



Antiproton-Ion-Collider

A Tool for the measurement of both
neutron and proton rms radii

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- Motivation
- Medium energy antiproton absorption
- Antiproton-Ion-Collider
- Cross section measurements
- N/P rms radii, c and a determination

[1] P. Kienle, Nucl. Instr. Meth. B 214 (2004) 191.

[2] H. Lenske and P.Kienle, arXiv:nucl.th/05022065v1, 25.Feb.2005

[3] AIC Technical Proposal to GSI January 2005



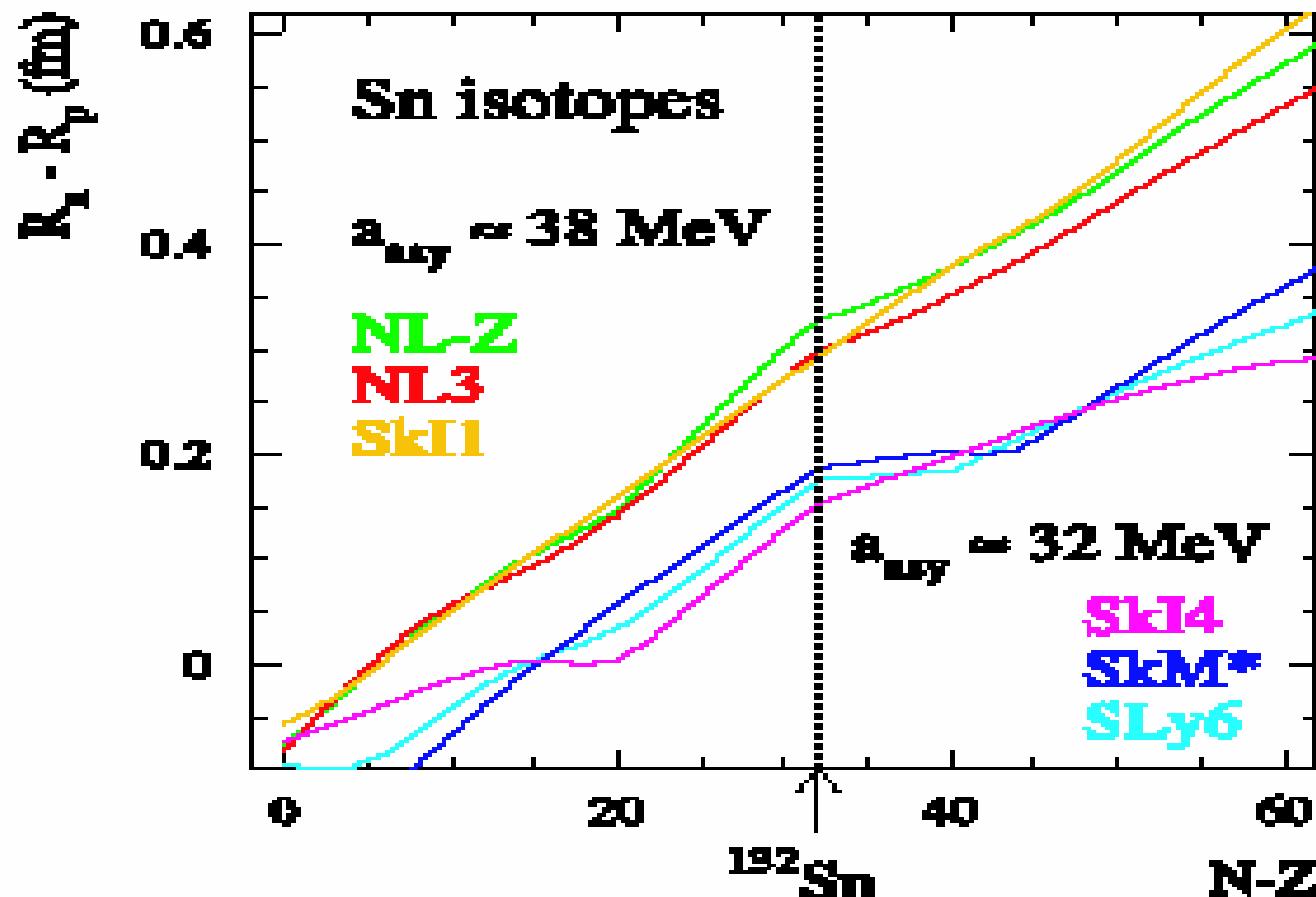
AIC Concept

- 30-100 MeV Antiproton–740A A MeV Ion(variable)
- Modification of e-ion collider
- Addition of antiproton injection and cooling up to $T=100$ MeV
- Fragment detection by Schottky mass spectroscopy and magnetic analysis in NESR
- Luminosity monitor by detection of Rutherford scattered antiprotons



Differences in Neutron and Proton Radii for Sn-Isotopes

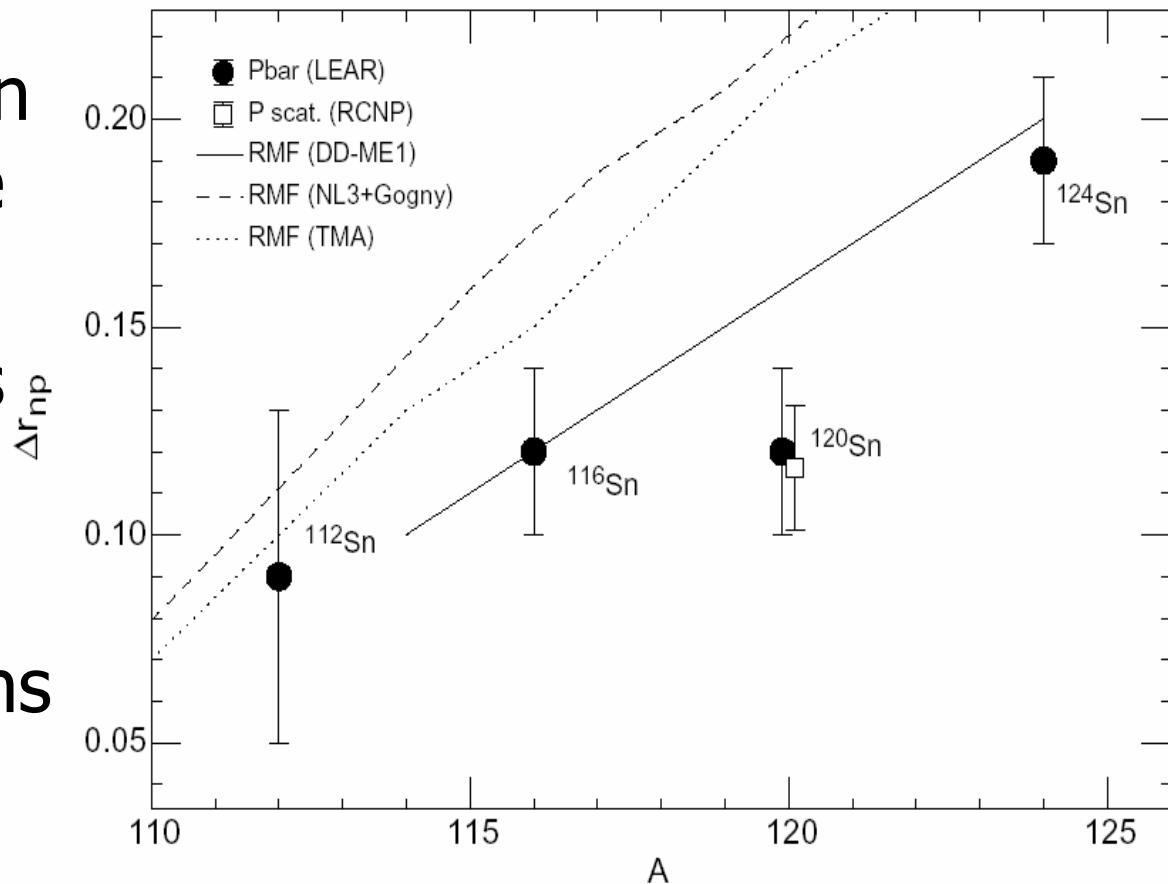
Theoretical predictions





Experimental Methods for rms Radii Differences

- Electron and Proton Scattering, Isotope Shift
- Antiprotonic Atoms
- Charge Exchange Reactions
- Knock-out Reactions



