

# MUONIC ANTI-HYDROGEN

— *Possible Production and Test of CPT Theorem*

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*Workshop on Physics with Ultra Slow Antiprotons*

*March 16, 2005*

*at RIKEN (Wako)*

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**Meson Science Laboratory, IMSS, KEK**

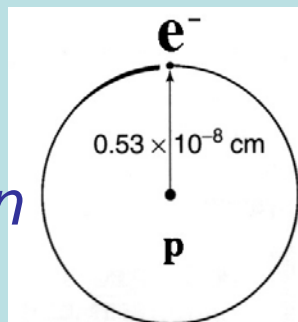
**Physics Department, University of California, Riverside**

***RIKEN***

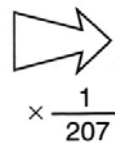
1. Introduction
2. Ultra Slow  $\mu^+$ ; Recent Progress and Future
3. Towards Production of Muonic Anti-Hydrogen
4. Possible High Precision Spectroscopy for Test of CPT Theorem
5. Conclusion; Future Perspectives

# Hydrogen, Anti-Hydrogen with ( $e^-$ , $e^+$ , $\mu^-$ , $\mu^+$ )

*Hydrogen*



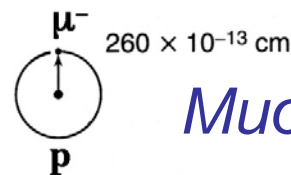
$$E_{1s}(pe^-): -13.6 \text{ eV}$$



$$\times \frac{1}{207}$$



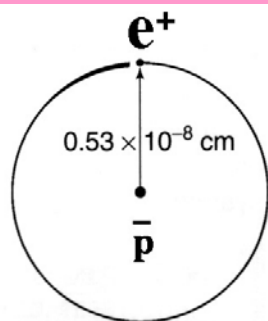
$$\times 207$$



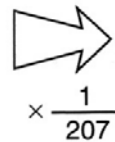
$$E_{1s}(p\mu^-): -2.5 \text{ keV}$$

*Muonic Hydrogen*

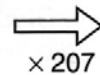
*Anti-Hydrogen*



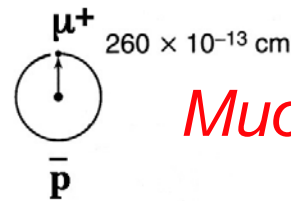
$$E_{1s}(\bar{p}e^+): -13.6 \text{ eV}$$



$$\times \frac{1}{207}$$



$$\times 207$$



$$E_{1s}(\bar{p}\mu^+): -2.5 \text{ keV}$$

*Muonic Anti-Hydrogen*

# What is a muon ?

Muon is an elementary particle first found in the cosmic ray in 1937. Muon is now produced in large numbers by using accelerators.

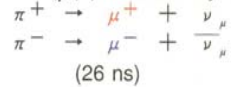
Charge	Spin	Mass	Lifetime
$\mu^+$	+1	106 MeV (1/9 of Proton)	2.2 $\mu$ s
$\mu^-$	-1	106 MeV (207 x Electron)	2.2 $\mu$ s

Structureless (point-like) particle and interacts mainly electromagnetically with atoms in matters

