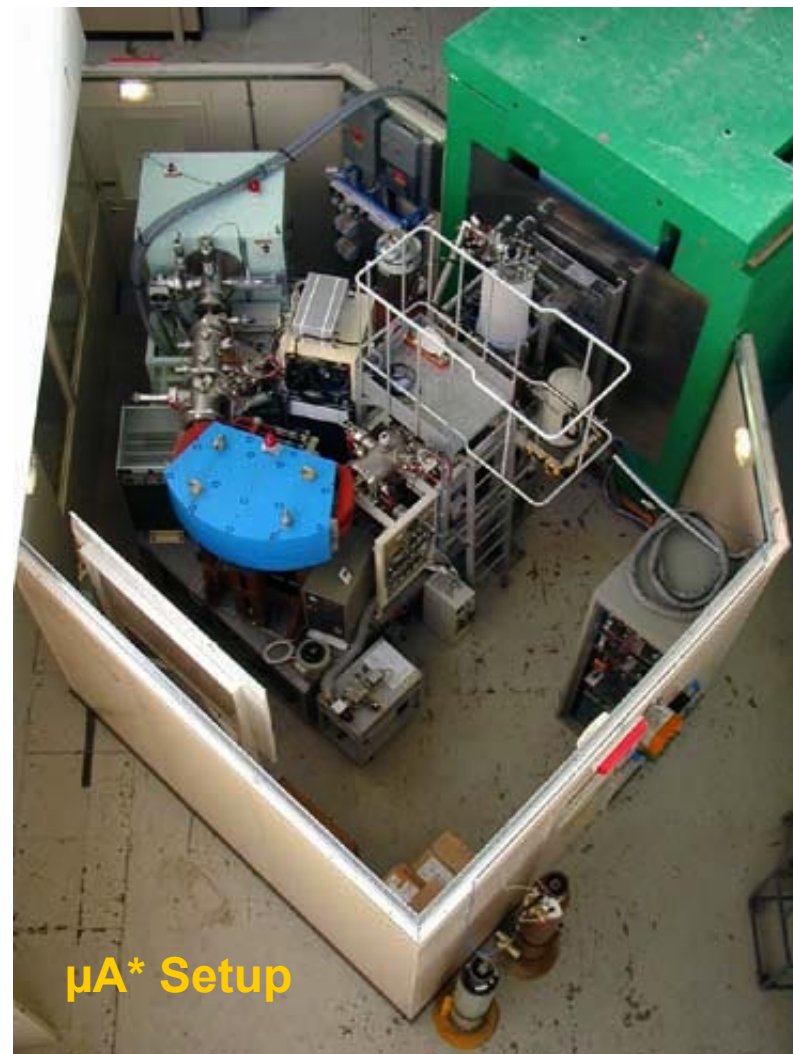
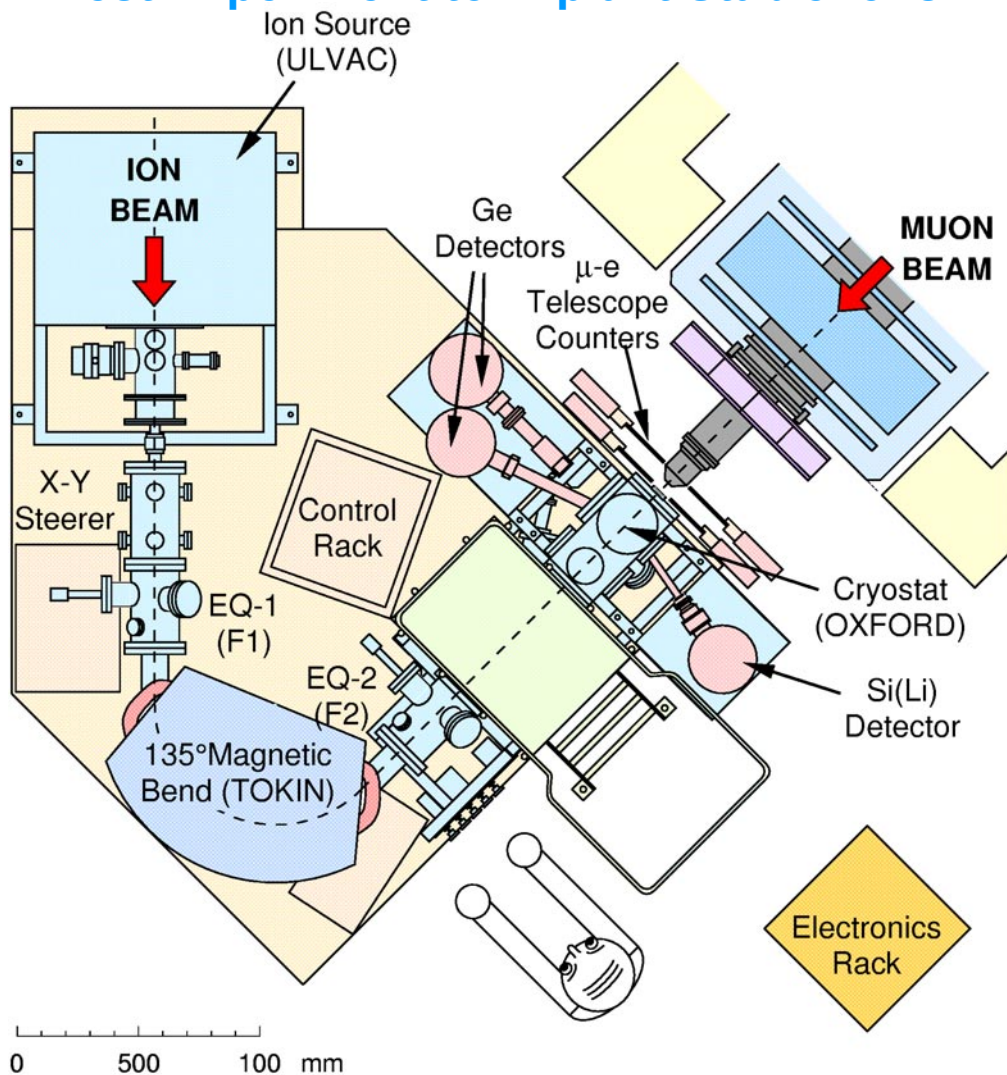
RIKEN-RAL Muon Facility at ISIS



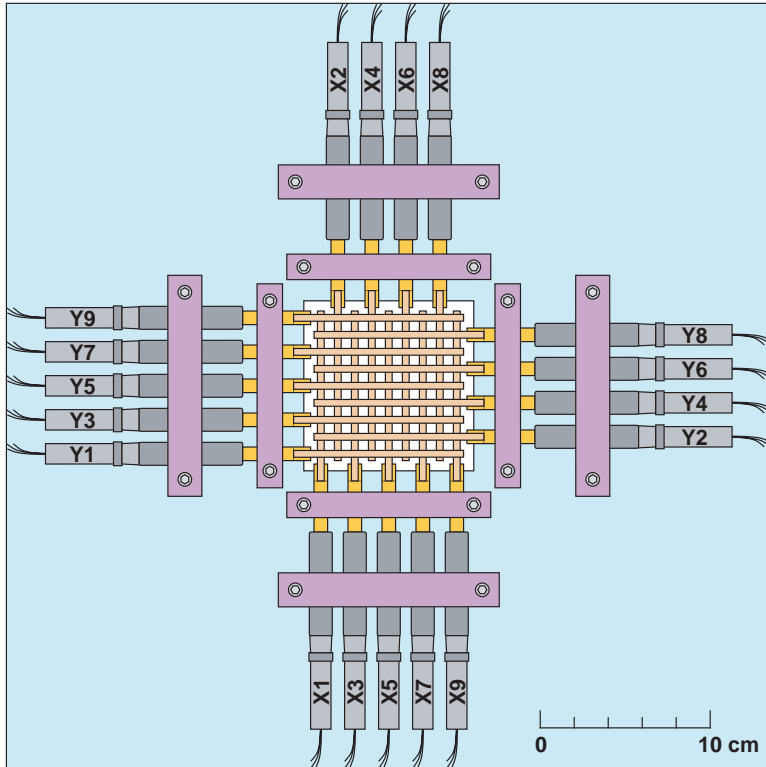
μA^* Setup at RIKEN-RAL Port 4



Test Experiment to Implant Stable Ions in Solid Hydrogen Films.



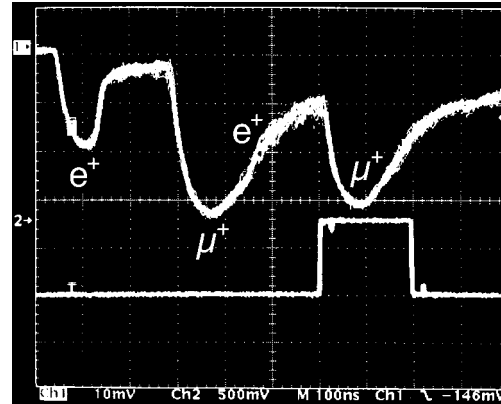
Muon Beam Profile (1)



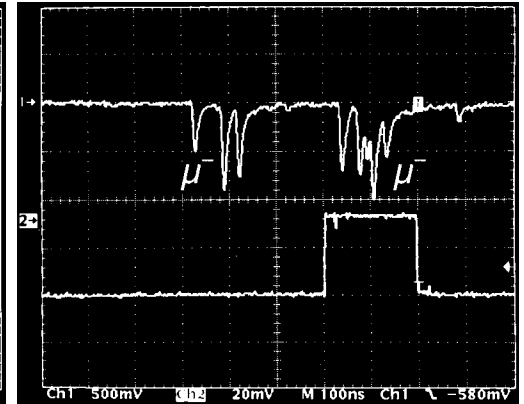
Muon Beam Profile Monitor

Photomultiplier output signal of counter X5

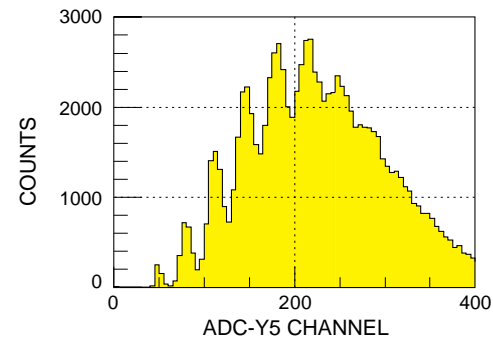
27 MeV/c surface μ^+



27 MeV/c decay μ^-



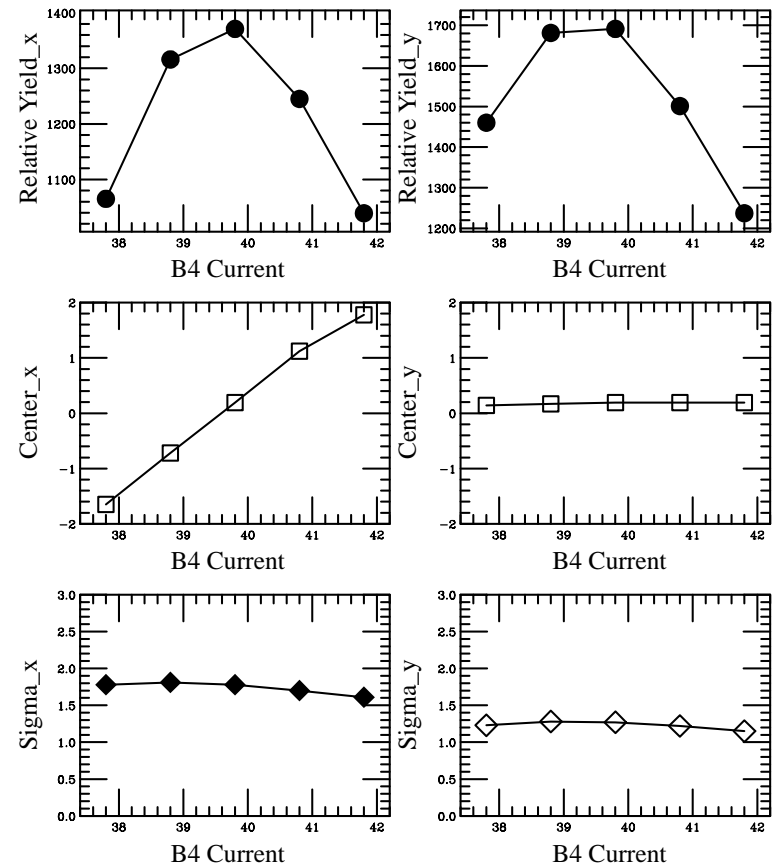
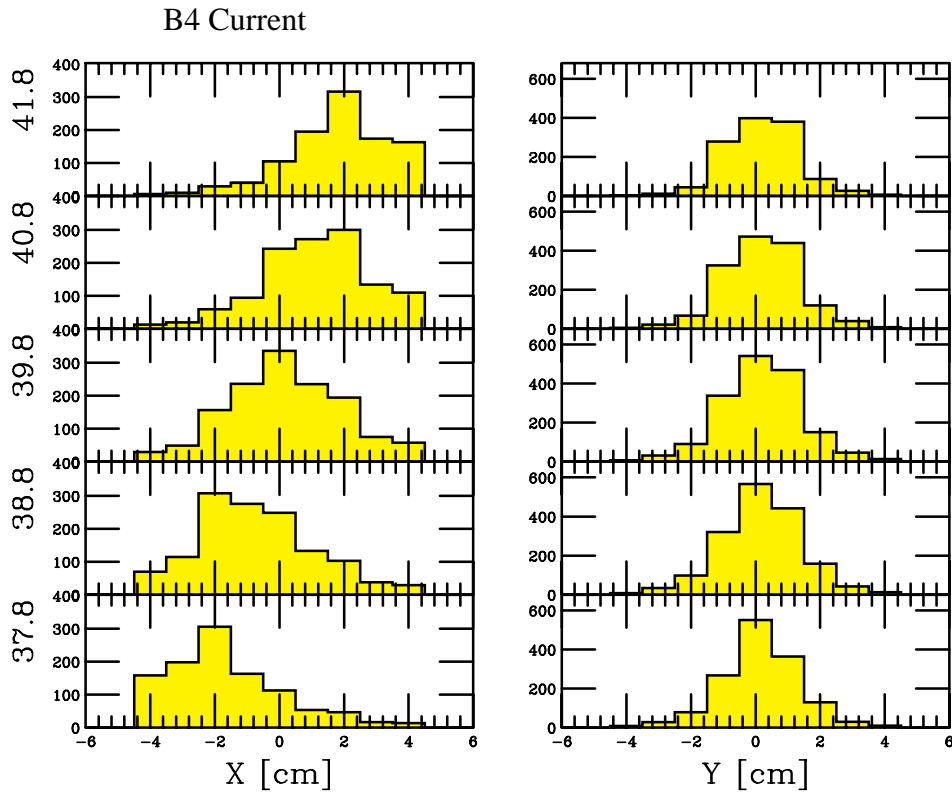
ADC output with 27 MeV/c decay μ^-



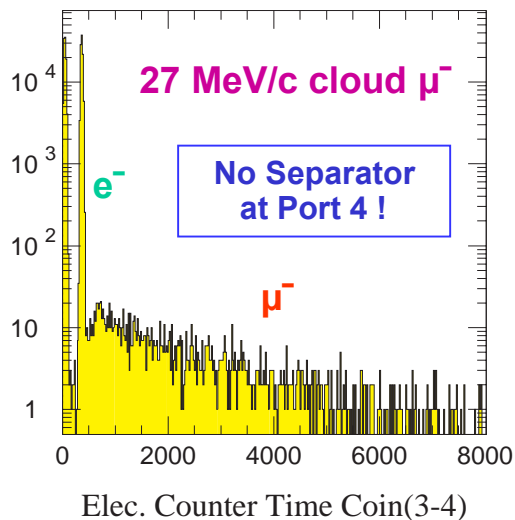
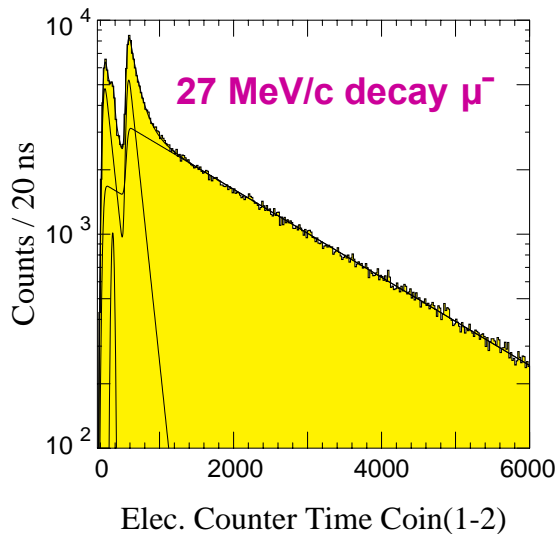
Muon Beam Profile (2)