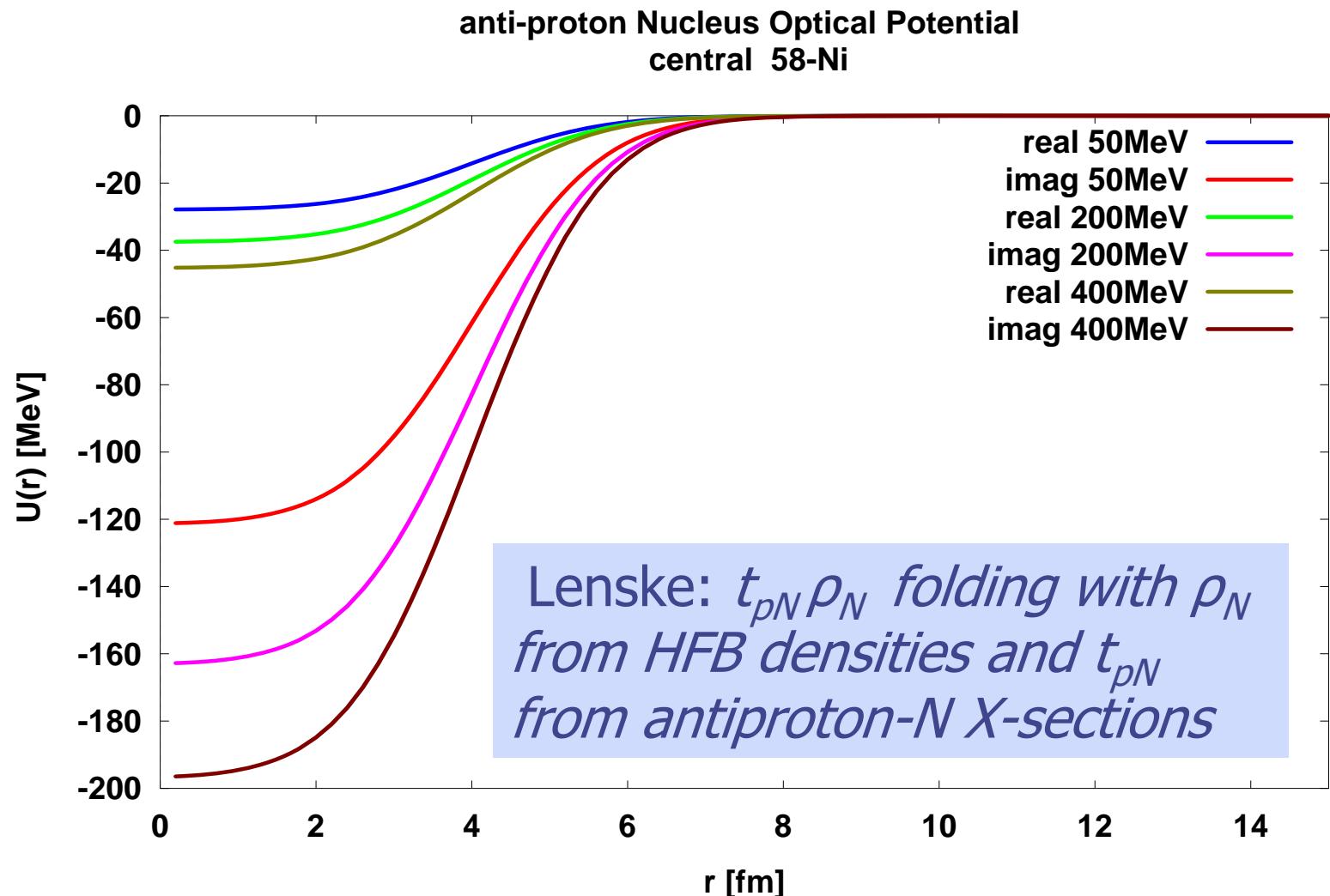


Antiproton Absorption on Neutrons or Protons

- Yields of A-1 isobars with (N-1) or (Z-1) from atomic antiproton absorption
- Absorption radius undefined
- Not directly applicable for RI-beam-nuclei
- Yields of A-1 Isobars with (N-1) or (Z-1) from medium energy antiproton absorption
- Absorption proportional to $\langle r^2 \rangle_n$ and $\langle r^2 \rangle_p$ respectively at high enough energies
- From energy dependence of absorption, c_n, a_n, c_p, a_p of Fermi distribution

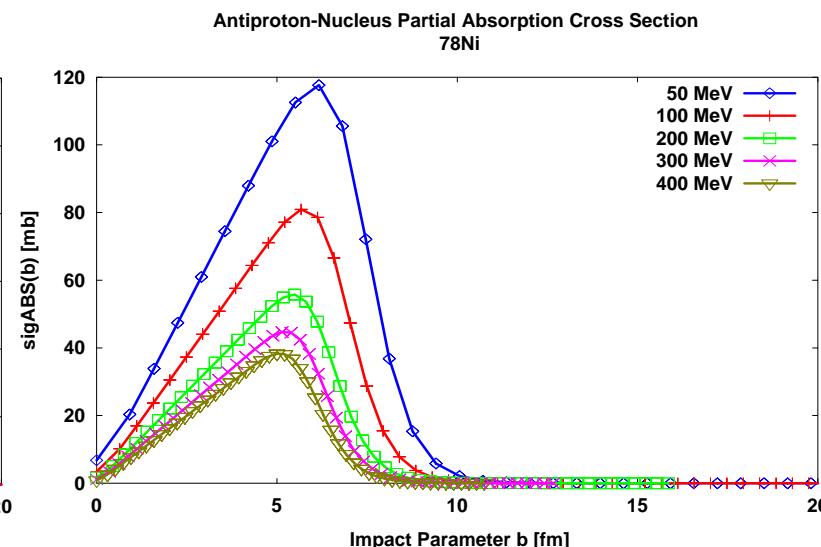
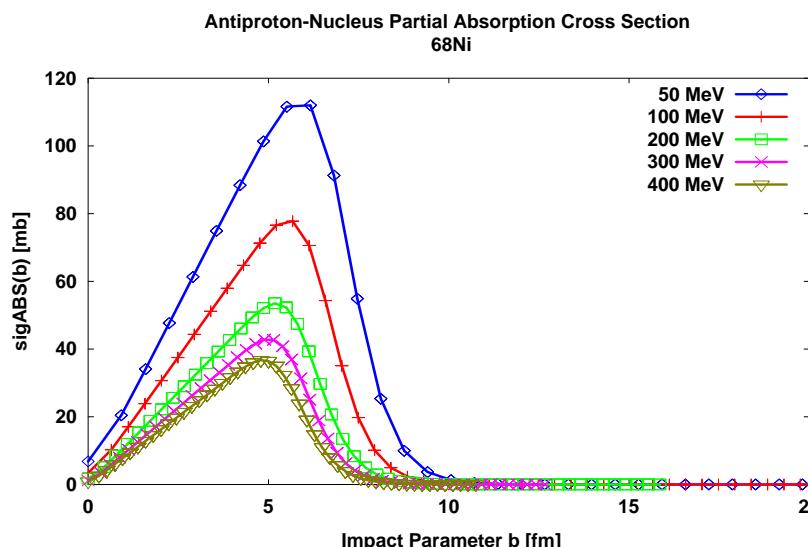
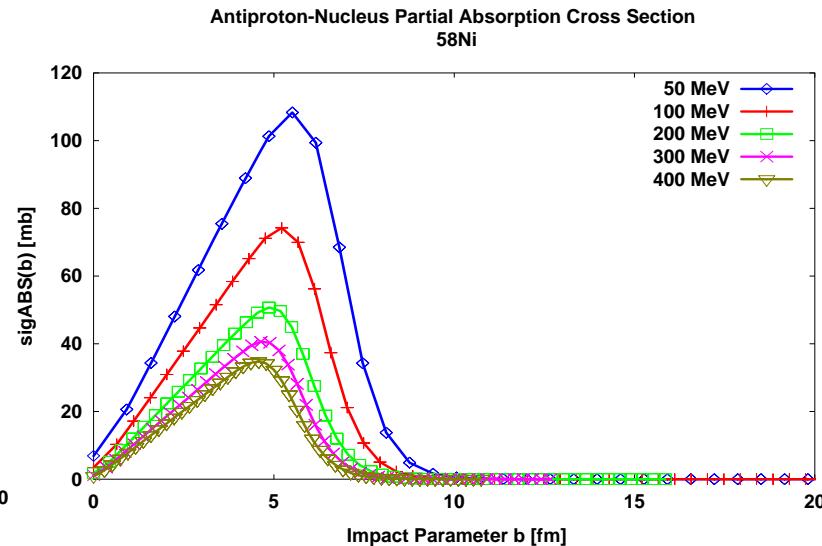
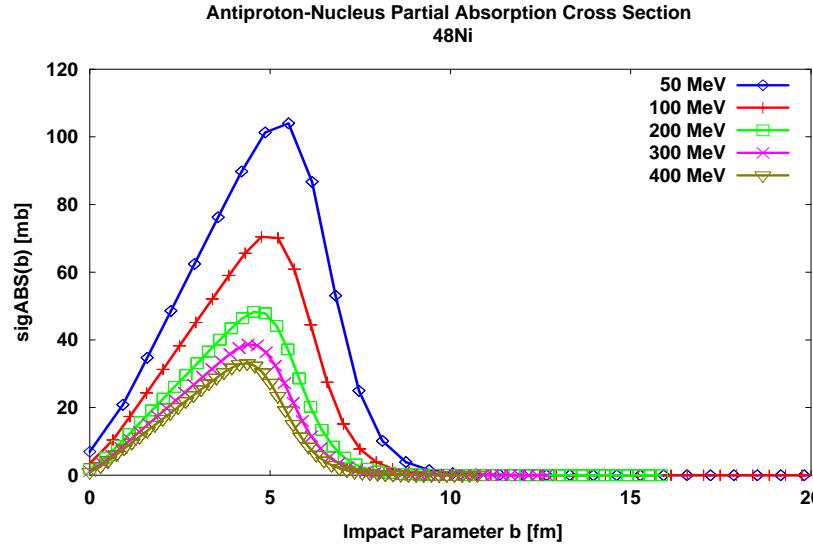