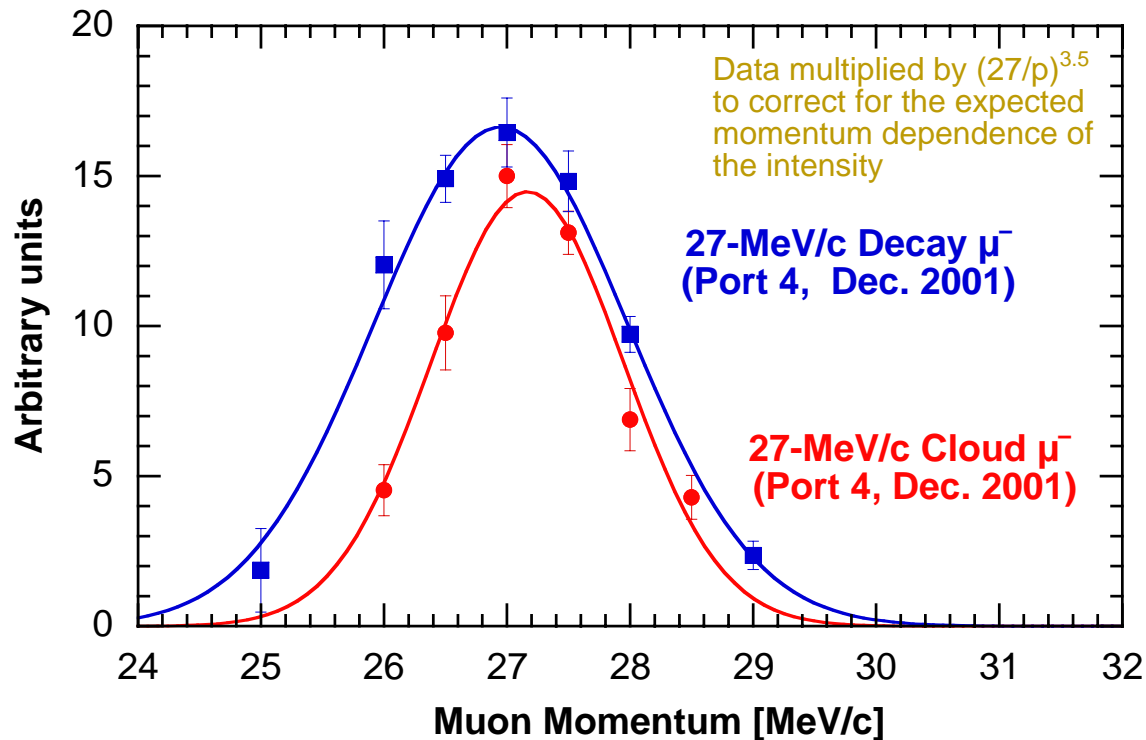
Horizontal and vertical muon beam profiles as a function of B4 dipole magnet measured with surface muons at Port 4.



Muon Beam Momentum Tuning



Target: 1-mm H₂ Layer



$y = b \cdot \exp(-((x-c)/d/c)^{2/2})$		
	Value	Error
b	8.3152	0.31079
c	26.948	0.054839
d	0.038189	0.0021276
Chisq	1.4064	NA
R	0.99803	NA

$y = b \cdot \exp(-((x-c)/d/c)^{2/2})$		
	Value	Error
b	14.478	0.67035
c	27.165	0.044866
d	0.028824	0.0016279
Chisq	3.96	NA
R	0.98548	NA

Muon Stopping Distribution

◆ Negative Muon Beam at RIKEN-RAL Port 4

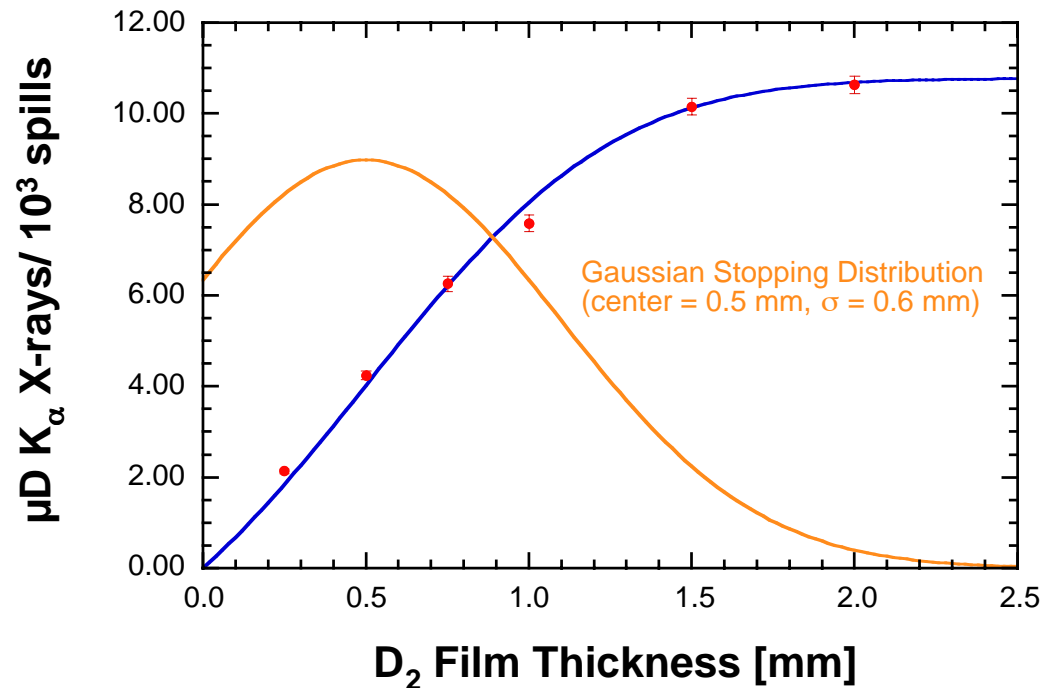
- ➔ Muon Source: Decay Muon
- ➔ Momentum: 27 MeV/c
- ➔ Width ($\Delta p/p$): $\sim 10\%$
- ➔ Intensity: $\sim 5000 \text{ s}^{-1}$
- ➔ Beam size: $\sim \text{Ø}40 \text{ mm}$

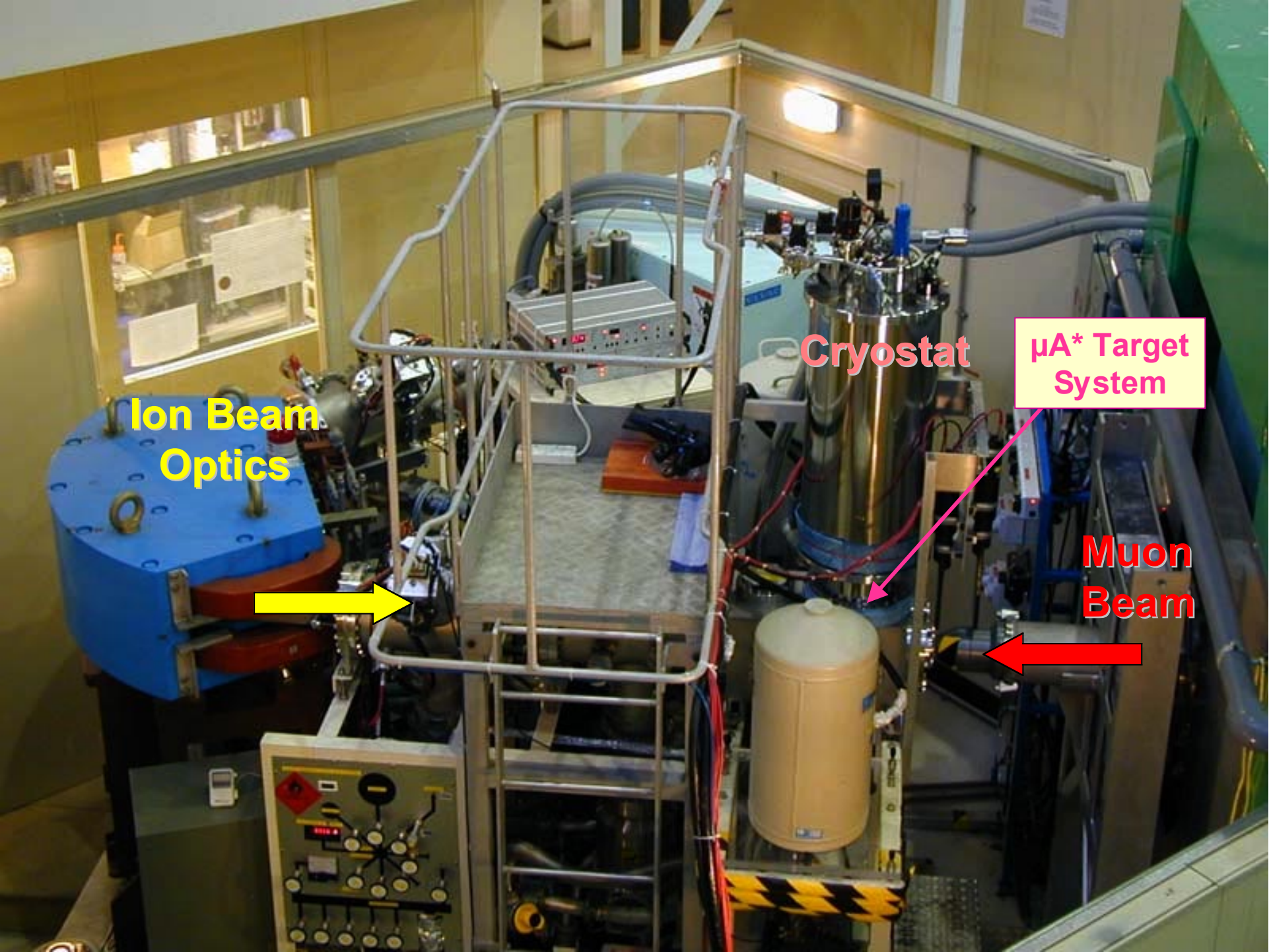


- Cloud Muon
- 27 MeV/c
- $\sim 7\%$
- $\sim 15000 \text{ s}^{-1}$
- if separator installed!
- ($\sim 3x$)

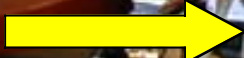
◆ Muon Stopping in Solid D₂

- ➔ 1-mm D₂: $\sim 60\%$
(3000 s^{-1})
- ➔ Silver Foil: $\sim 20\%$
- ➔ Ratio: 3





Ion Beam Optics

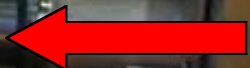


Cryostat

μ A* Target System



Muon Beam

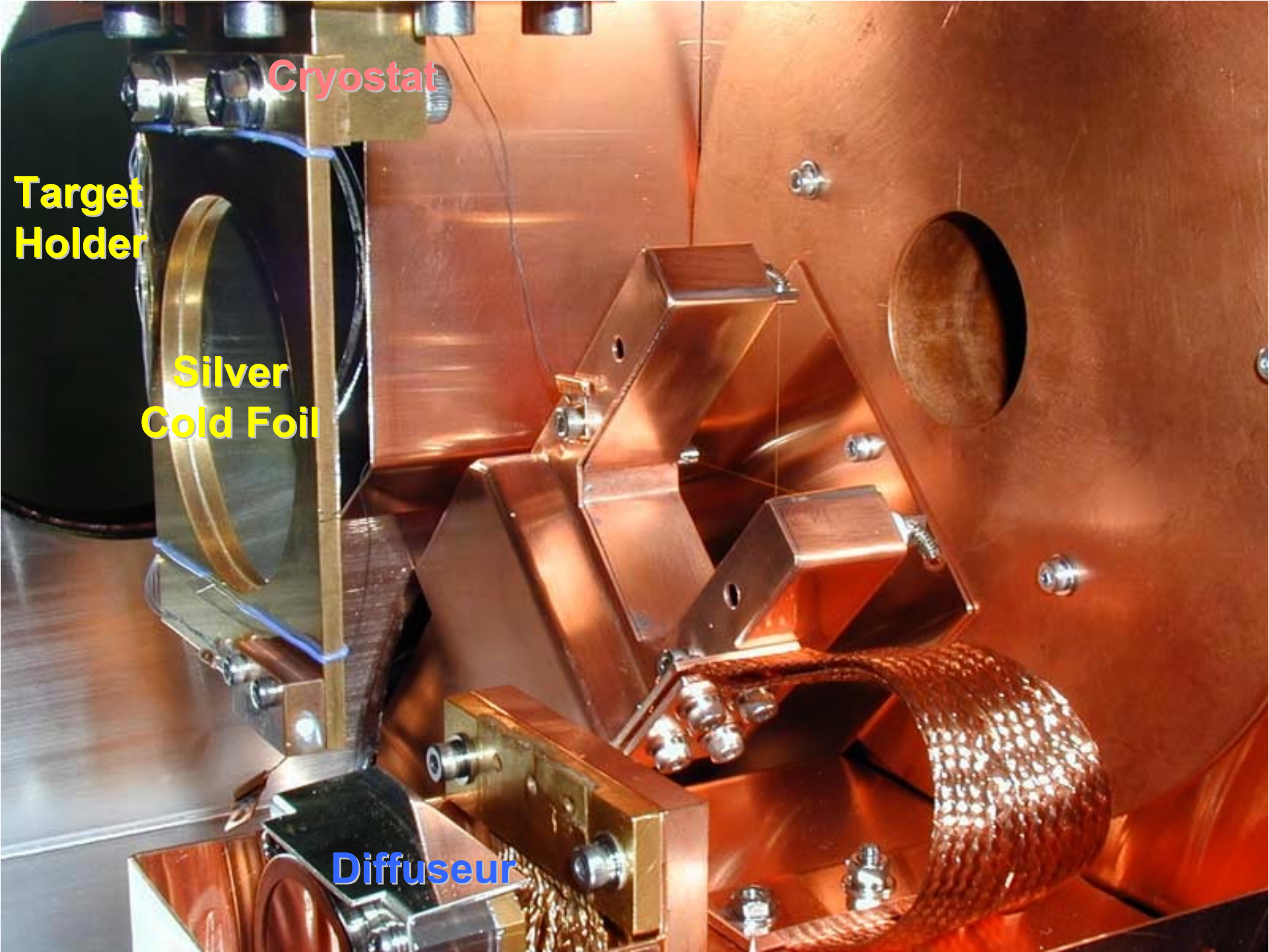


Cryostat

**Target
Holder**

**Silver
Cold Foil**

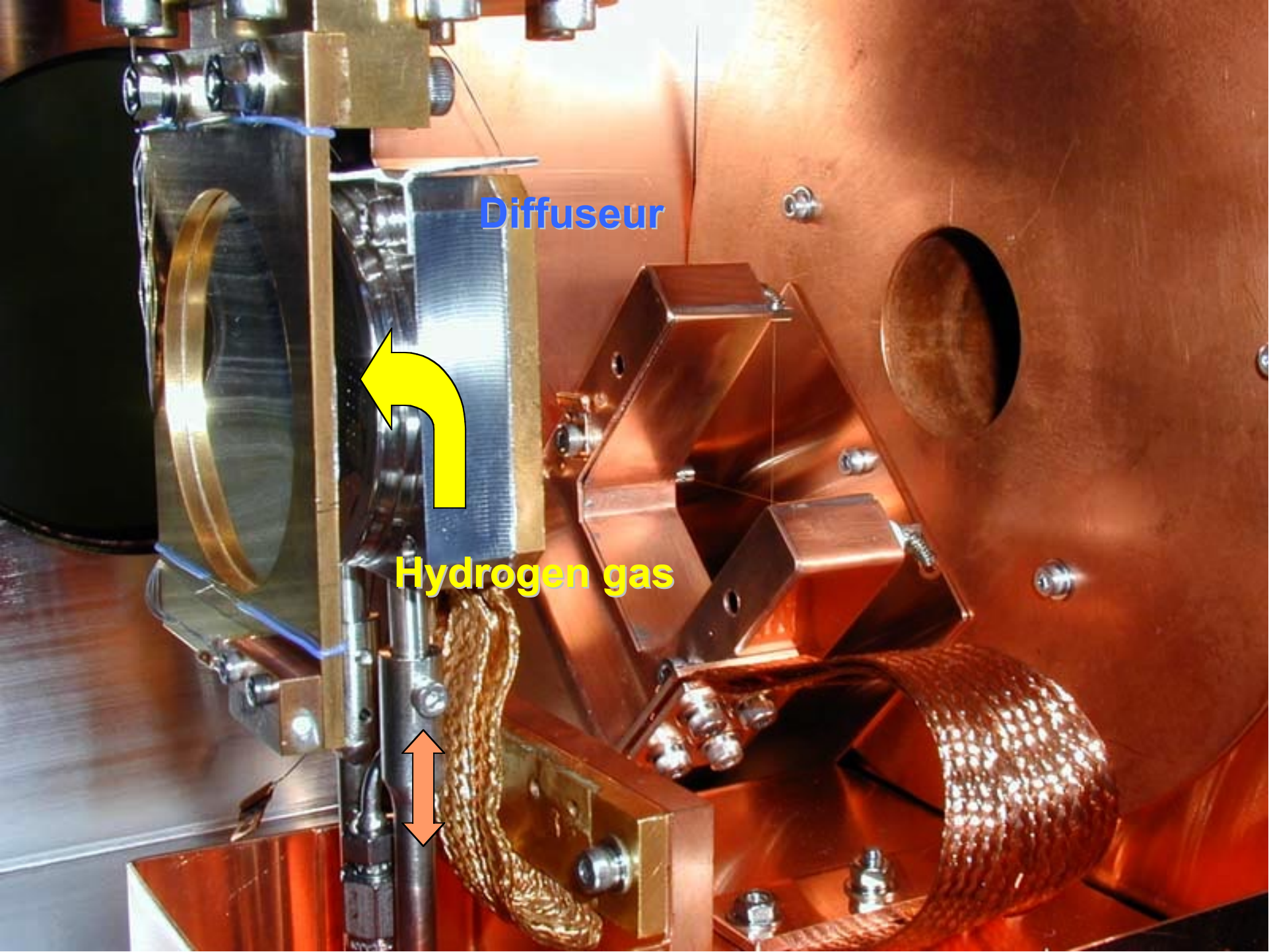
Diffuseur

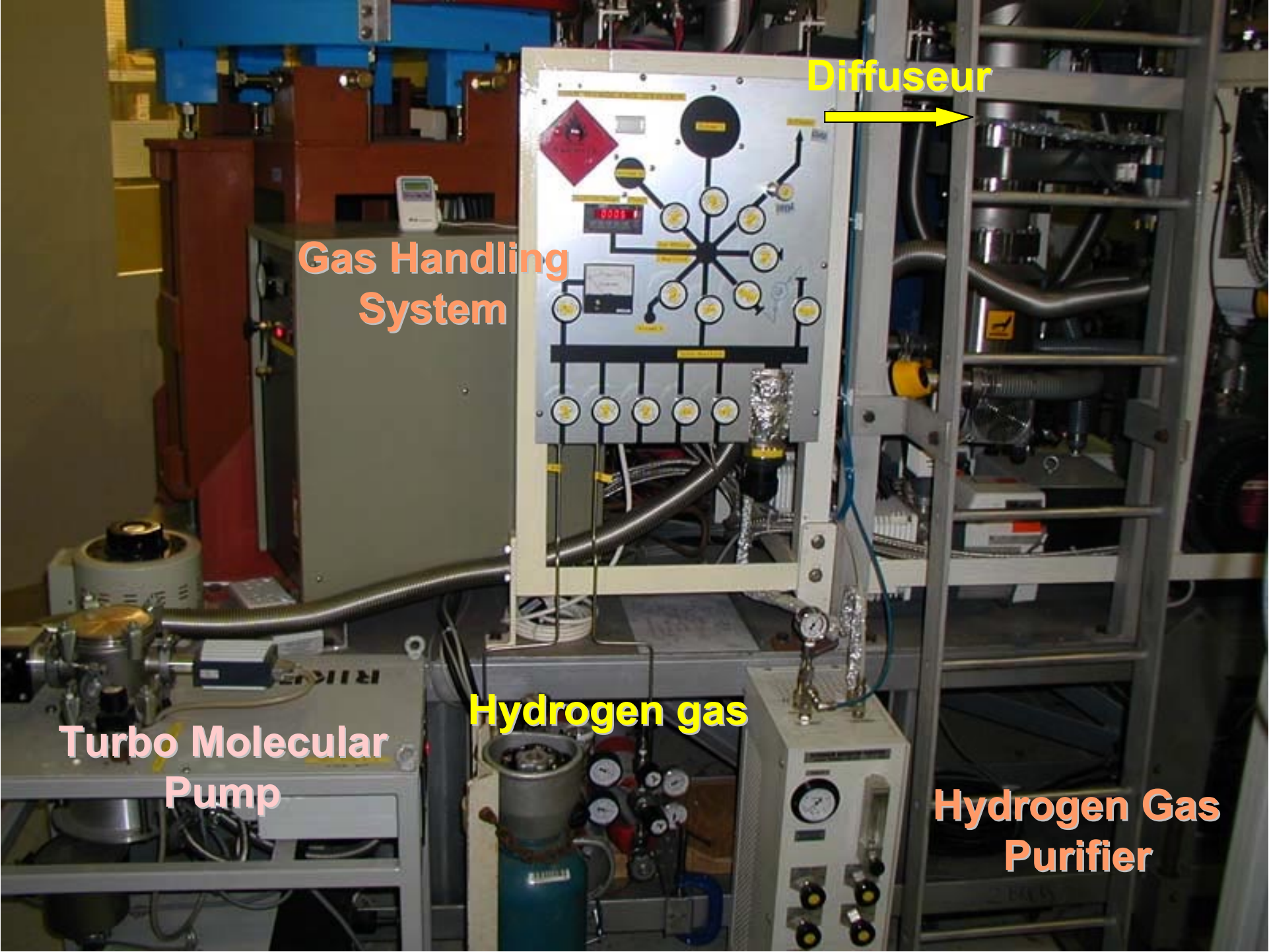


Diffuseur

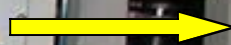


Hydrogen gas





Diffuseur

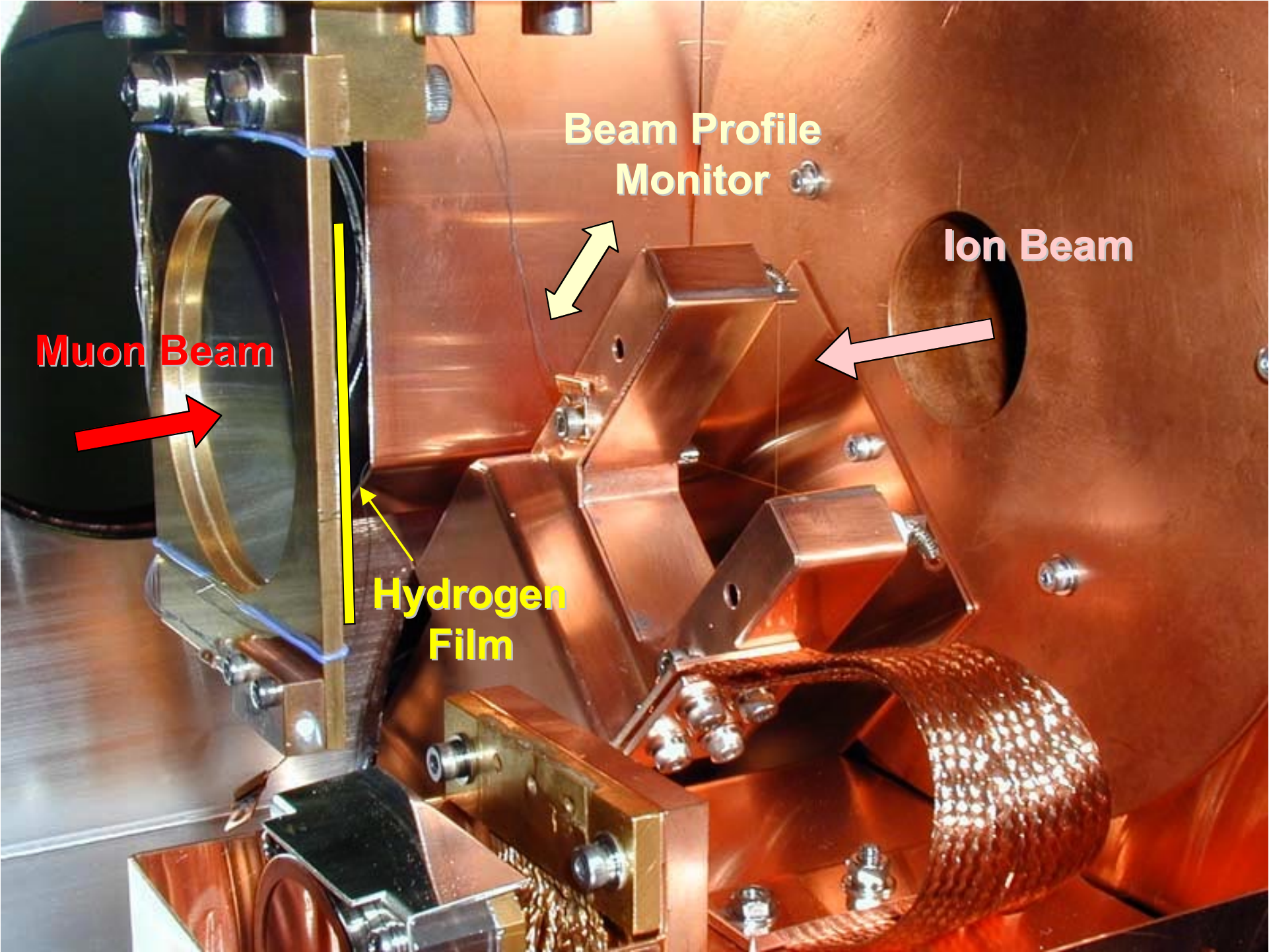


Gas Handling System

Turbo Molecular Pump

Hydrogen gas

Hydrogen Gas Purifier

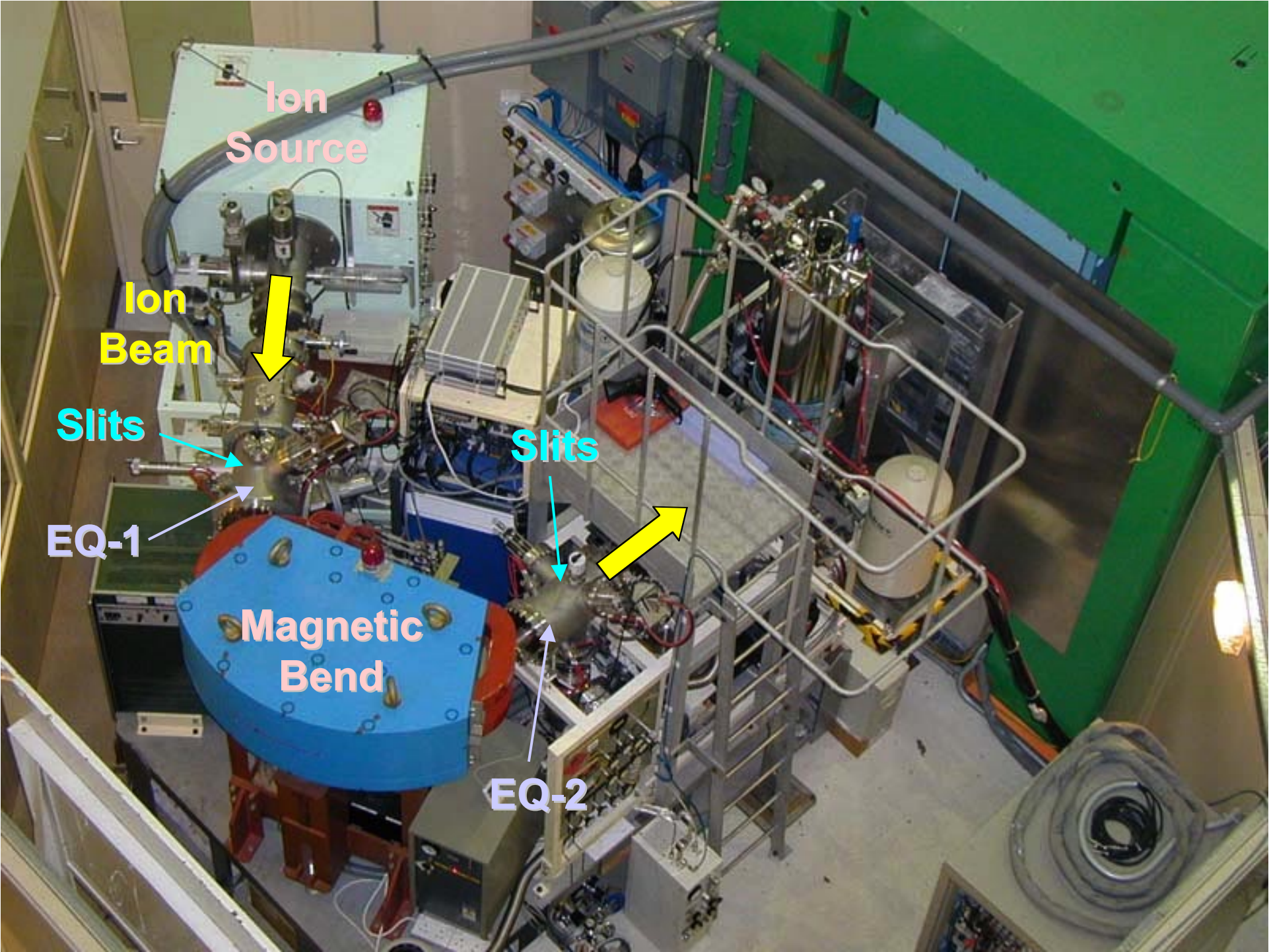


Muon Beam

Beam Profile Monitor

Ion Beam

Hydrogen Film