Antiproton optical potential, ^{58}Ni



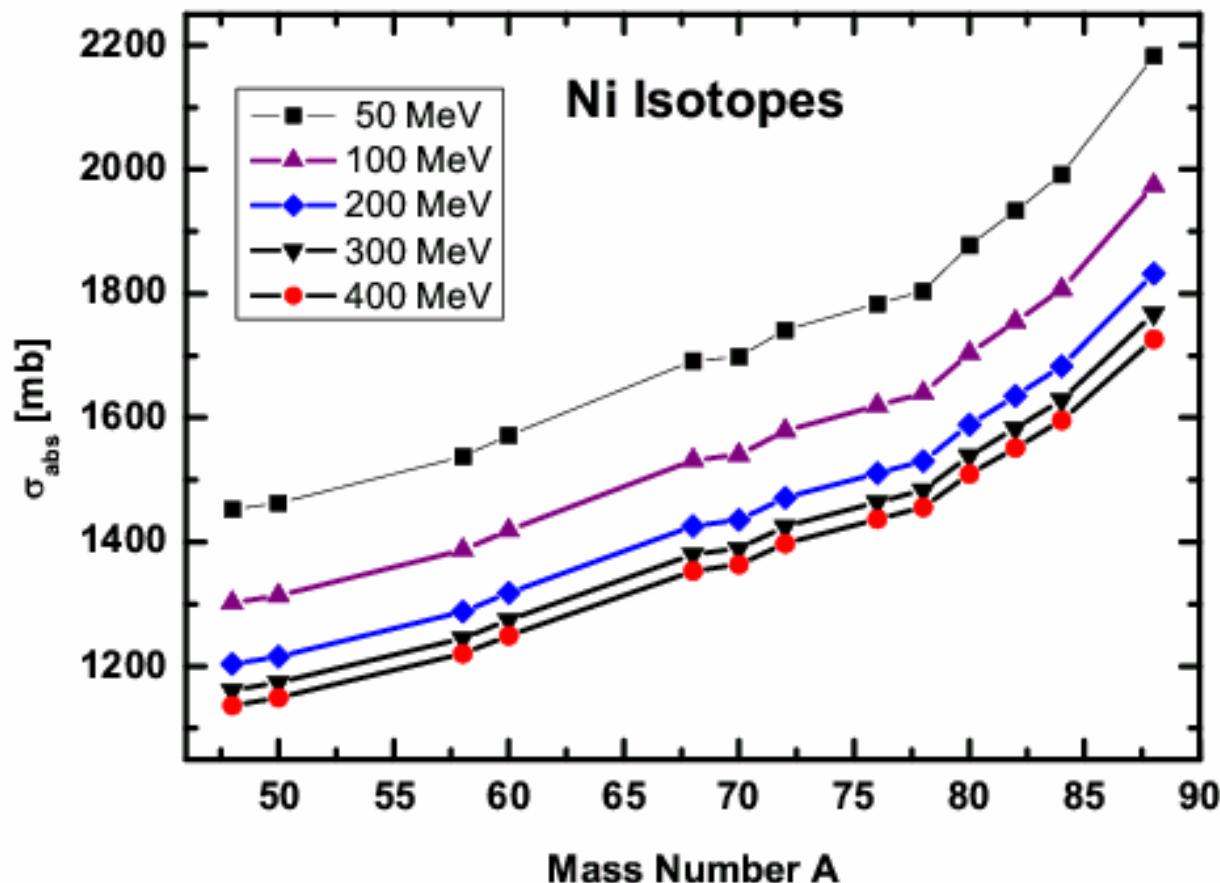


Impact Parameter Dependence





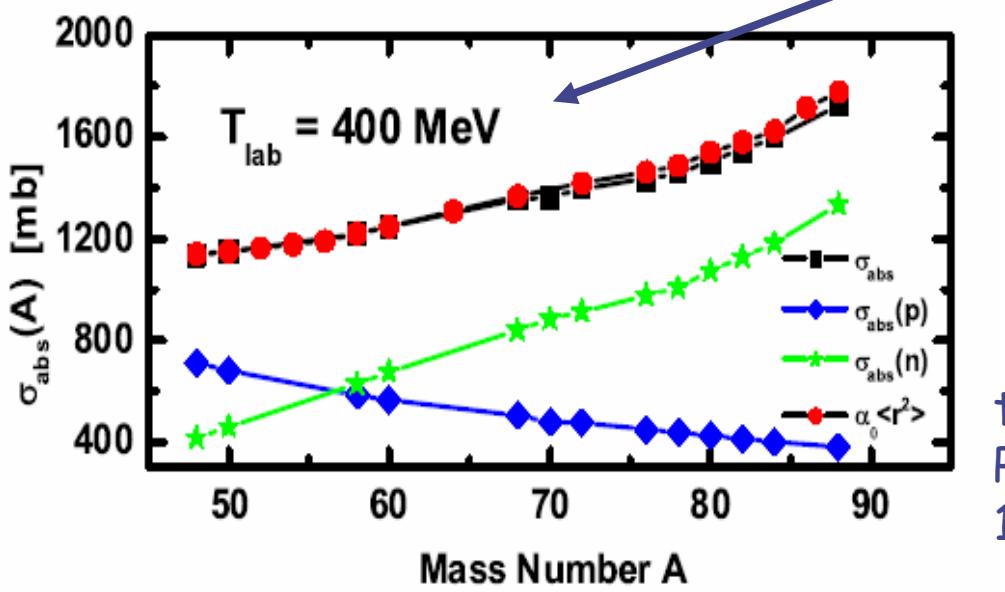
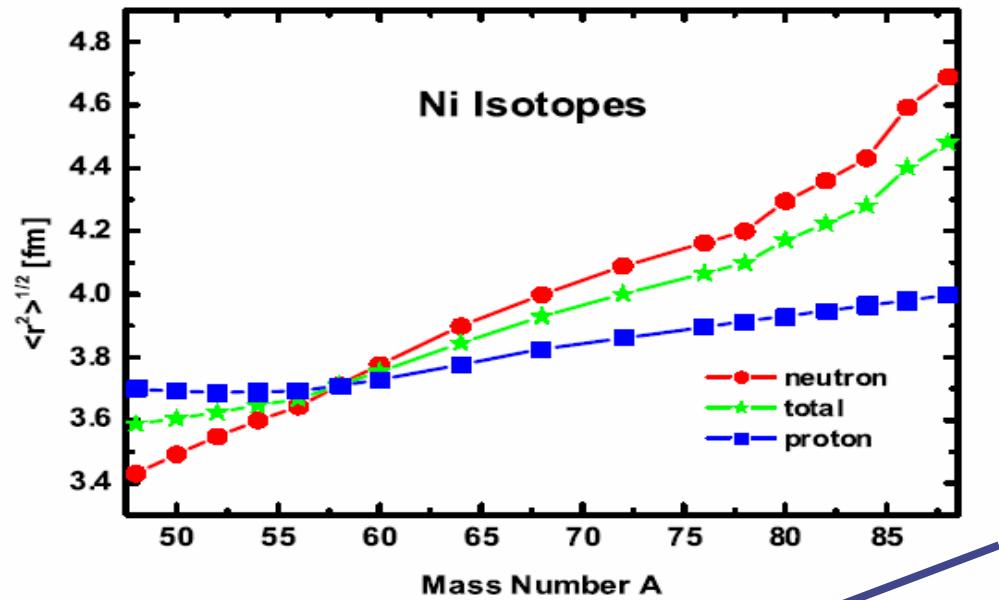
Energy Dependance of Absorption in Ni