Ion Source

Ion Beam

Slits

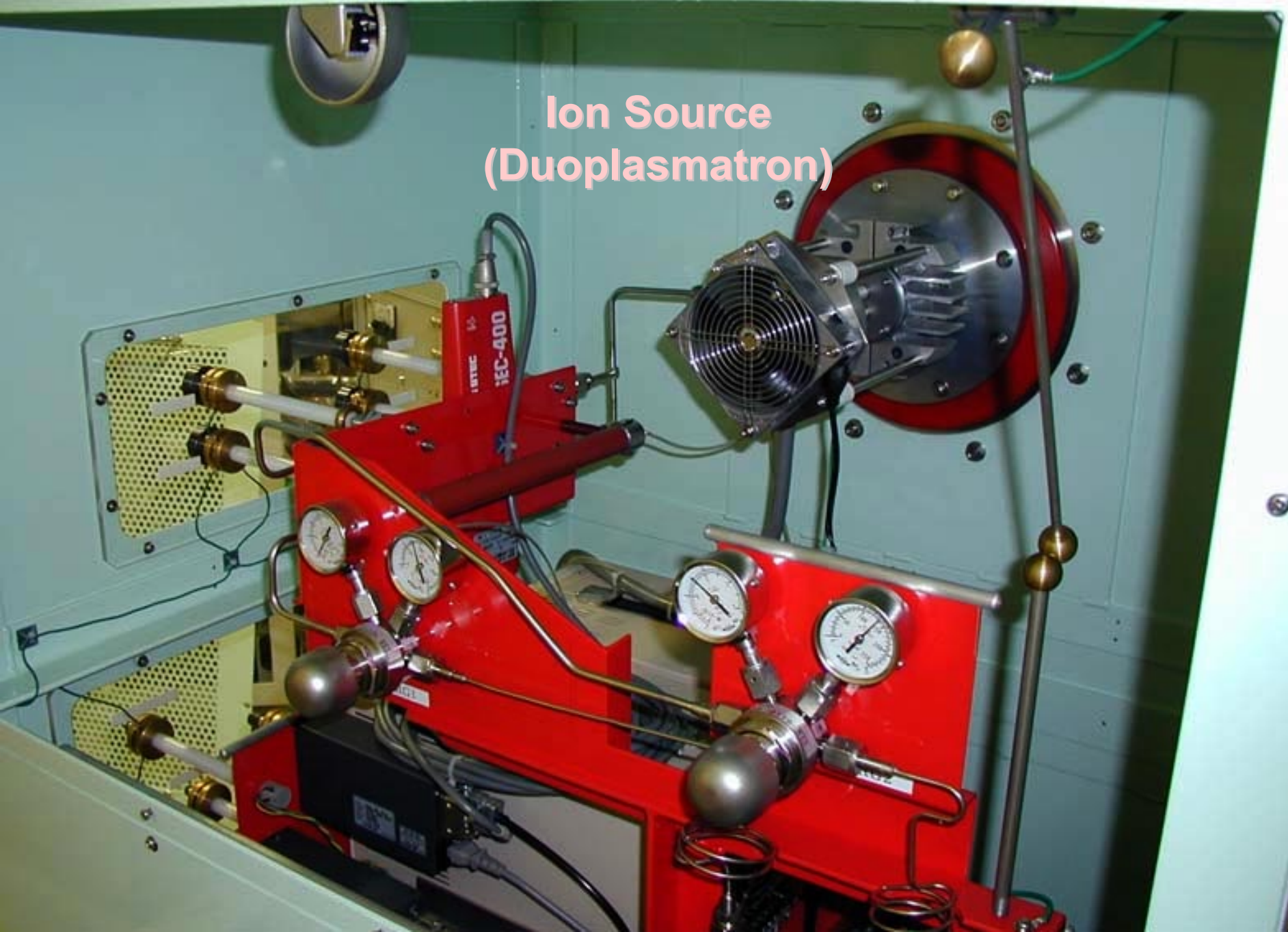
EQ-1

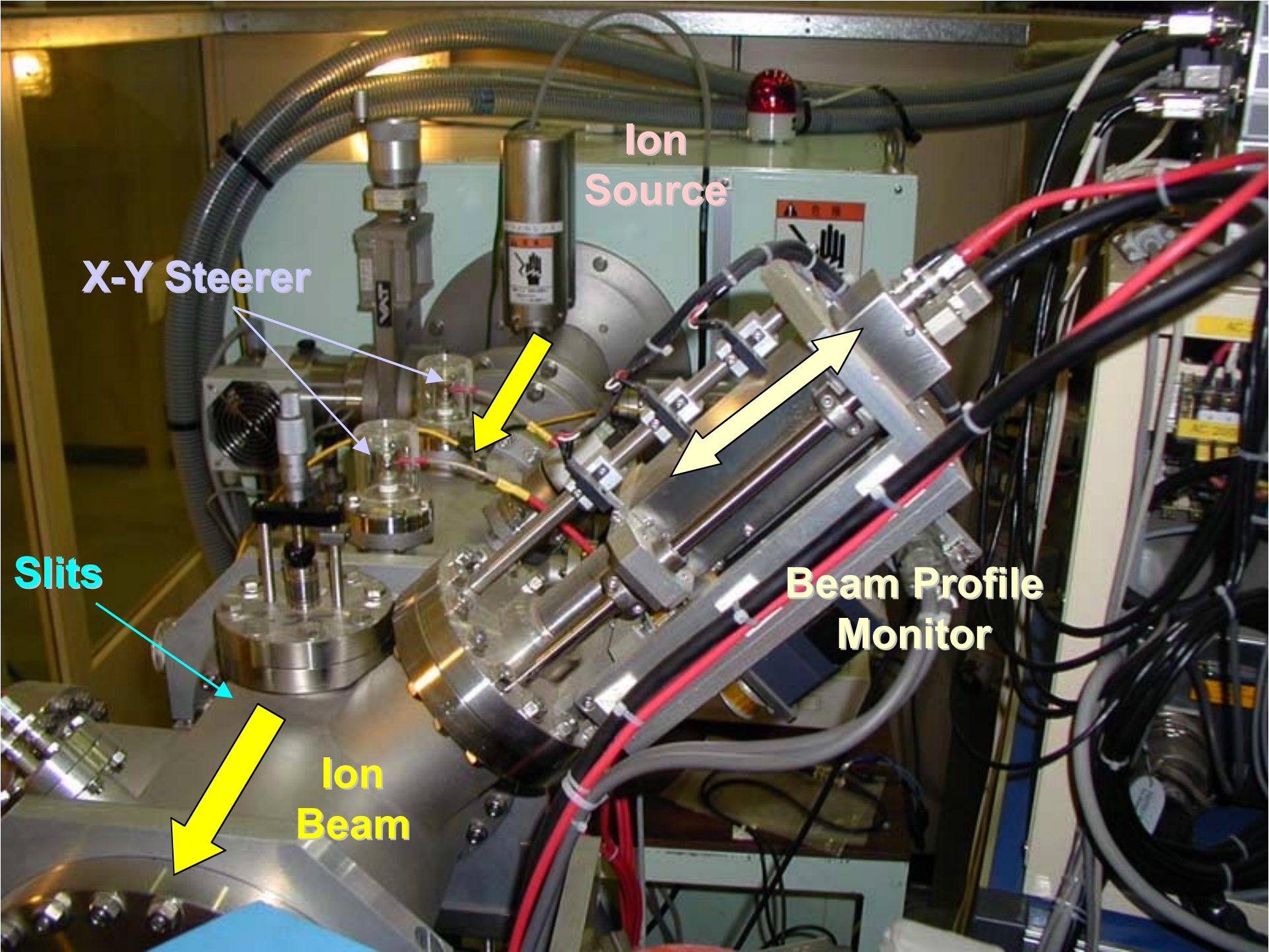
Magnetic Bend

Slits

EQ-2

Ion Source (Duoplasmatron)





Ion Source

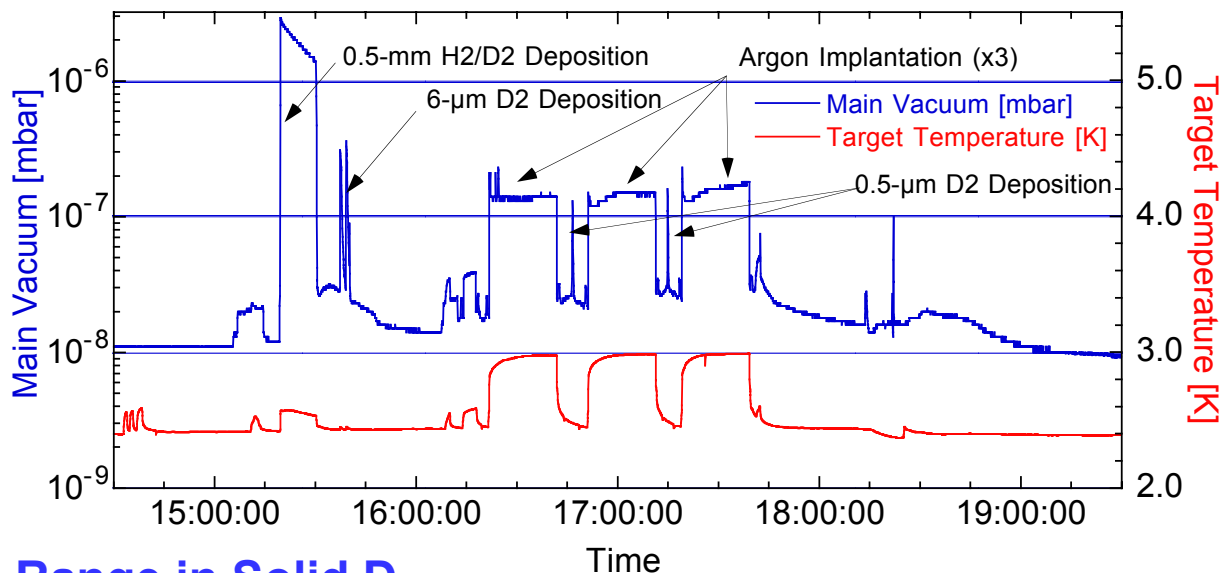
X-Y Steerer

Slits

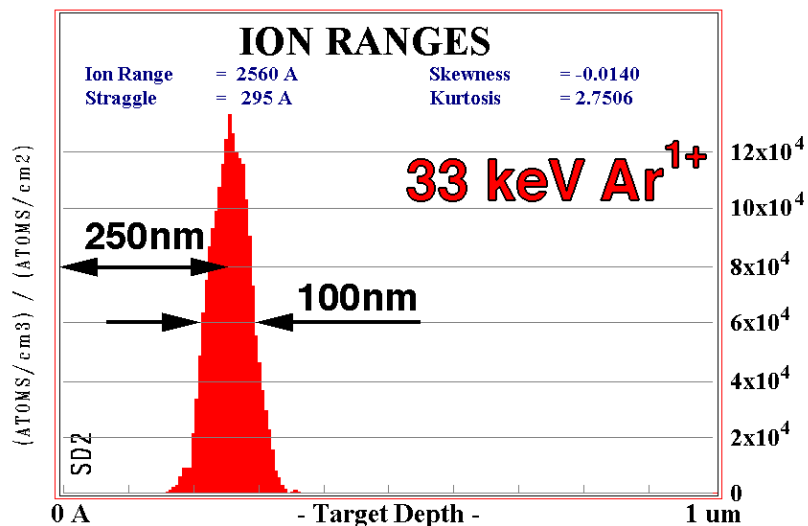
Ion Beam

Beam Profile Monitor

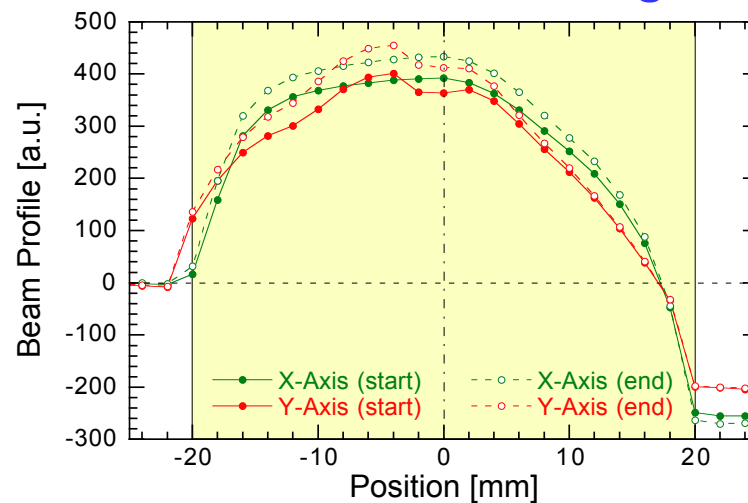
Target Preparation



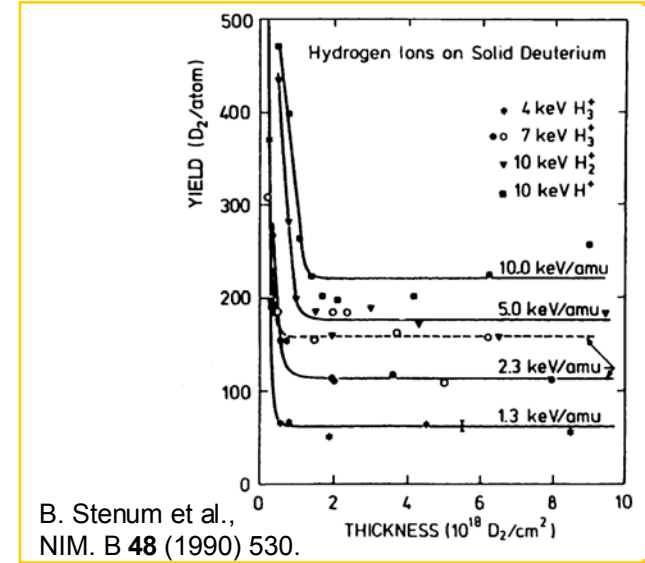
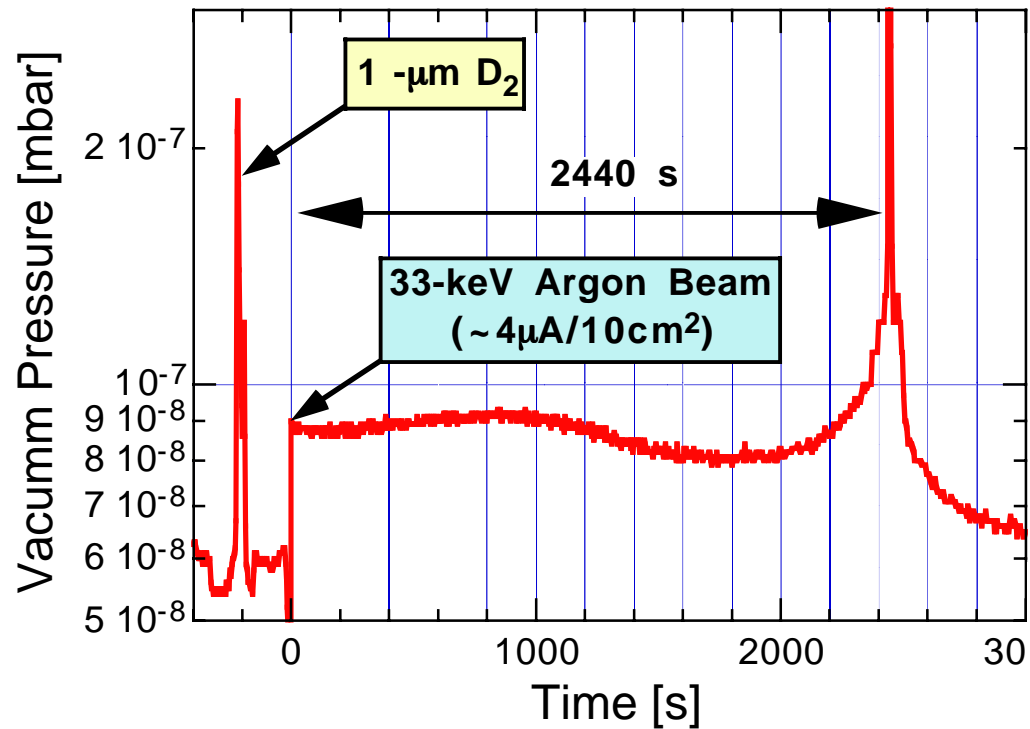
Argon Ion Range in Solid D₂



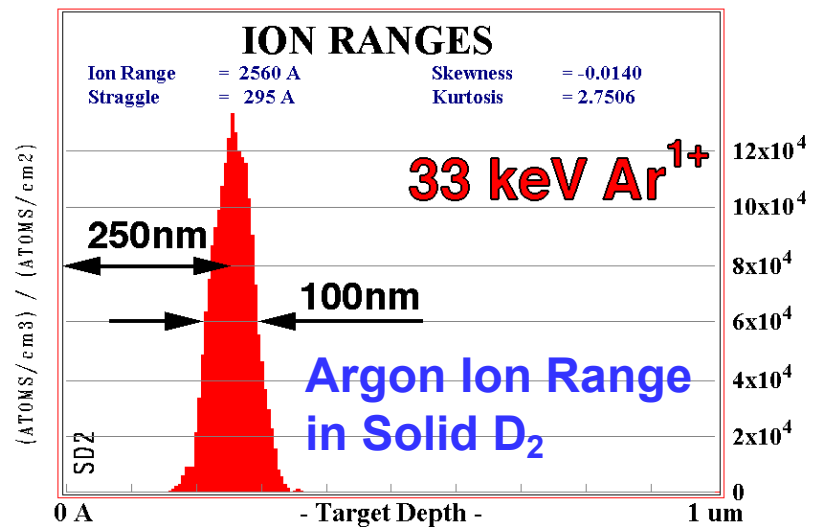
Beam Profile on Target



Sputtering of Solid Deuterium Films

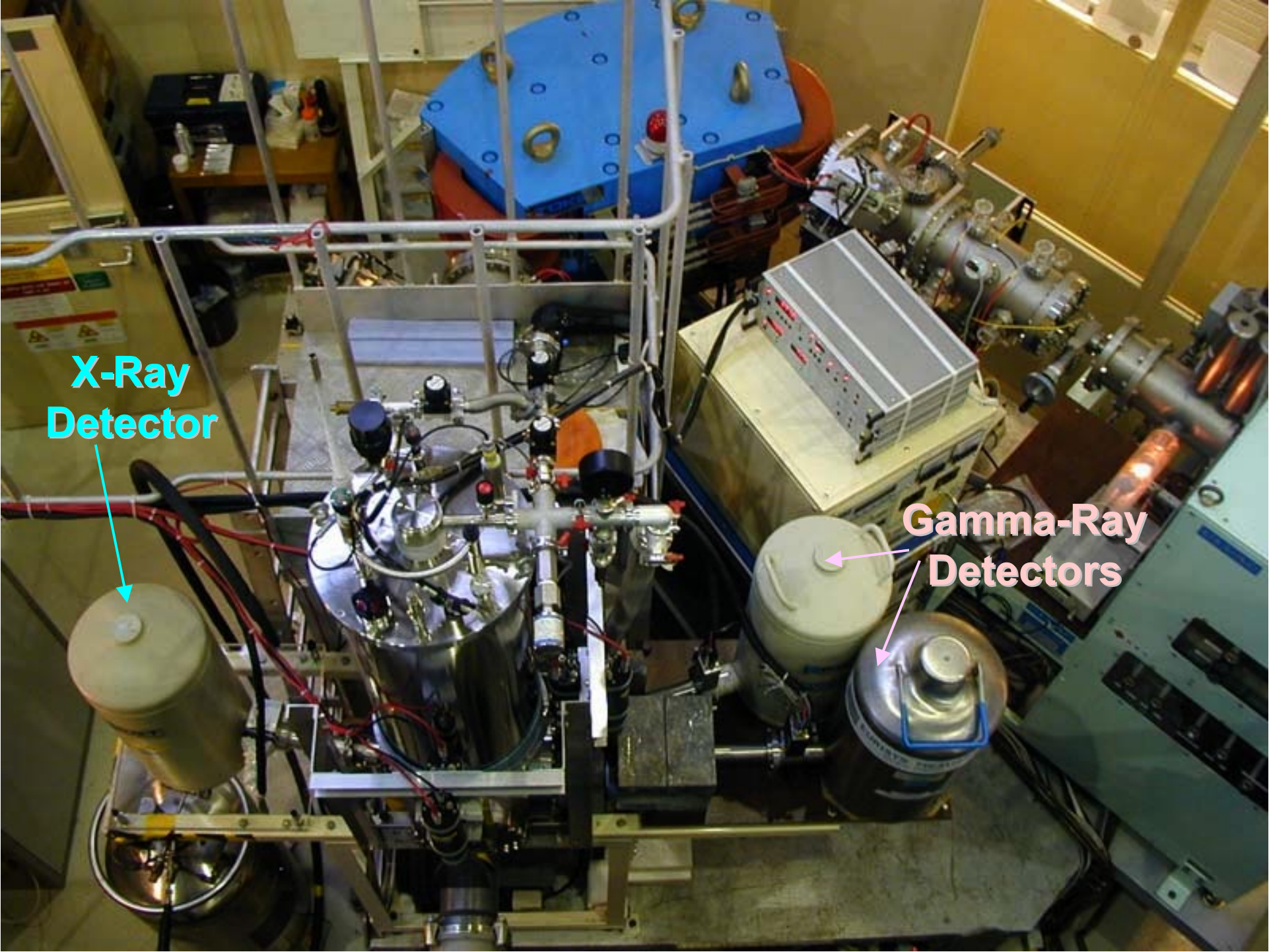


➔ Sputtering Yield $\approx 350 \text{ D}_2/\text{Ar Ions}$
 ($\sim 40 \text{ nm}/\mu\text{A}/\text{cm}^2$)

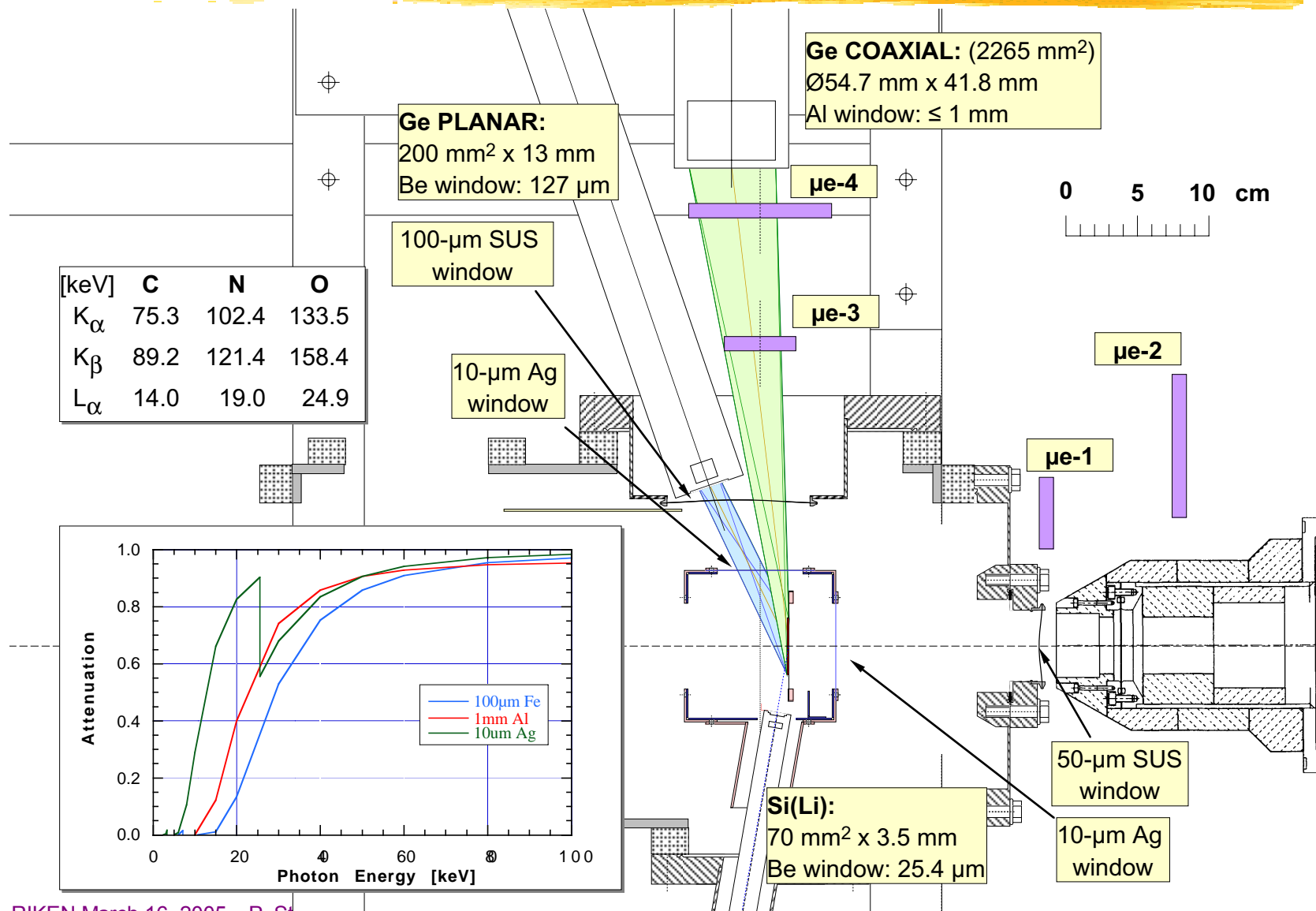


**X-Ray
Detector**

**Gamma-Ray
Detectors**



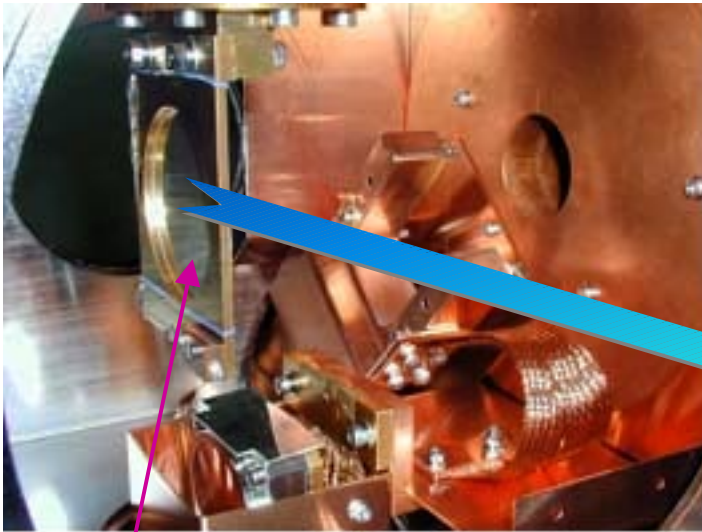
μA^* Setup Detector-Target Layout



Muonic Silver X-Rays



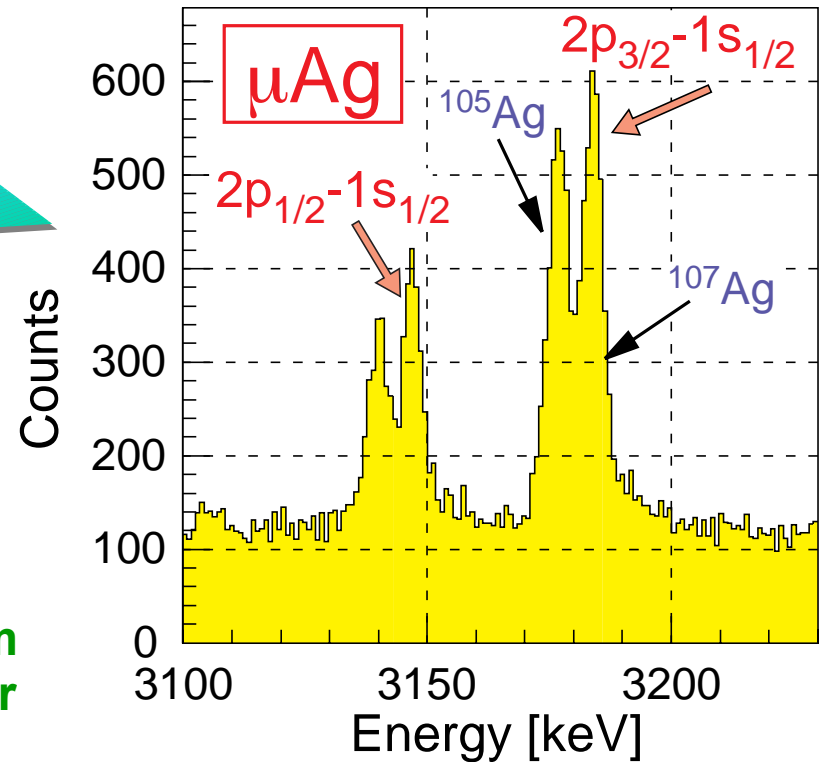
μA* Target System



Cold Foil
(100-μm Ag)

Germanium
γ-Ray Detector

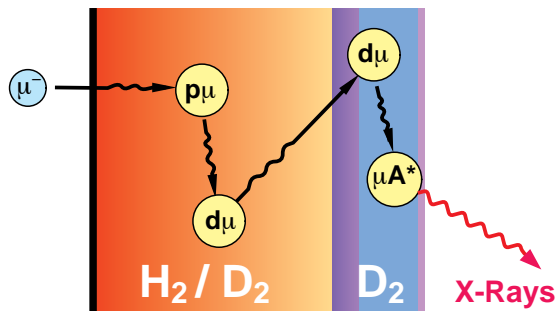
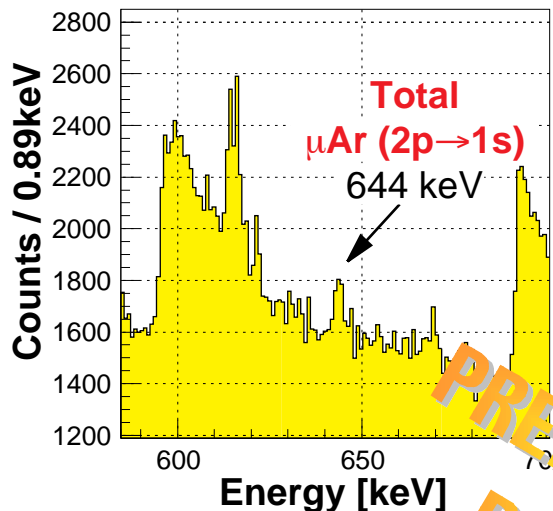
Muonic Silver X-rays from the Cold Foil



(1) 0.5-mm H₂/D₂ + 7- μ m D₂(Ar-multi)

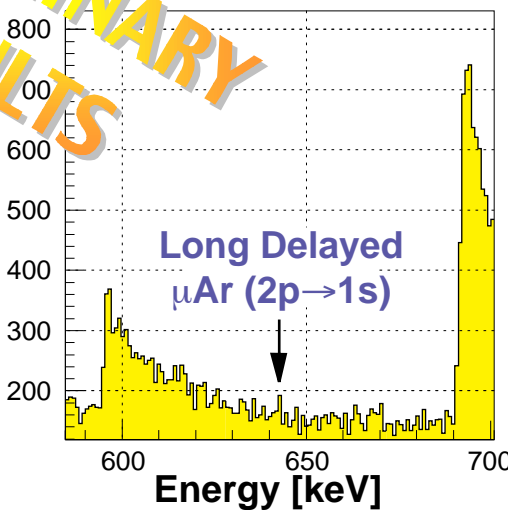
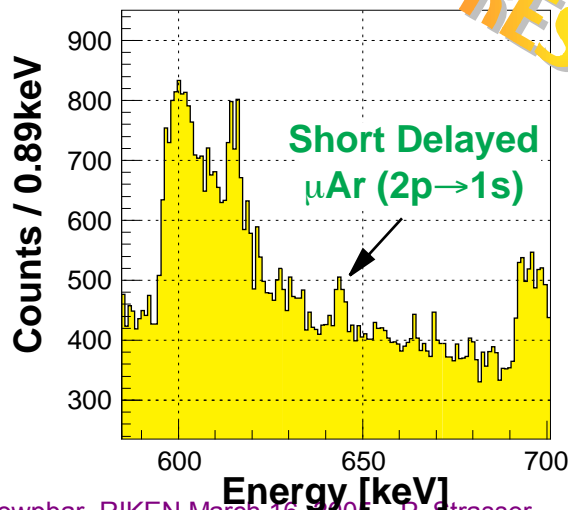
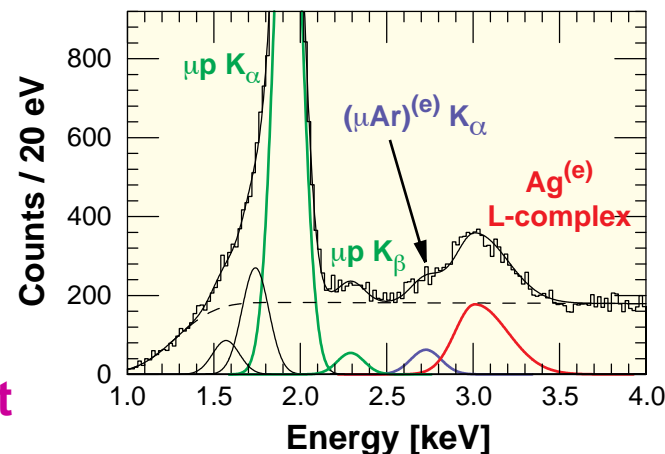


Ge(coaxial) γ -Ray Energy Spectra



Two-Layer Arrangement

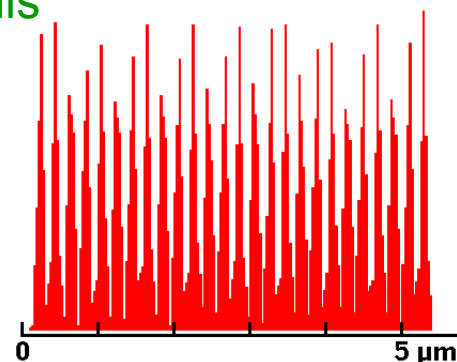
Si(Li) X-Ray Energy Spectrum



PRELIMINARY RESULTS

Implanted ⁴⁰Ar Ions in 5 μ m
~10¹⁶ at/cm² (500 ppm)

12'170 kspills
(67.6 hrs)



$d\mu$ Atom Scattering in Solid Deuterium

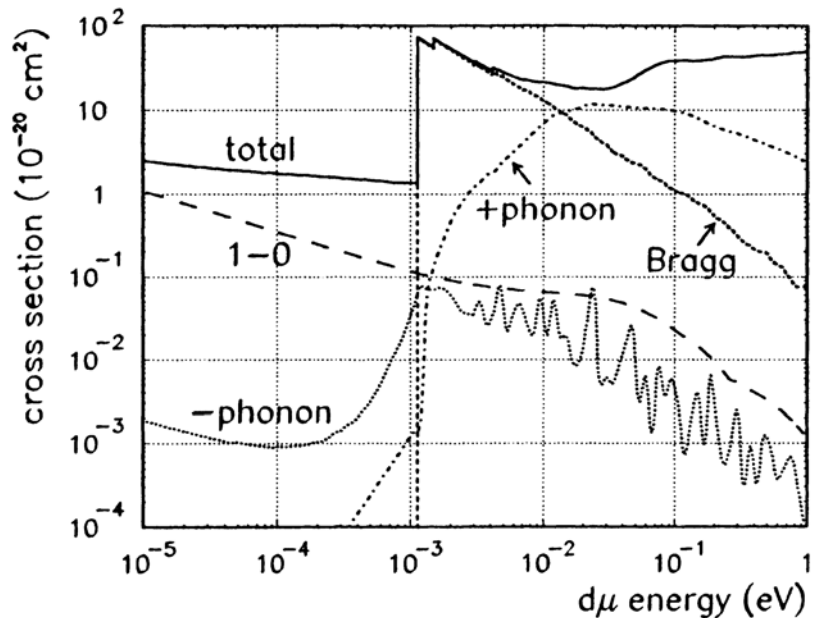
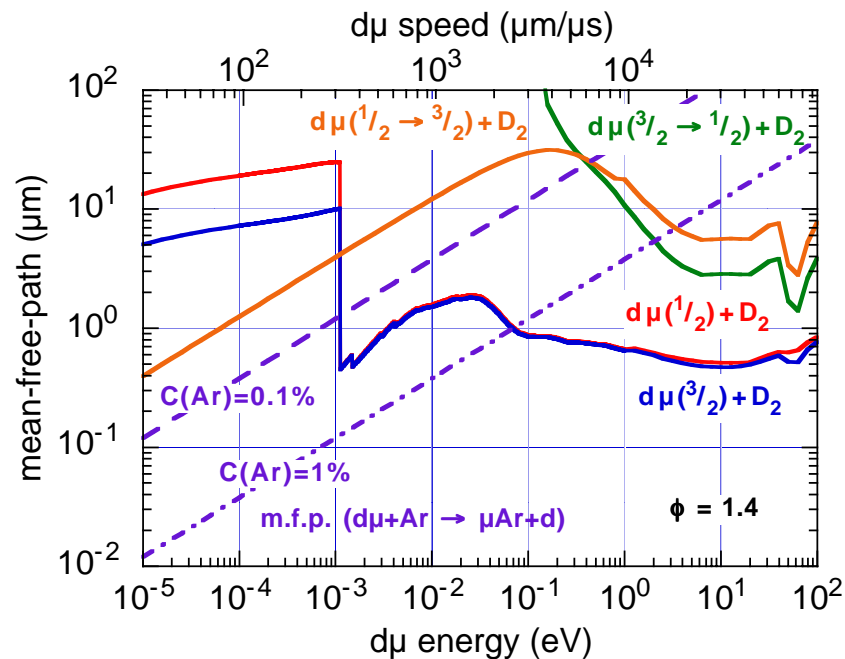


Figure 5. Total cross-section for $d\mu(F = 1/2)$ scattering in 3 K solid deuterium ($K = stat$). The label 1-0 denotes the rotational de-excitation $K = 1 \rightarrow K = 0$.