- At high energies X-section saturates at geometrical limit
- At lower energies tails of nucleons contribute



$\langle r^2 \rangle_{t,n,p}$ and $\sigma_{t,n,p}$ for Ni Isotopes



$$\sigma_R^{\text{total}} = C \langle r_{n+p}^2 \rangle$$

$$\sigma_R^n = C \langle r_n^2 \rangle$$

$$\sigma_R^p = C \langle r_p^2 \rangle$$

with C from theory

H.Lenske,P.Kienle
 $t_p = t_n$, T.Eliooff et al.
Phys,Rev.
128,869,(1962)₉

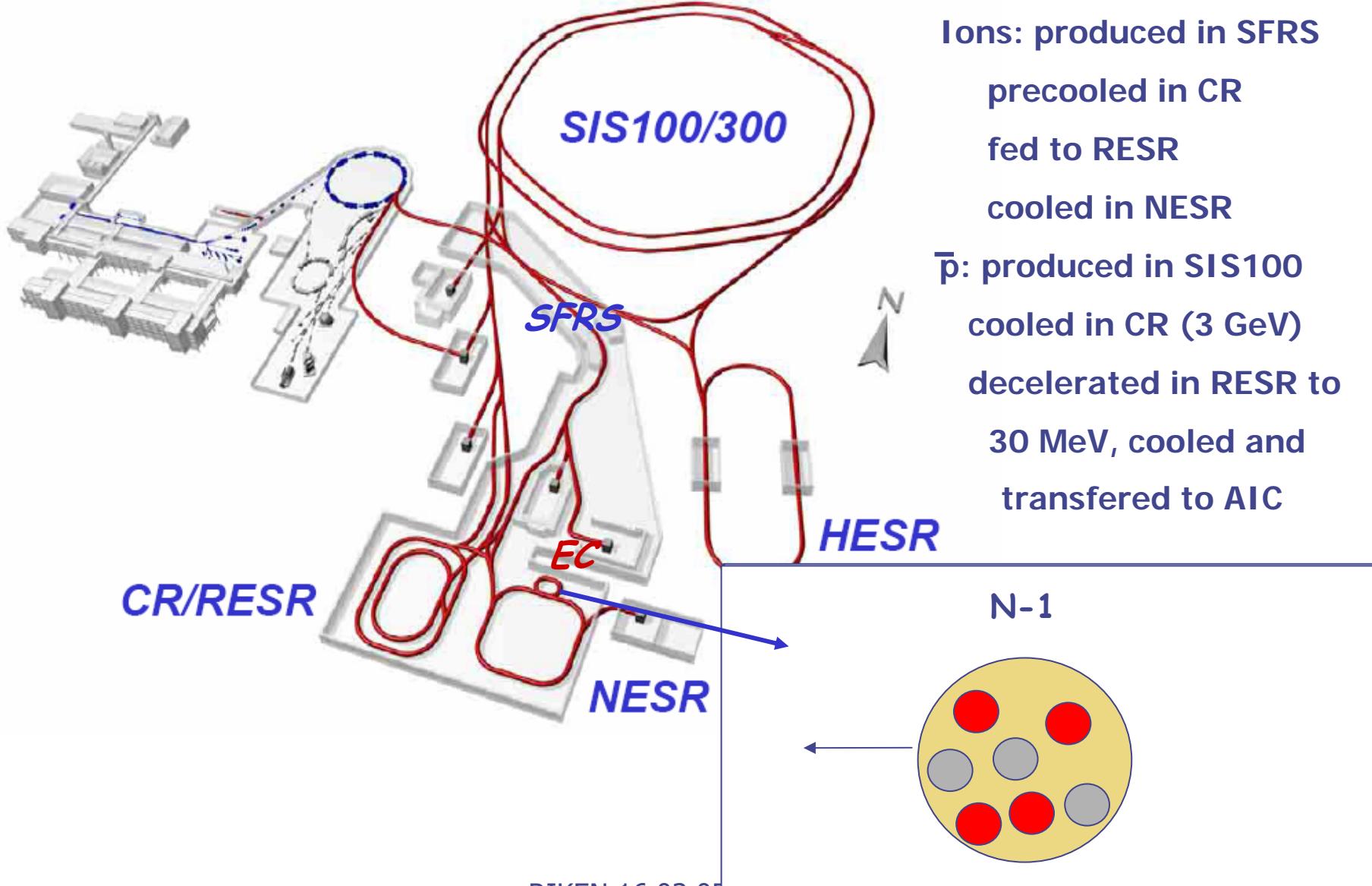


Determination of Parameters of Fermi Distribution: $c_n, a_n; c_p, a_p$

- The energy dependence of $\sigma_n(T)$ and $\sigma_p(T)$ can be measured
- At high T cross sections are determined by c_n and c_p respectively
- At low T the tails of the Fermi distributions contribute
- The cross sections at low T are determined by c_n and a_n , and c_p and a_p
- A detailed analysis of $\sigma_n(T)$ and $\sigma_p(T)$ is in progress

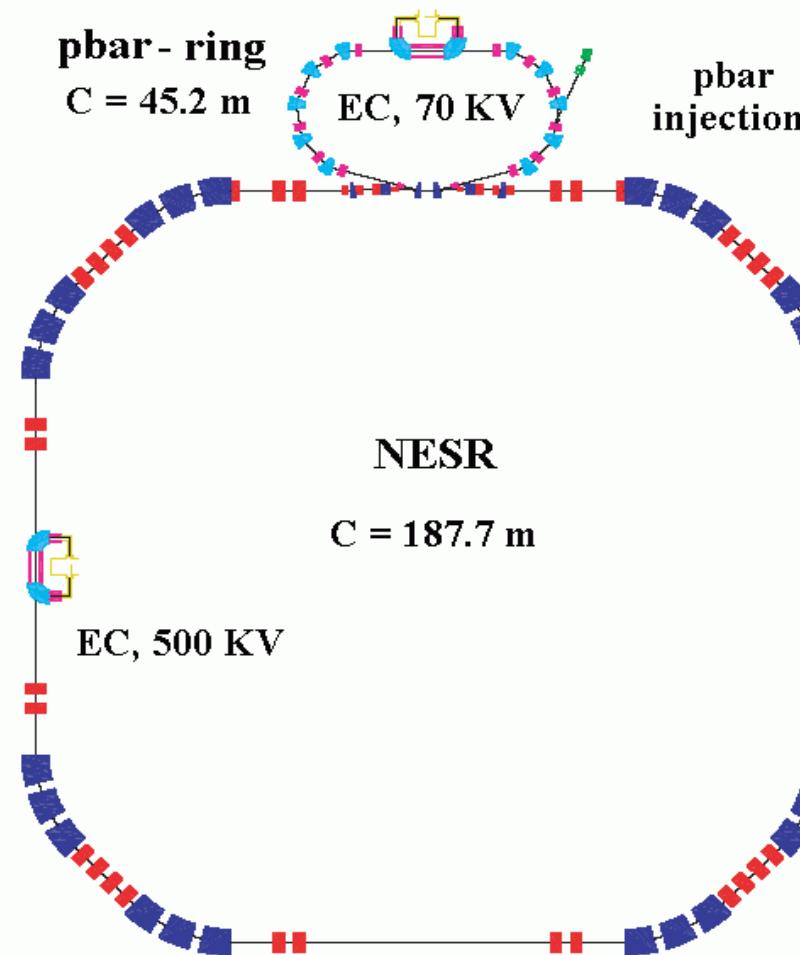


The Idea of AIC in FAIR



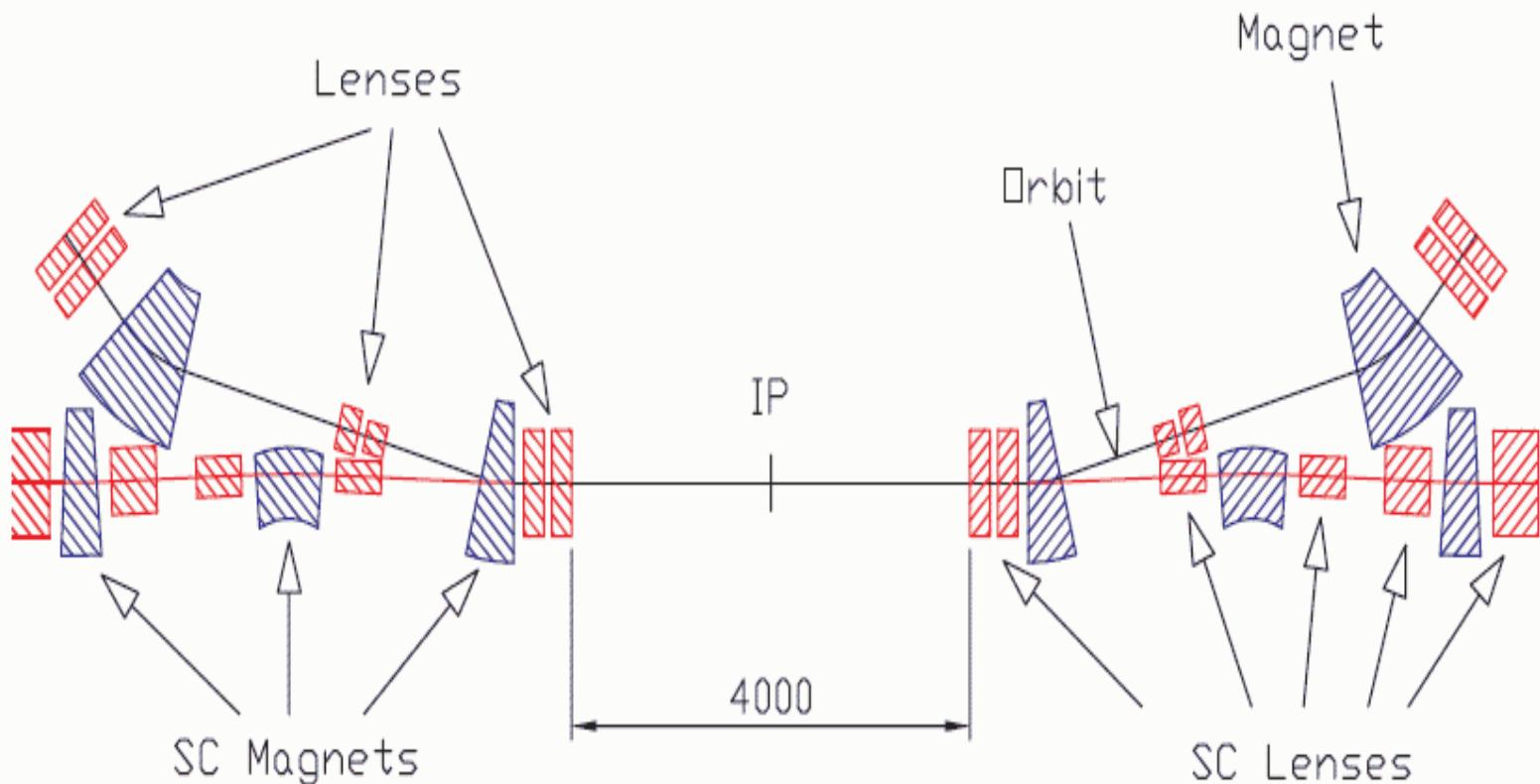


AIC Conceptual Design



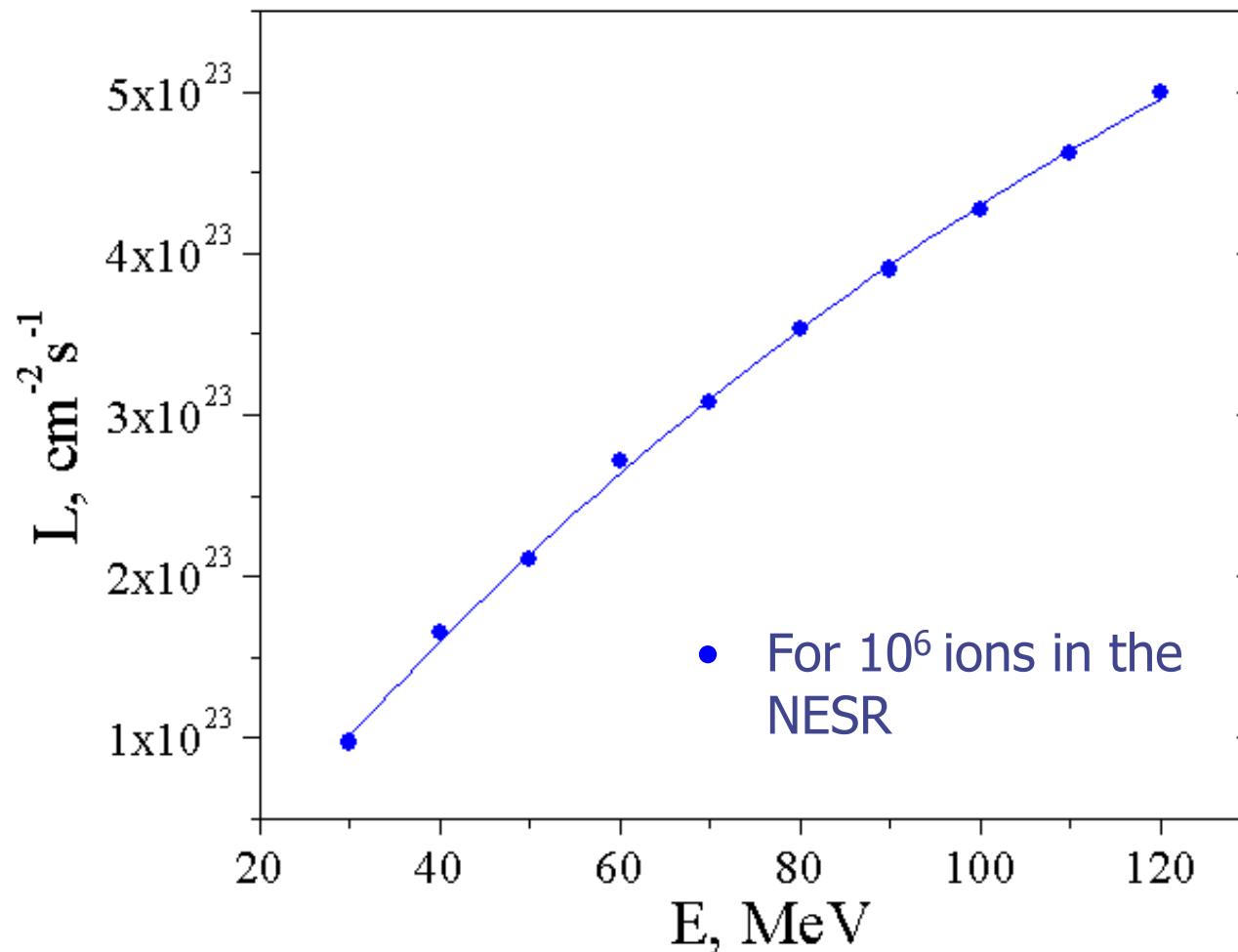


AIC Interaction Zone





AIC Luminosity, $L(E)$





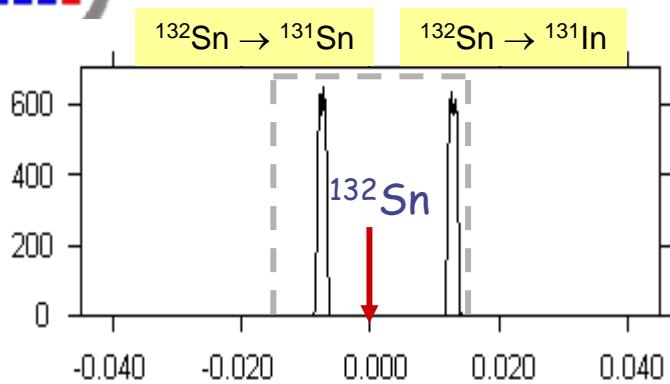
Yield, Luminosity, Measuring Time

- Using continuous longitudinal stacking: $N_s = \tau(dN/dt)$

Ion	$T_{1/2}$	yield	Luminosity	Time for 10^4 events
^{52}Ca	12s	$4 \cdot 10^5$ pps	$5 \cdot 10^{23} \text{cm}^{-2}\text{s}^{-1}$	~ 300 min
^{55}Ni	0.5s	$8 \cdot 10^7$ pps	$4 \cdot 10^{24} \text{cm}^{-2}\text{s}^{-1}$	~ 35 min
^{134}Sn	2.7s	$8 \cdot 10^5$ pps	$2 \cdot 10^{23} \text{cm}^{-2}\text{s}^{-1}$	~ 360 min