Deceleration of Muonic Hydrogen Atoms in Solid Hydrogens

A. Adamczak, Hyperfine Interactions **119** (1999) 23.

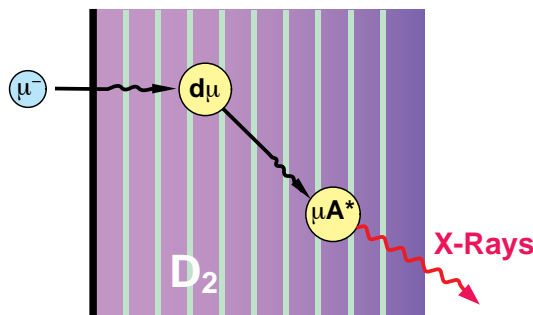
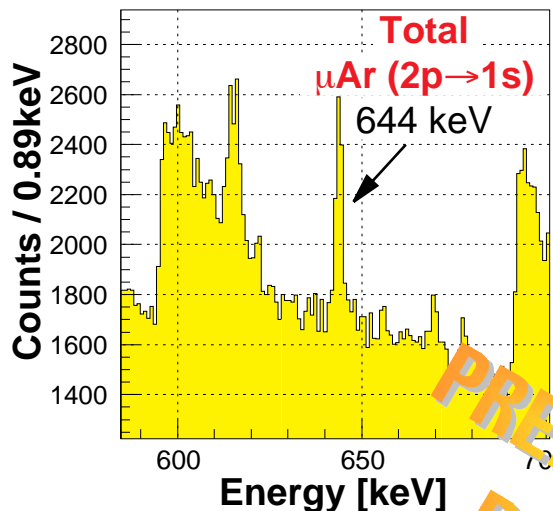
$d\mu$ Mean-Free-Path in Solid D_2



(2) 0.5-mm D₂(Ar-multi)

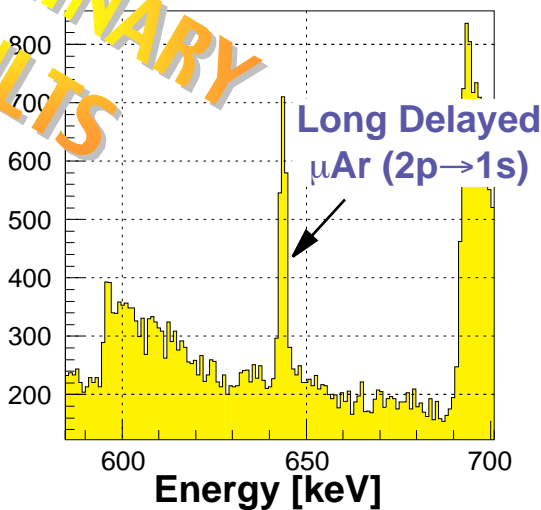
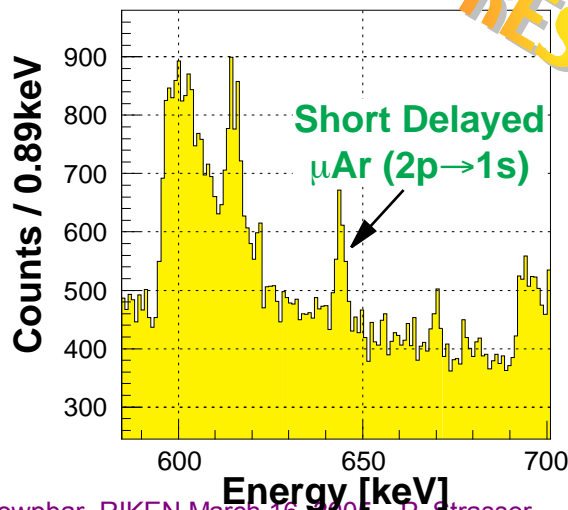
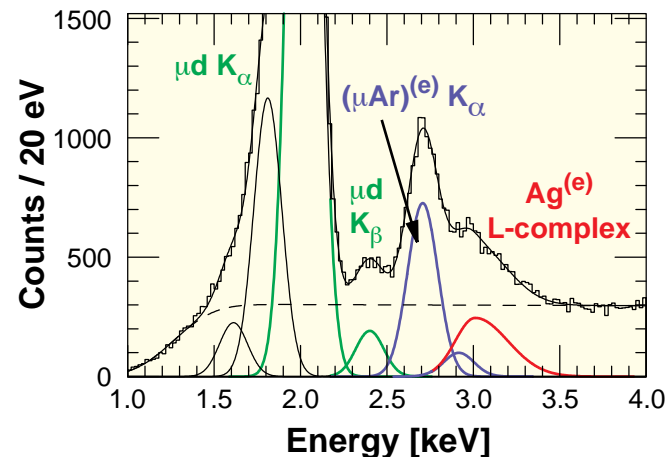


Ge(coaxial) γ -Ray Energy Spectra



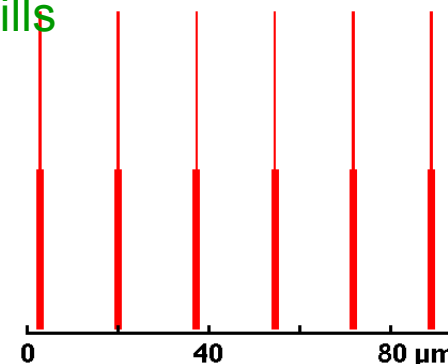
Single D₂ Layer

Si(Li) X-Ray Energy Spectrum



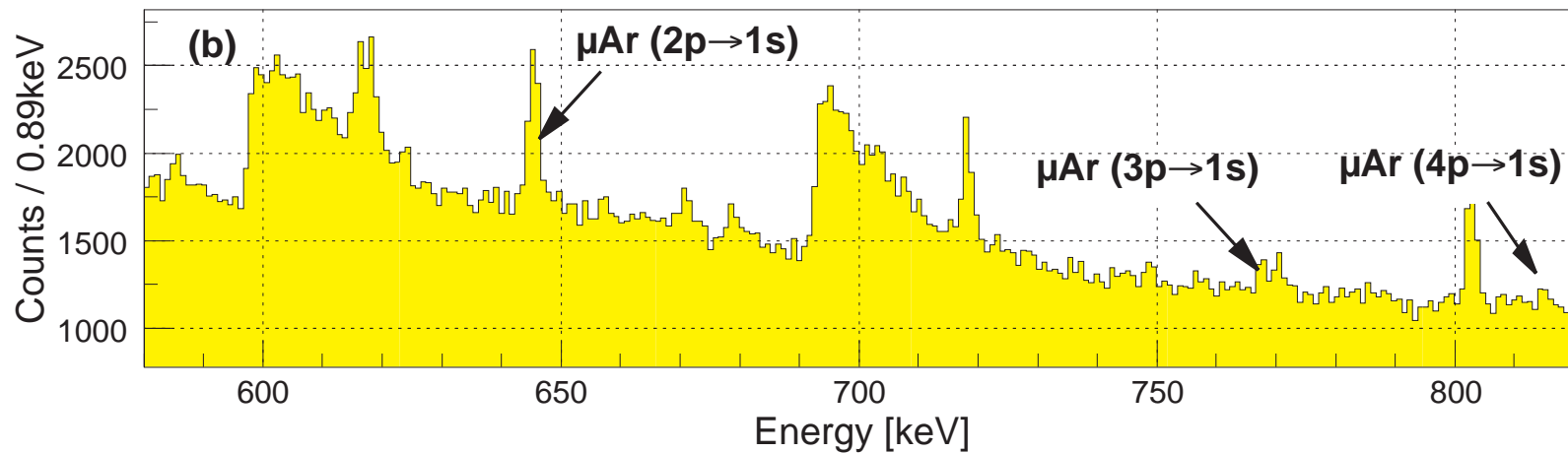
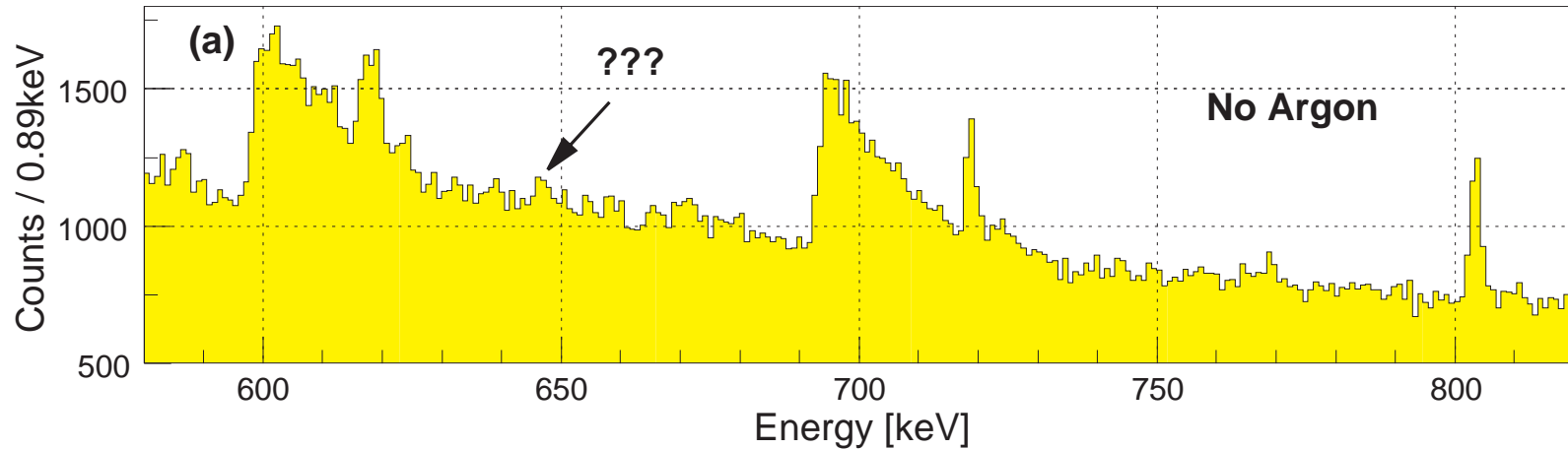
Implanted ⁴⁰Ar Ions in 0.5 mm
~10¹⁶ at/cm² (~ 6 ppm)

12'560 kspills
(69.8 hrs)

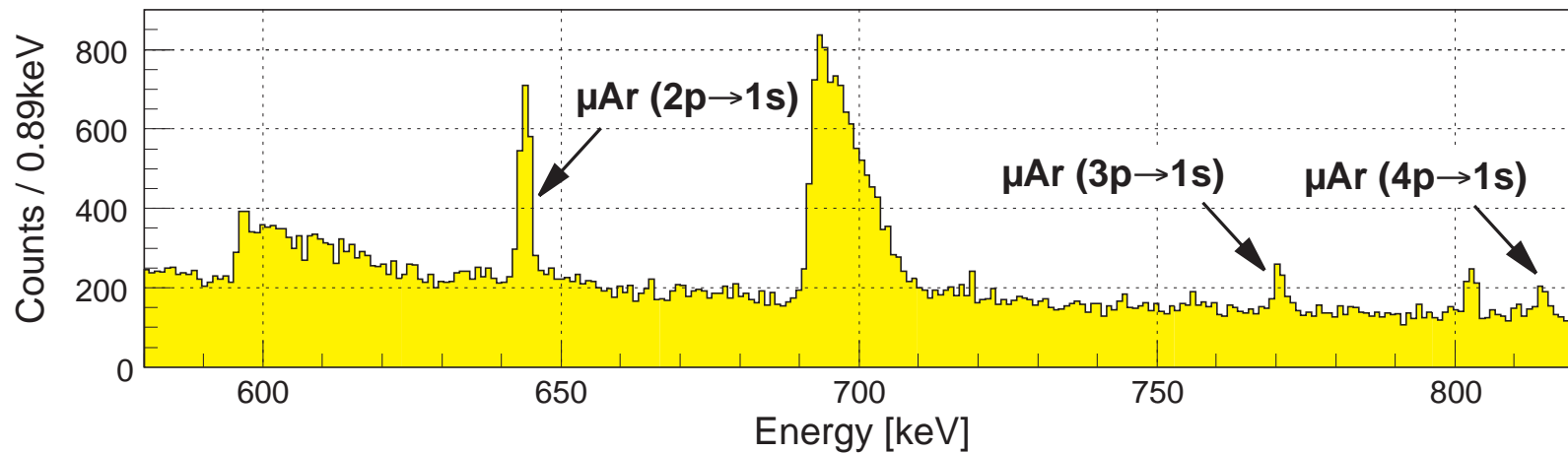
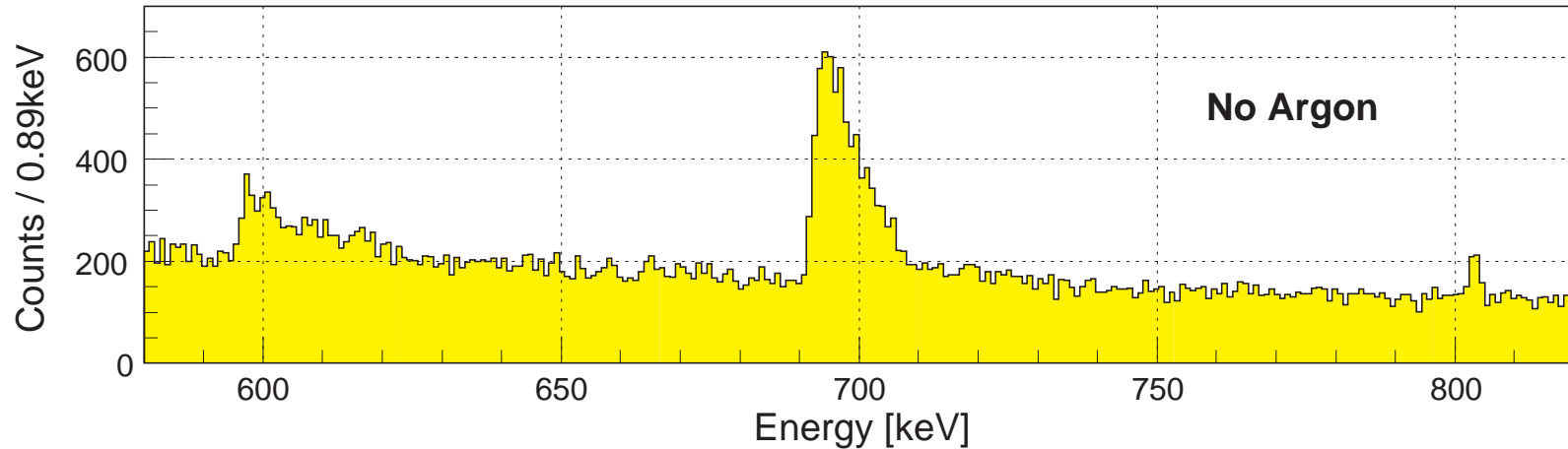


PRELIMINARY RESULTS

Total Energy Spectra (1-mm D₂)



Delayed Energy Spectra (1-mm D₂)

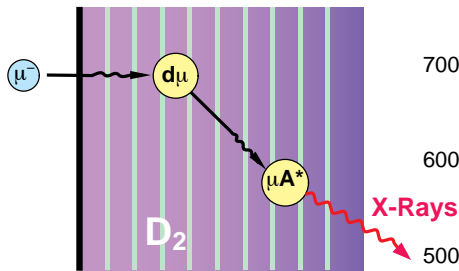


(3) 1.0-mm D₂(Ar-multi)



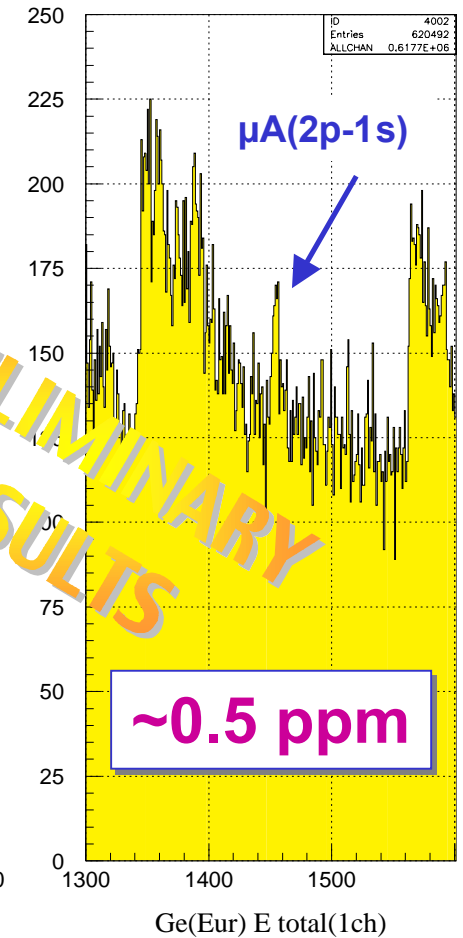
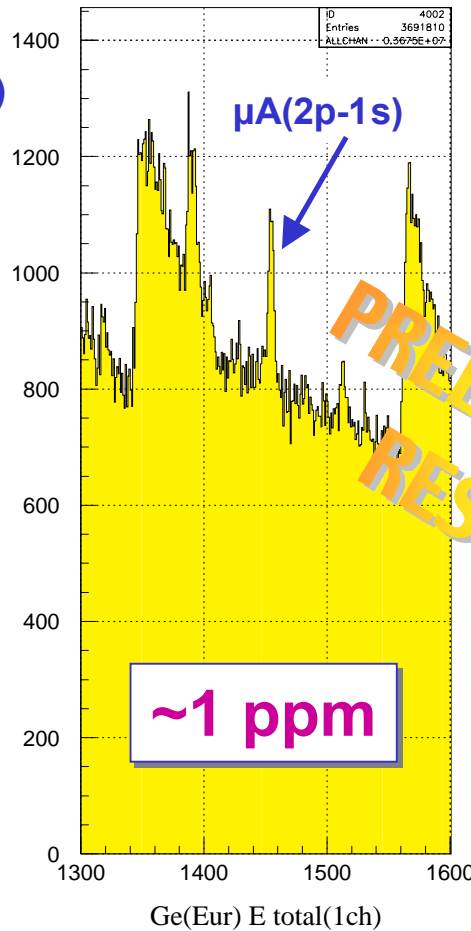
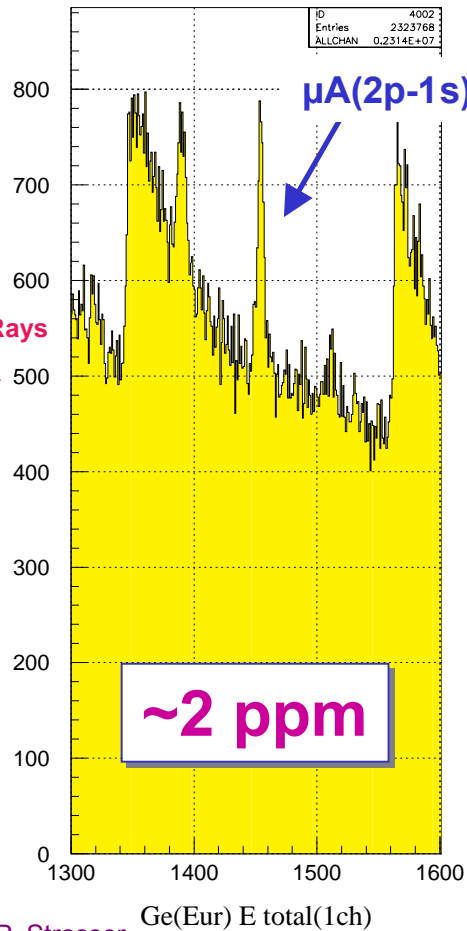
Implantation:	20x	10x	5x
Distance:	50 μm	100 μm	200 μm

Single D₂ Layer



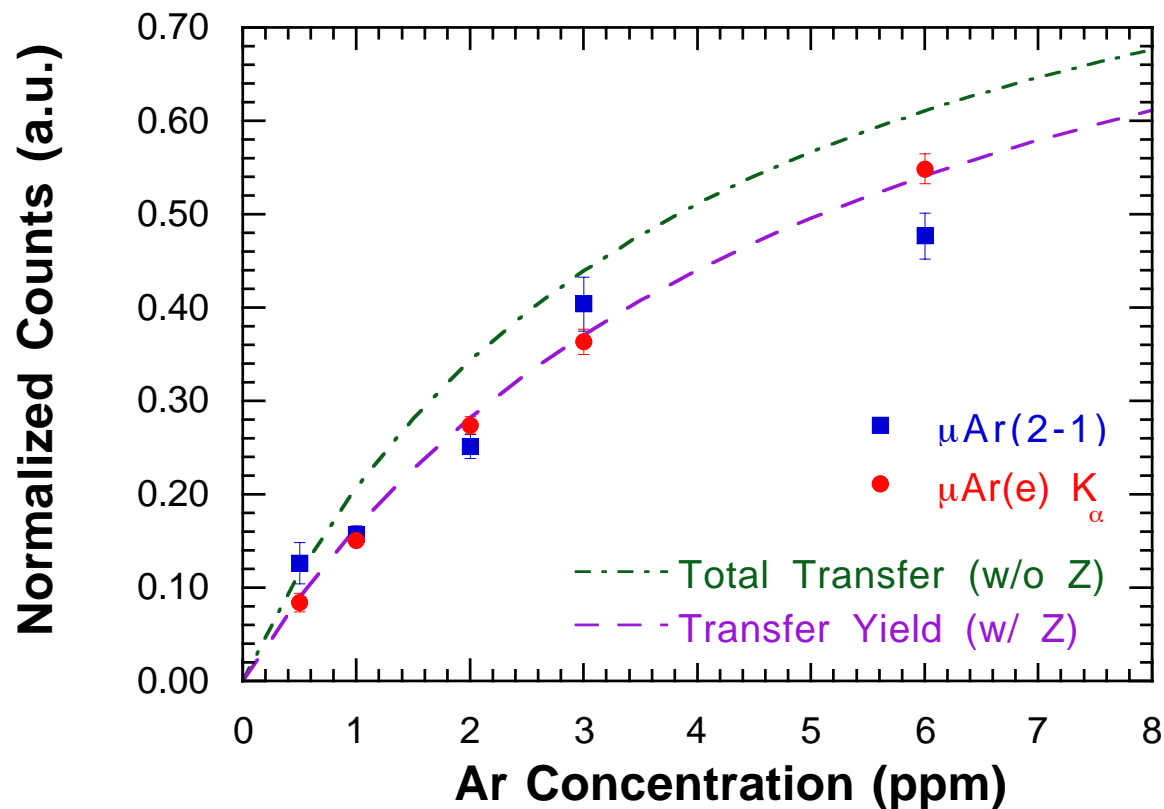
distance between implantation

Total γ-Ray Energy Spectra



PRELIMINARY RESULTS

Transfer Yield



PRELIMINARY RESULTS

Z = Air (N₂, O₂)

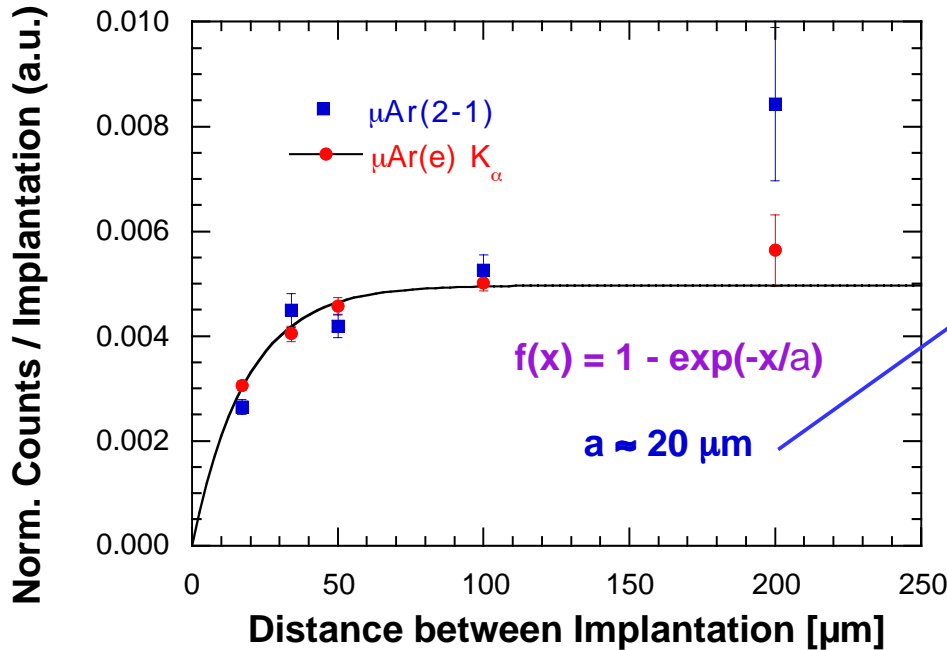
For a uniform target

Normalized data only
No correction applied yet !

$$Y_{dAr} = \frac{\phi C_{Ar} \lambda_{dAr}}{\lambda_0 + \phi C_{Ar} \lambda_{dAr} + \phi C_Z \lambda_{dZ}}$$

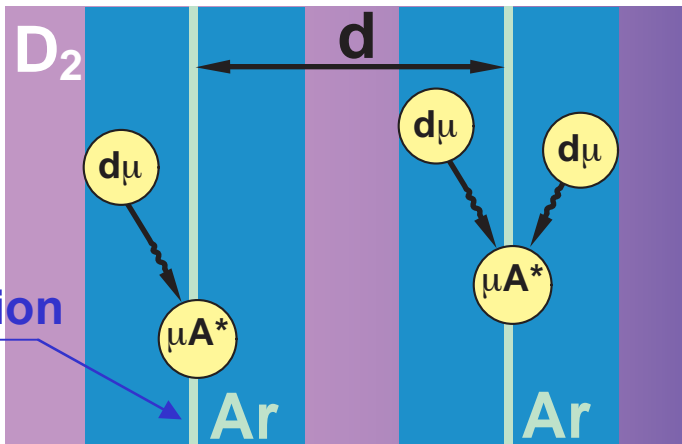
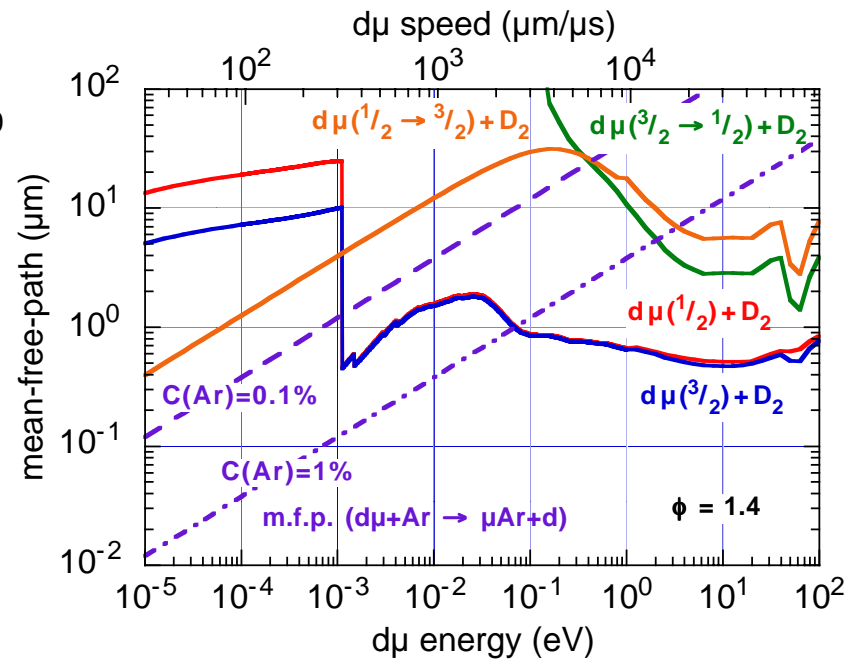


dμ Atom Diffusion in Solid D₂



PRELIMINARY RESULTS

dμ Mean-Free-Path in Solid D₂



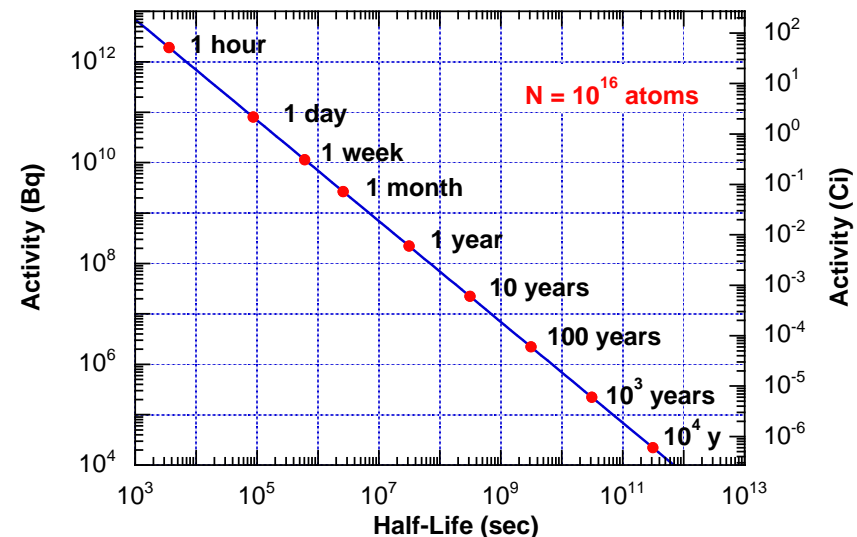
Towards Radioactive Muonic Atoms



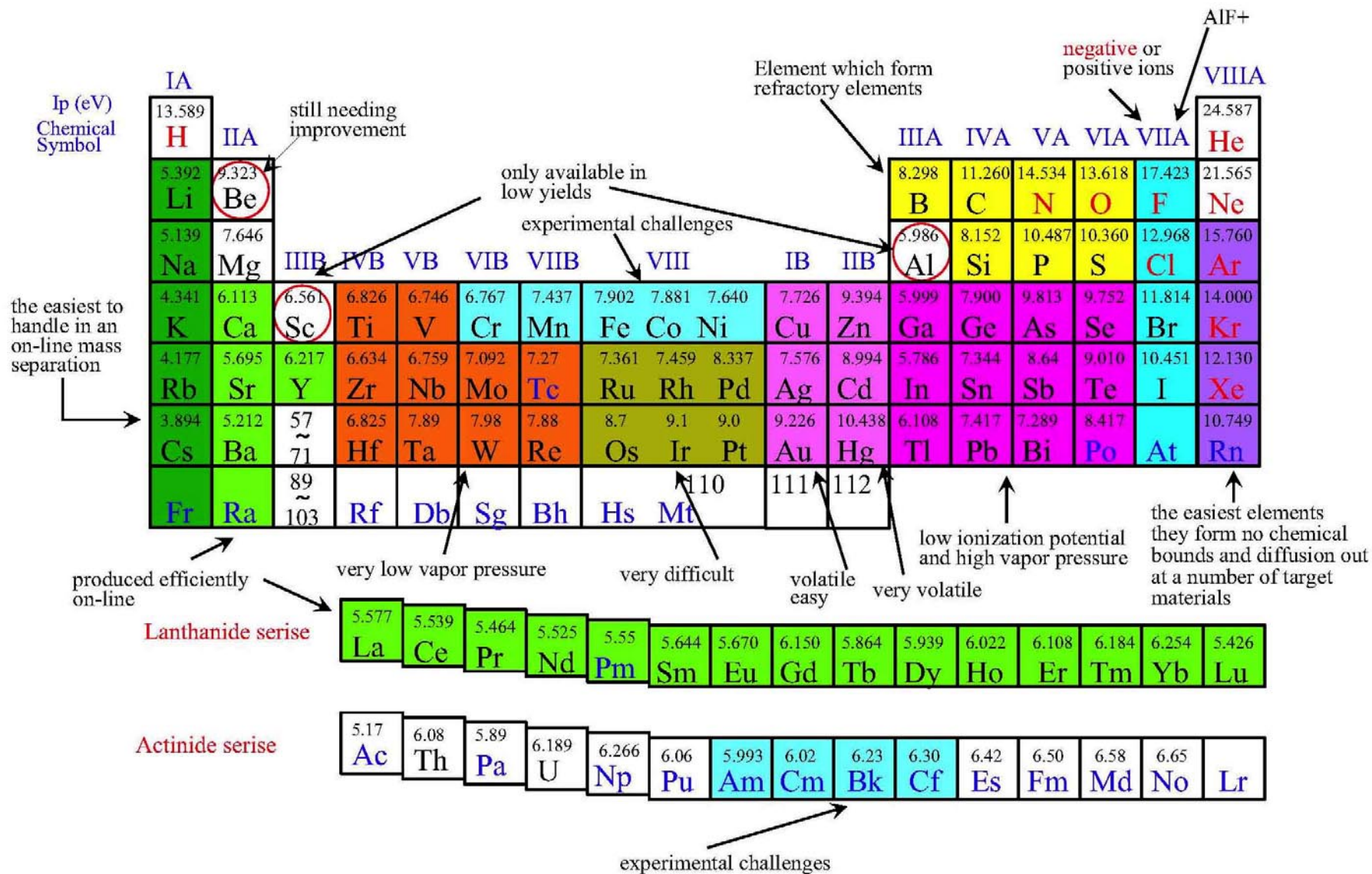
- ◆ Experiment using **LONG-LIVED ISOTOPES** under consideration, e.g., radium isotopes of special interest for P&T violation in atoms (K. Jungmann, KVI).
- ◆ Need a **NEW ION SOURCE** to produce **LONG-LIVED RI BEAMS**.
- ◆ **NOW** at RIKEN-RAL: **10^{16} atoms** needed in $\text{Ø}5\text{cm} \times 1\text{mm D}_2$ target ($3000 \mu^-/\text{s}$).