^{187}Pb	34s	$1 \cdot 10^7$ pps	$3 \cdot 10^{25} \text{cm}^{-2}\text{s}^{-1}$	~ 2 min



P/q Distributions of A-1 Nuclei

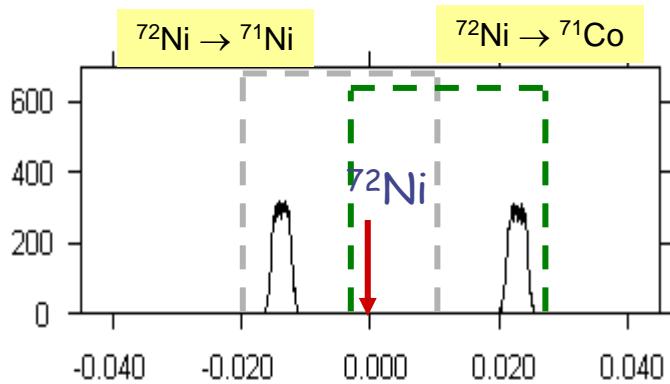


$A \sim 130$:

A & both $A-1$ nuclei in the acceptance

⇒ Schottky method using one ring setting

⇒ recoil detection

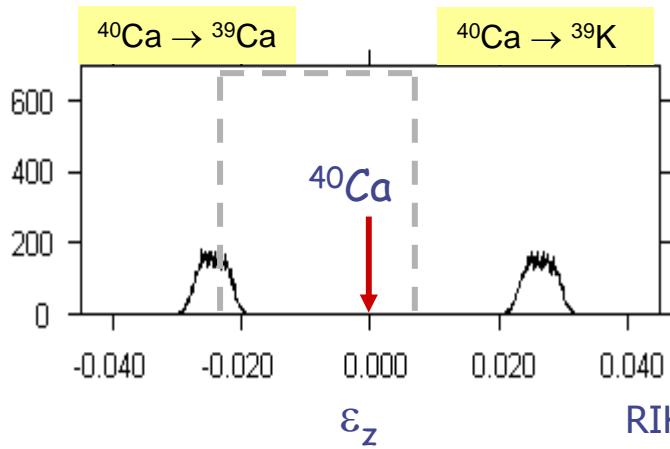


$A \sim 70$:

A & one $A-1$ nucleus in the acceptance

⇒ Schottky method using two ring settings

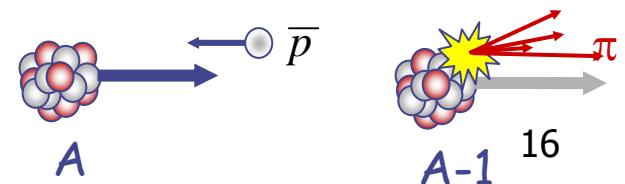
⇒ recoil detection



$A < 60$:

$A-1$ nucleus not in the acceptance

⇒ recoil detection

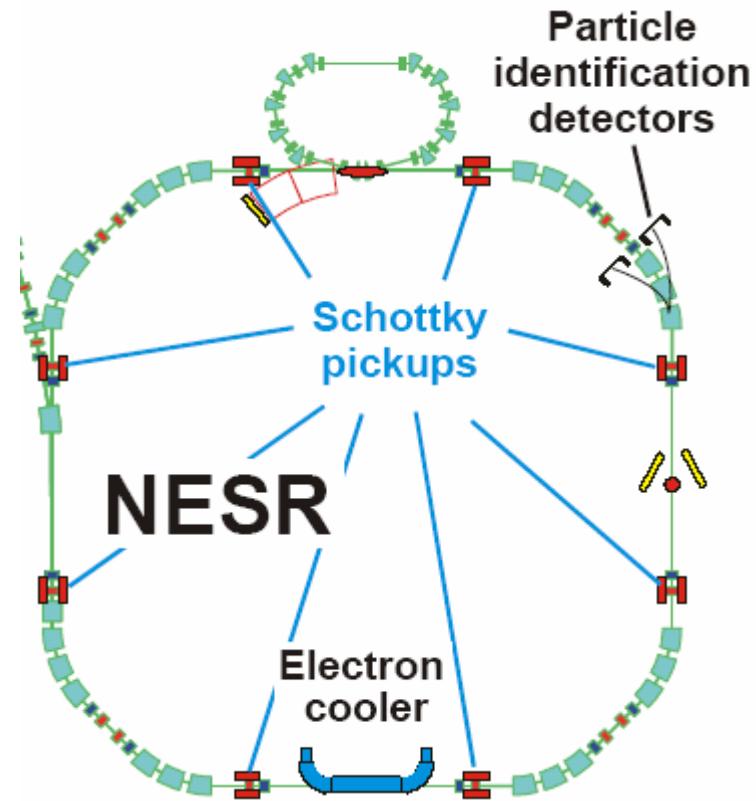
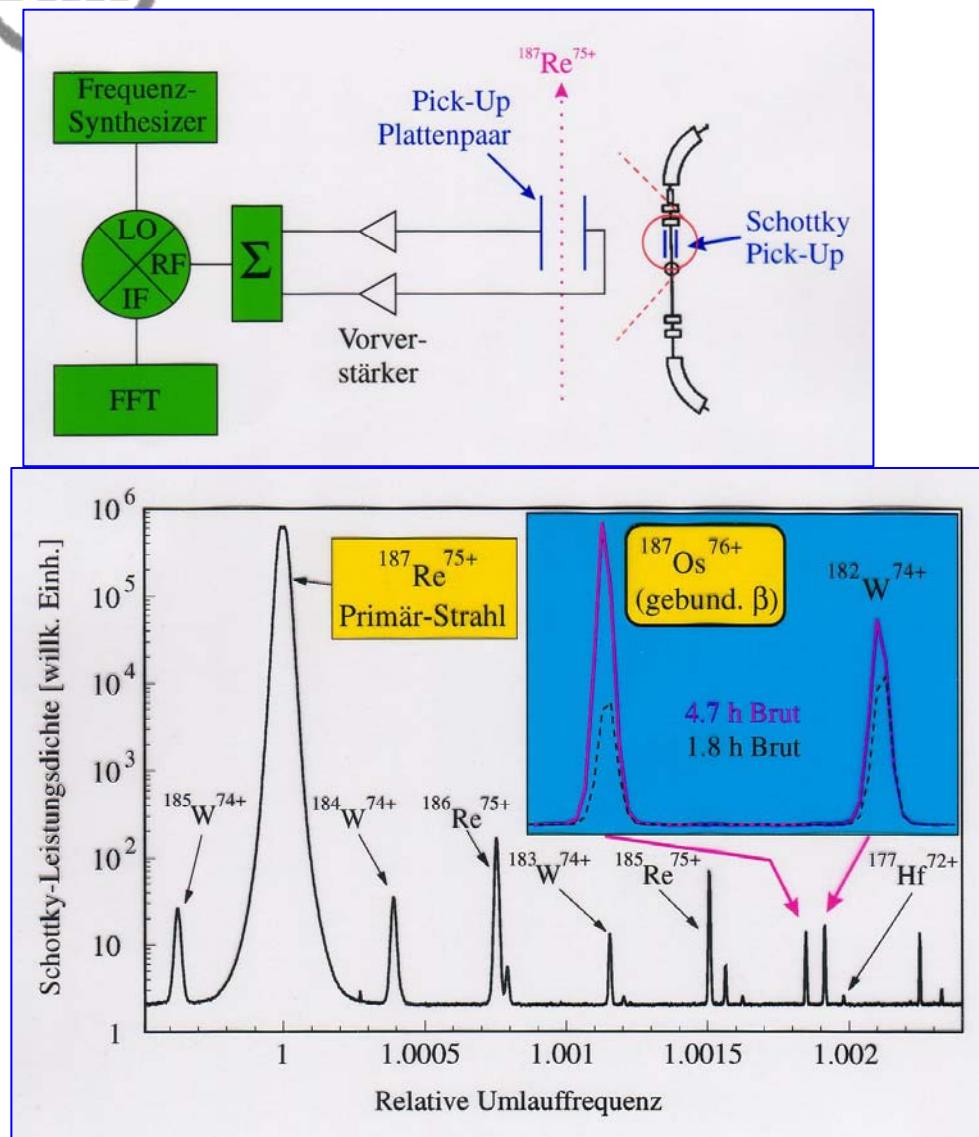




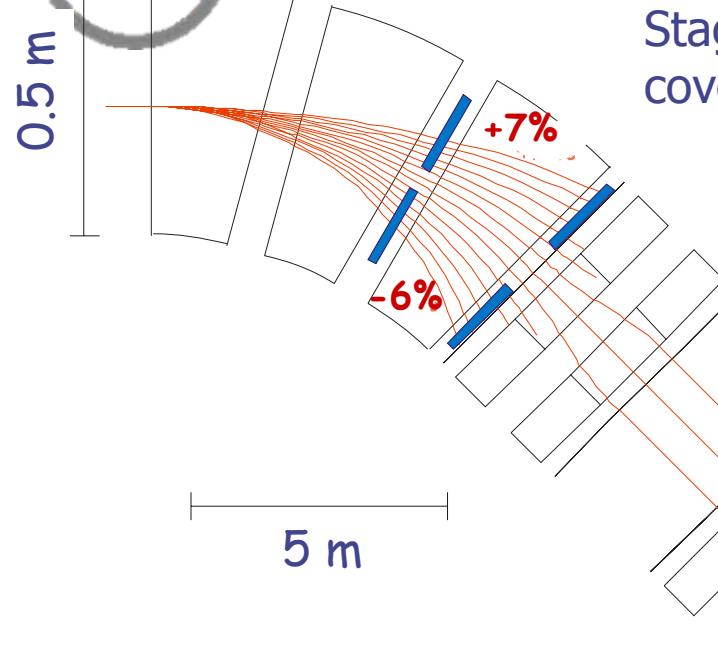
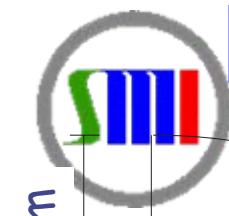
Momentum Distribution of A-1 Nuclei

- Experiments at LEAR showed that the antiproton is a quasielastic process
- The recoil momentum distribution reflects the momentum distribution of the absorbed neutron or proton
- The recoil momentum distribution can be measured by magnetic spectrometry and Schottky spectroscopy

Schottky Detection of Recoils

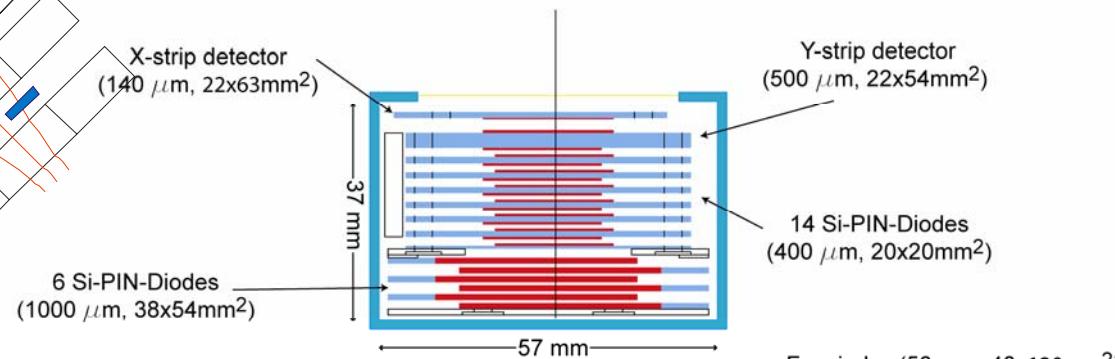


Recoil Detection after dipole section

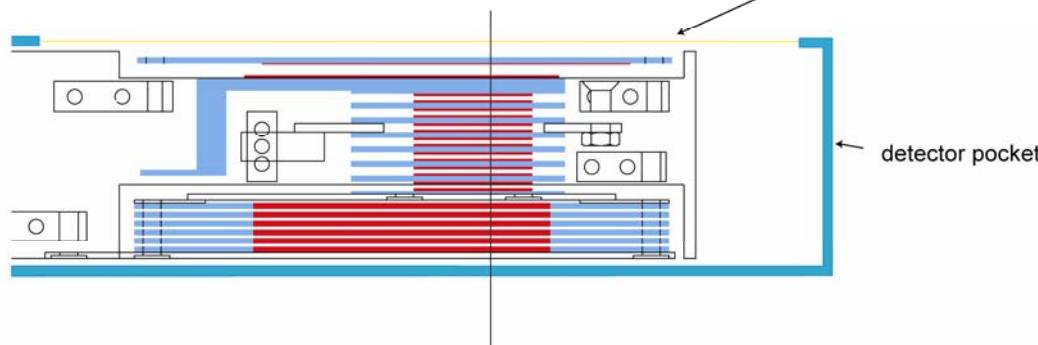


Staged set of recoil detectors
covers large momentum range

Existing ESR detector (TUM)