Possible Improvements: **60 times!**

- ➔ 20 times (1 cm^2 target)
- ➔ 3 times (cloud μ^-)
- ◆ Need **$\sim 100\text{x}$** more in the **ION SOURCE**.
- ◆ **ACTIVITY** versus **HALF-LIFE**.



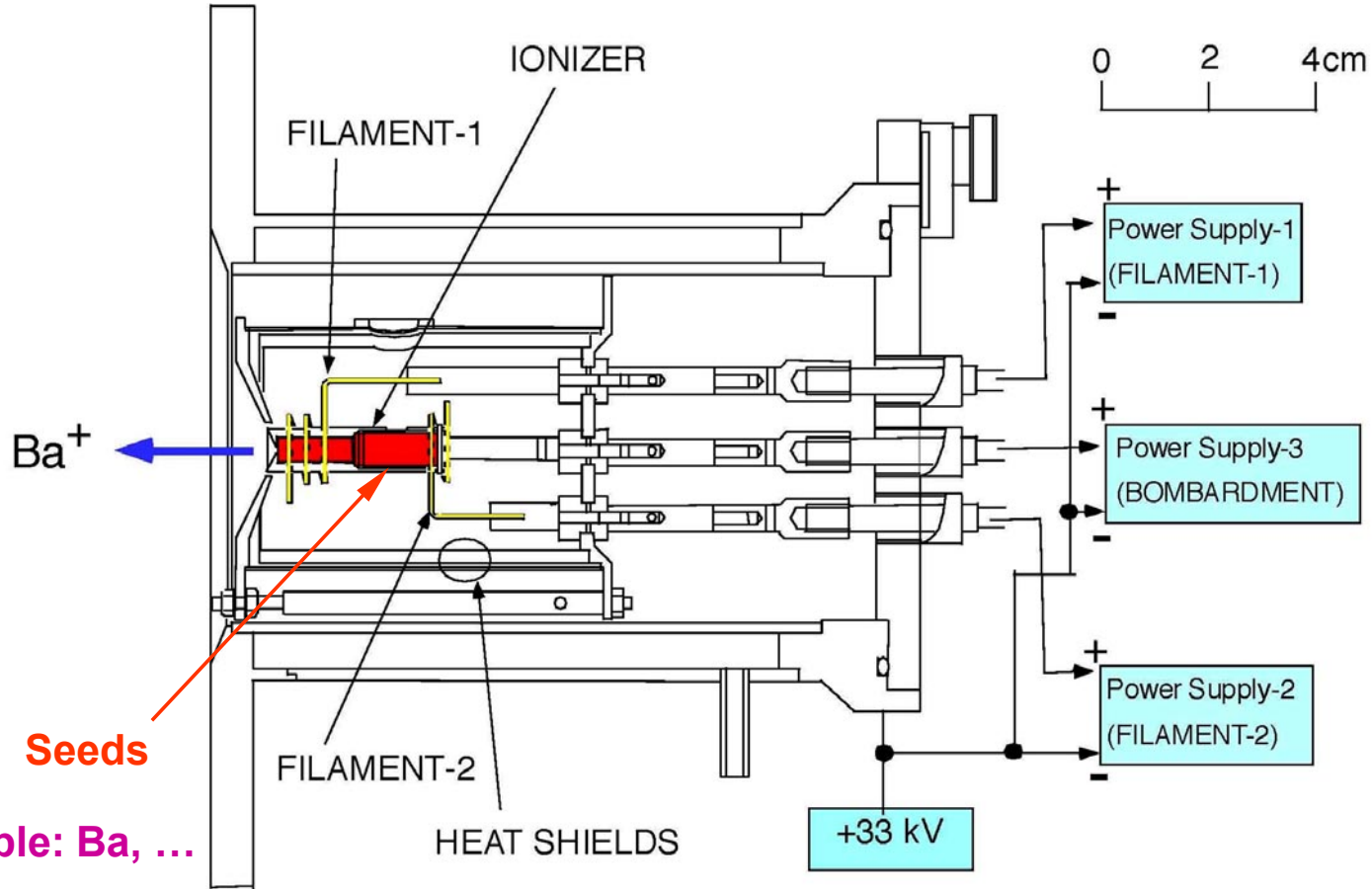
Periodic Table of Elements



New Surface Ionization Ion Source



New Collaborators: A. Taniguchi (Kyoto), S. Ichikawa (JAERI), H. Miyatake (KEK)



First stable: Ba, ...
then Rf

Good for alkali metals & alkaline-earth metals!

IA		
13.589		
H		IIA
5.392		9.323
Li		Be
5.139		7.646
Na		Mg
4.341		6.113
K		Ca
4.177		5.695
Rb		Sr
3.894		5.212
Cs		Ba
Fr		Ra



Future Prospects

Muon Beam Requirement for μA* Experiment:

◆ Muon Stopping in Solid Deuterium

- ➔ Momentum: $\sim 27 \text{ MeV}/c$
- ➔ Width ($\Delta p/p$): $\leq 5 \%$
- ➔ Beam intensity: $> 1 \times 10^{7-8} \text{ s}^{-1}$
- ➔ Beam size: $\leq 1 \text{ cm}^2$

◆ X-Ray and γ-Ray Detection System

- ➔ Muon beam: pulsed
- ➔ Pulse structure: single
- ➔ Pulse width: $\leq 20\text{--}50 \text{ ns}$
- ➔ Repetition rate: $1\text{--}10 \text{ kHz}$

High Intensity Accelerator

◆ Muonic Atoms (in brief)

Transfer Rate:
$$Y_x = \frac{\phi \lambda_z}{\lambda_0 + \phi \lambda_z}$$

We need $\lambda_z \approx C_z Z \times 10^{10} \text{ s}^{-1}$

(approximation)
$$N_z N_\mu \approx \frac{10^{17}}{Z} \quad (\lambda_z \ll \lambda_0)$$

to produce **1 μA* per cm²**.

N_z, N_μ : Z and μ^- in **0.5-mm D₂**

SUPER OMEGA Project (K. Shimomura et al., KEK)



◆ Injection

- ➔ 2 normal solenoids ~ 400mSr
- ➔ Residual magnetic field on the proton beam line ~10 Gauss

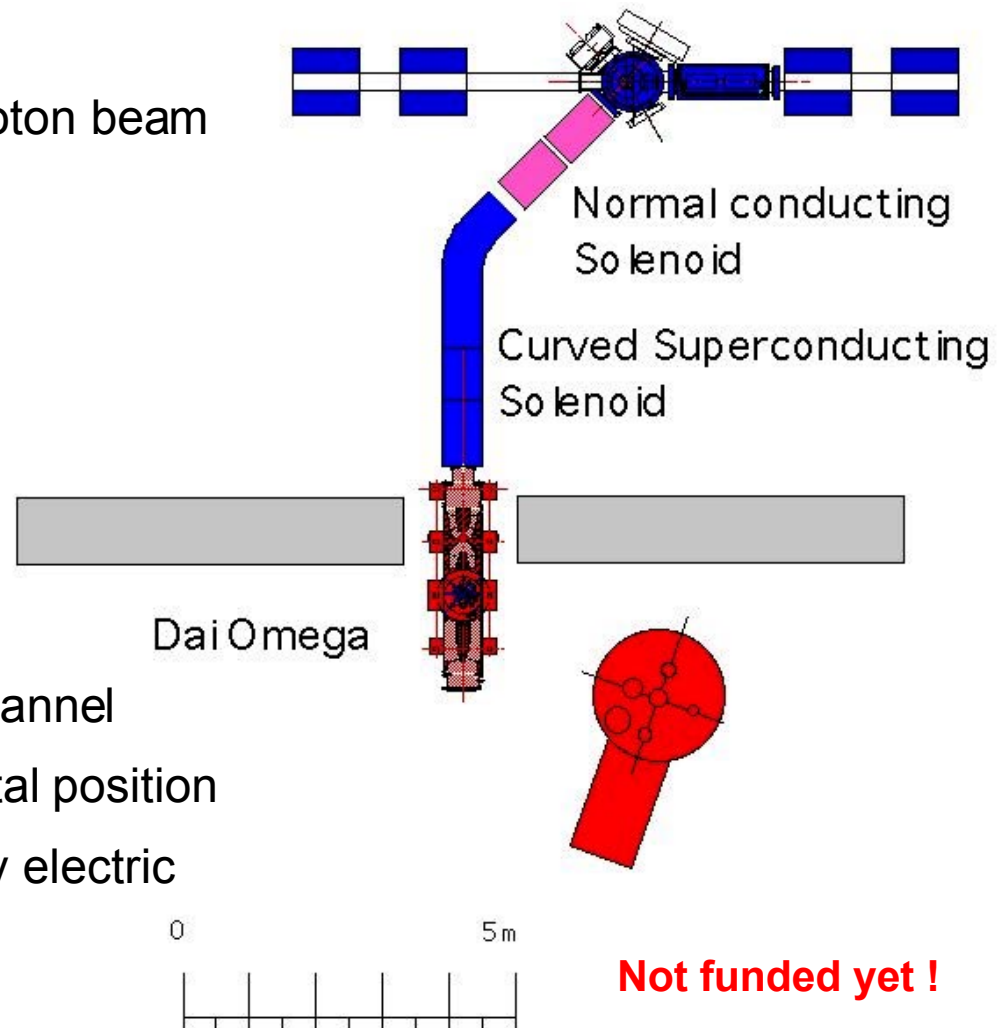
◆ Transport

- ➔ Curved superconducting solenoid
- ➔ Reduction of neutral background
- ➔ Selection of charged particle

◆ Extraction

- ➔ Dai Omega type axial focusing channel
- ➔ Strong focusing at the experimental position
- ➔ Selection of muon and positron by electric separator

at J-PARC Muon Facility



Not funded yet !

SUPER OMEGA Project (K. Shimomura et al., KEK)



◆ Yield Estimation

- ➔ Solid angle: $\sim 400\text{mSr}$
- ➔ Momentum: $27\text{ MeV}/c$
- ➔ Momentum width: $4\text{--}10\%$
- ➔ Surface Muons (μ^+): $2\text{--}5 \times 10^8\text{ s}^{-1}$
- ➔ **Cloud Muons (μ^-): $4\text{--}10 \times 10^6\text{ s}^{-1}$**

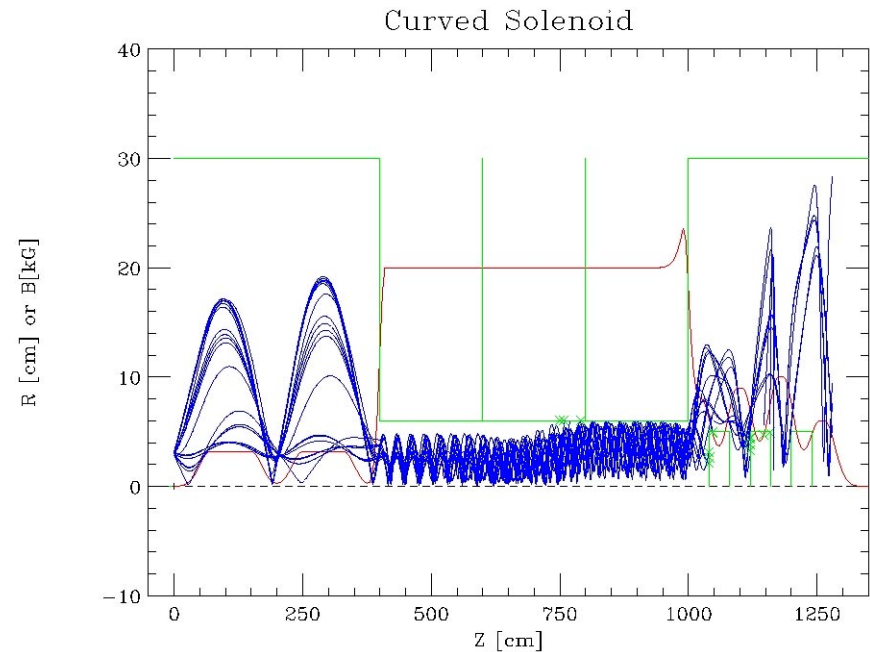
◆ Science (μ^+)

- ➔ Ultra-Slow Positive Muon $2\text{--}5 \times 10^4\text{ s}^{-1}$
- ➔ Muon micro-beam, ...

◆ Science (μ^-)

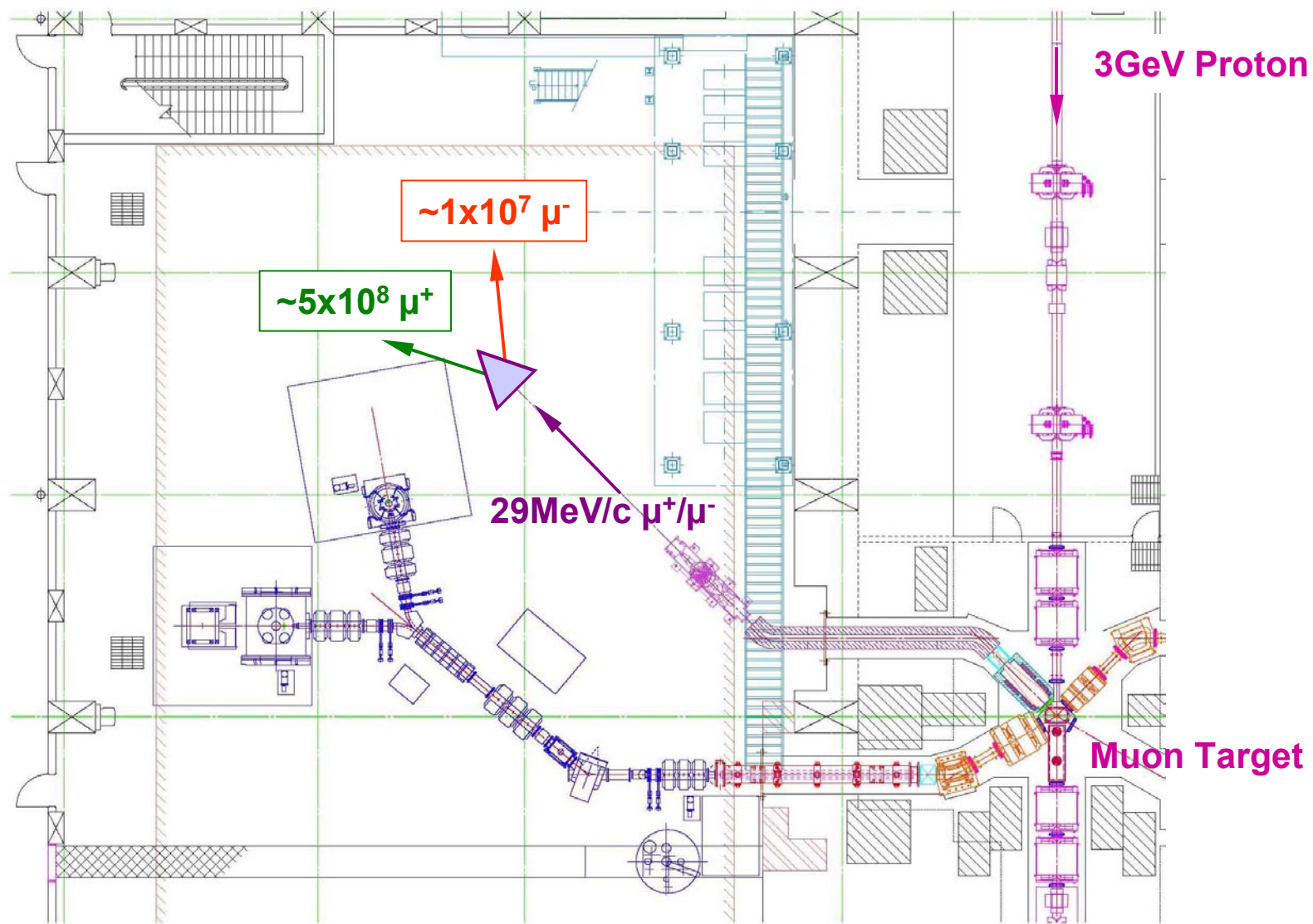
- ➔ μA^* Formation
- ➔ Element Analysis by Muon Spectroscopy
- ➔ ...

Beam Optics Calculation



by K. Ishida (RIKEN)

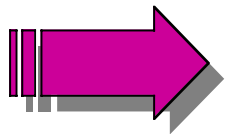
My Dream at J-PARC Muon Facility



Summary



- ◆ **In the near future, investigations of unstable nuclei using muonic atom spectroscopy will become possible at facilities with intense μ^- and RI beams.**
- ◆ **Meanwhile, using dedicated long-lived RI ion source, radioactive muonic atom study will soon be a reality at new intense muon facility.**



There will be a unique opportunity at the new **J-PARC MUON FACILITY.**

and maybe in the near future at a **NEUTRINO FACTORY !**