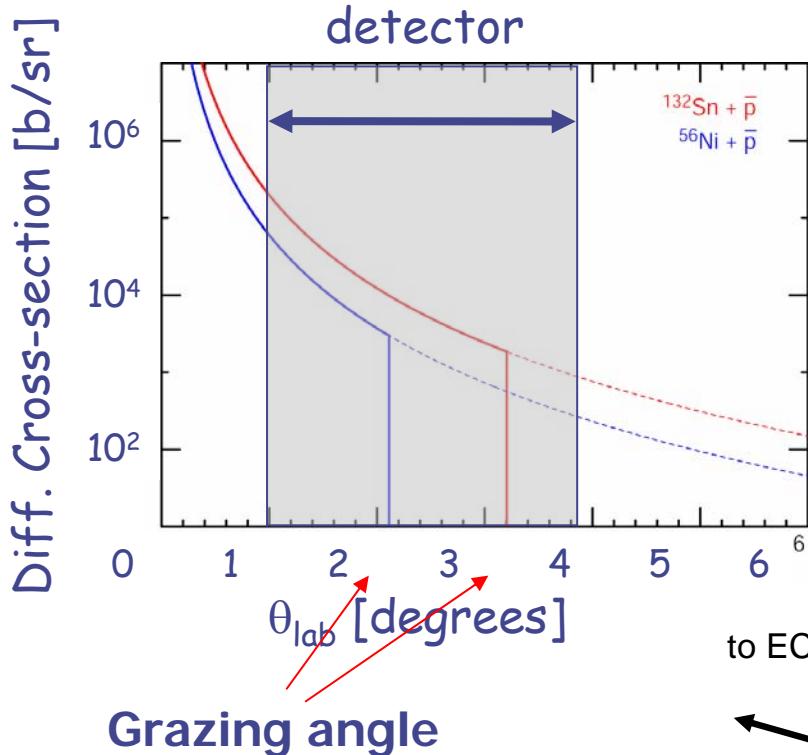


**Position resolution
better than 0,3 mm
+ energy loss
measurement**

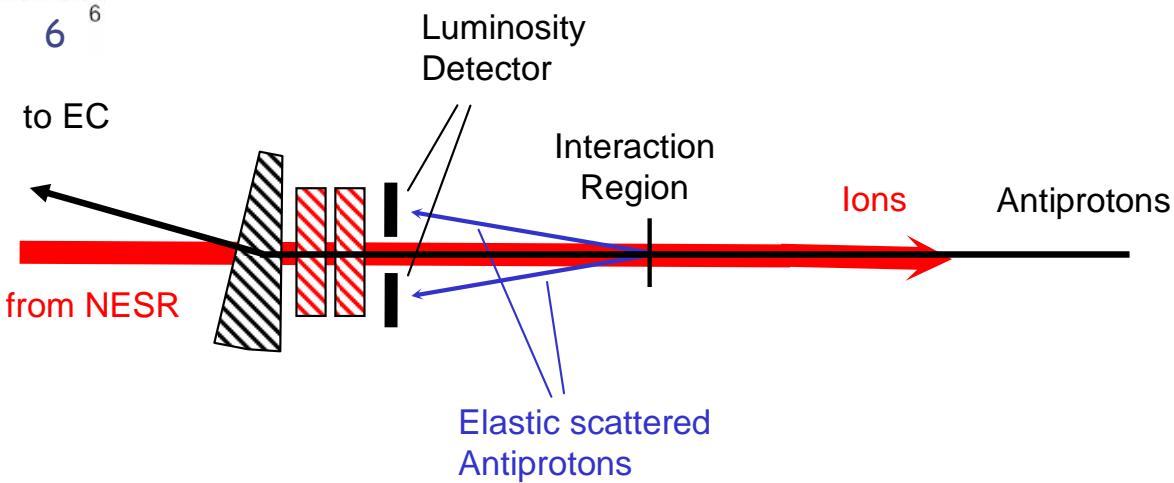
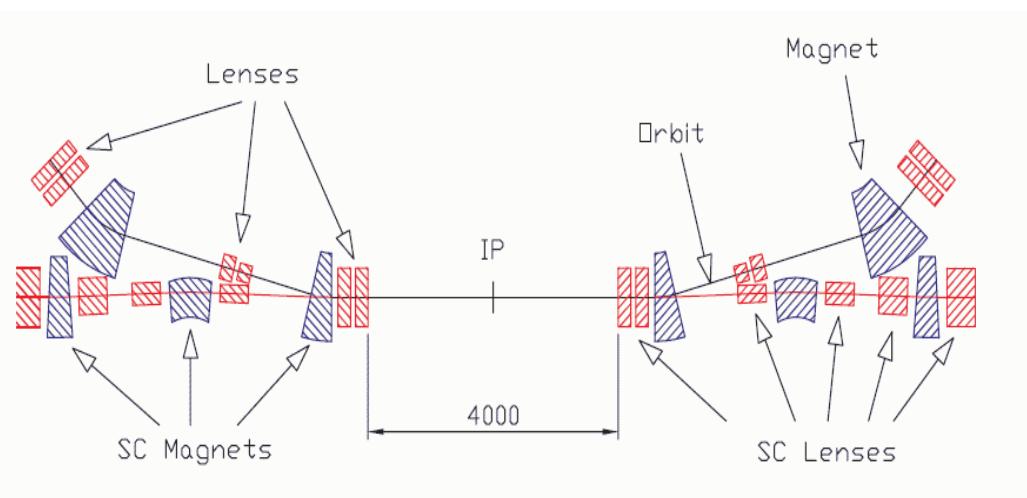




Luminosity Measurement



$$Ldt = -\frac{dN_{elast}}{\sigma_{elast}}$$





X-Sections and MS Radii

Luminosity from elastic scattering

Total reaction cross-section
from reduction of primary ions
with mass A

$$\sigma_T = -\frac{dN_R}{Ldt}$$

$$\sigma_T = C \langle r_{n+p}^2 \rangle = x(\sigma_n + \sigma_p)$$

exp. determined loss-factor

$$x = \frac{(\sigma_n + \sigma_p)}{\sigma_T}$$

$$x(\sigma_n + \sigma_p) = C \left(\langle r_n^2 \rangle + \langle r_p^2 \rangle \right)$$

$$\langle r_n^2 \rangle = \frac{x}{C} \sigma_n$$

$$\langle r_p^2 \rangle = \frac{x}{C} \sigma_p$$

$$Ldt = -\frac{dN_{elast}}{\sigma_{elast}}$$

cross-section for production
of A-1 nuclei:

$$\sigma_{i=n,p} = \epsilon_{(A-1,i)} \cdot \frac{dN_{(A-1,i)}}{Ldt}$$

$\epsilon_{(A-1,i)}$ Detection efficiency
for A-1 nuclei

$$\frac{\langle r_n^2 \rangle}{\langle r_p^2 \rangle} = \frac{\sigma_n}{\sigma_p}$$



AIC Physics Program

- Benchmarking: radii for the Sn isotopic chain
 - stable isotopes, measured with different techniques
 - plan: extending from ^{105}Sn to ^{135}Sn
- Radii along other closed-shell isotopic and isotonic chains
- Radii for nuclei near the drip-line in light nuclei
 - transition from halo nuclei to neutron skins
- Behaviour of radii across a shape transition
 - e.g. from ^{80}Zr to ^{104}Zr
- Odd-even effects in nuclear radii
- Study the antiproton-neutron interaction



Summary and Outlook

- Antiproton-nucleus cross section at 740 MeV/u is proportional to $\langle r^2 \rangle$
- Detection of A-1 products allows
 - determination of proton and neutron radii
 - in the same experiment (same systematic uncert.)
 - in a model independent way
 - parameters of Fermi distribution from energy dependence
- AIC is feasible in terms of technology and physics output
- Simple counting experiment using Schottky method or recoil detectors (once the collider runs)
- AIC allows systematic investigation of
 - Neutron skins
 - Transition from halos to skins
 - Odd-even staggering in radii
 - Shape coexistence and its effect on neutron and proton radii
 - Nucleon-antiproton interaction



AIC Collaboration

Antiproton-Ion Collider Collaboration



- Spokesperson / Deputy: R. Krücken^C / J. Zmeskal^A
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Antiproton optical potential

$$f_{\bar{p}N}(T_{Lab}, q) = \frac{ik}{4\pi} \sigma_{\bar{p}N}(T_{Lab}) (1 - i\epsilon) F_{\bar{p}N}(q^2)$$

$$F_{\bar{p}N}(q^2) = e^{-\beta^2 q^2}$$

$$t_{\bar{p}N}(T_{Lab}, q^2) = \frac{2\pi\hbar}{M} f_{\bar{p}N}(T_{Lab}, q^2)$$

$$U_{opt}(\mathbf{r}) = \sum_{N=p,n} \int \frac{d^3q}{2\pi^3} \rho_N(q) t_{\bar{p}N}(T_{Lab}, q^2) e^{i\mathbf{q}\cdot\mathbf{r}}$$

$$U_{opt} = U_c + V + iW$$



Cross Section

$$\left(-\frac{\hbar^2}{2\mu} \vec{\nabla}^2 + U_{opt} - T_{lab} \right) \Psi^{(+)}(\mathbf{k}, \mathbf{r}) = 0$$

$$\Psi^{(+)}(\mathbf{k}, \mathbf{r}) \rightarrow e^{i\mathbf{k}\cdot\mathbf{r}} + f_{\bar{p}A}(\hat{k}) \frac{e^{ikr}}{r} \quad S_{\ell j} = \eta_{\ell j} e^{2i\delta_{\ell j}}$$

$$\sigma_{abs}(\ell j) = \frac{4\pi}{k^2} \frac{2j+1}{2s+1} (1 - |S_{\ell j}|^2) = \frac{4\pi}{k^2} \frac{2j+1}{2s+1} (1 - \eta^2)$$

$$\sigma_{abs} = \sum_{\ell j} \sigma_{abs}(\ell j)$$

$$\sigma_{abs} = \frac{4\pi}{k} \int d^3 r \Psi^{(+)\dagger}(\mathbf{k}, \mathbf{r}) \frac{-2\mu}{\hbar^2} \Im U_{opt}(\mathbf{r}) \Psi^{(+)}(\mathbf{k}, \mathbf{r})$$

$$\sigma_{abs}^{(q)} = \frac{4\pi}{k} \int d^3 r \Psi^{(+)\dagger}(\mathbf{k}, \mathbf{r}) - \frac{2\mu}{\hbar^2} W^{(q)}(\mathbf{r}) \Psi^{(+)}(\mathbf{k}, \mathbf{r})$$