Pion ( $\pi$ ) production by accelerated beam

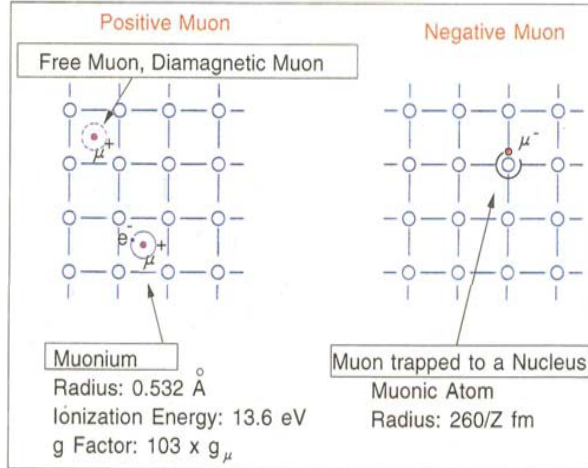


Muon ( $\mu$ ) production by  $\pi\mu$  decay

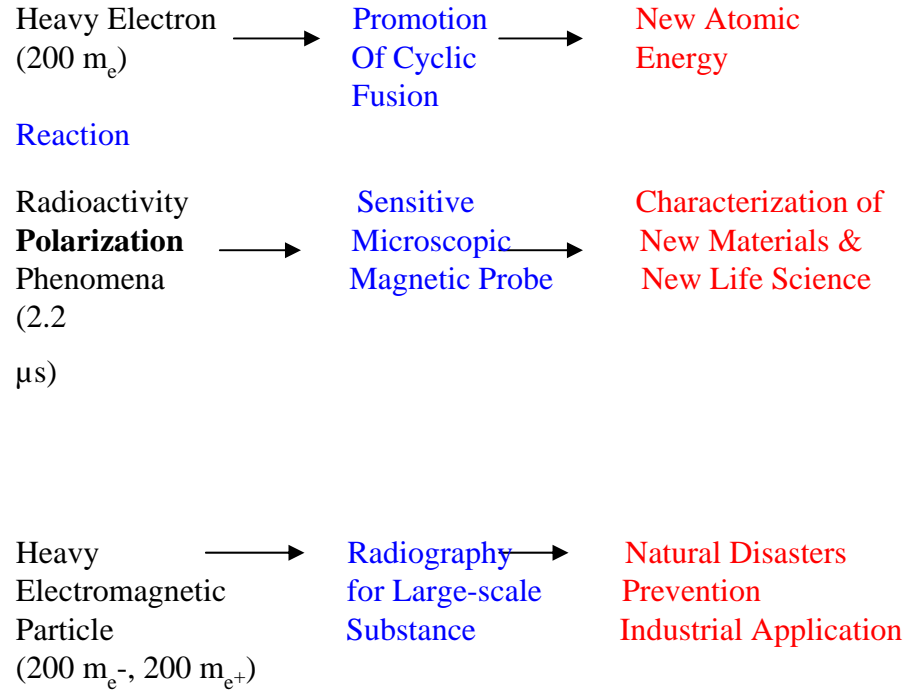


Behavior in Matters

$\mu^+$  "Light proton"  
 $\mu^-$  "Heavy electron"



# Muon for human life



# ULTRA SLOW $\mu^+$

## — *RECENT PROGRESS AND FUTURE* —

### PROPOSED & REALIZED (☆) MUON COOLING METHOD

	————— —————	IONIZATION COOLING PRISM	$\mu^+$ , $\mu^-$ $\mu^+$ , $\mu^-$
MeV	————— ————— —————	PHASE SPACE COMPRESSION	$\mu^+$ , $\mu^-$
	————— —————	$\mu^-$ RE-EMISSION FROM $\mu$ CF	$\mu^-$
KeV	————— ————— —————	☆ FRICTIONAL COOLING (PSI)	$\mu^+$ , $\mu^-$
	————— —————	☆ COLD MODERATOR (TRIUMF/PSI)	$\mu^+$
eV	————— ————— —————	☆ THERMAL MUONIUM IONIZATION (KEK)	$\mu^+$

# KEK METHOD OF ULTRA SLOW $\mu^+$

## THERMAL MUONIUM & ITS LASER IONIZATION

### Historical Development at KEK-MSL

1. Thermal Muonium Production in Vacuum from Hot Tungsten (W) Surface

*A.P. Mills. Jr., K. Nagamine et al.*

*Phys. Rev. Lett. 56(1986) 1463*

2. Laser Resonant Ionization (1 s  $\rightarrow$  2 s  $\rightarrow$  unbound)

of Thermal Muonium

*S. Chu, A.P. Mills. Jr., K. Nagamine et al.*

*Phys. Rev. Lett. 60(1988) 101*

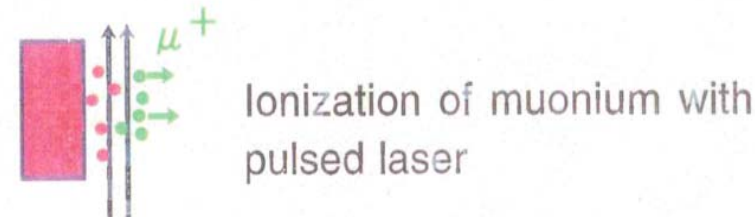
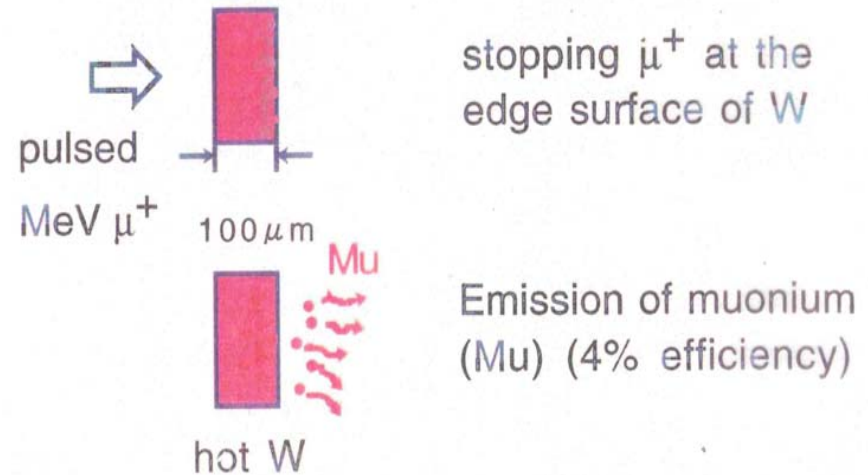
3. Laser Resonant Ionization (1 s  $\rightarrow$  2 p  $\rightarrow$  unbound)

of Thermal Muonium and Ultra-Slow  $\mu^+$  Production

*K. Nagamine, Y. Miyake et al.*

*Phys. Rev. Lett. 74(1995) 4811*

Generation of thermal energy muonium in vacuum



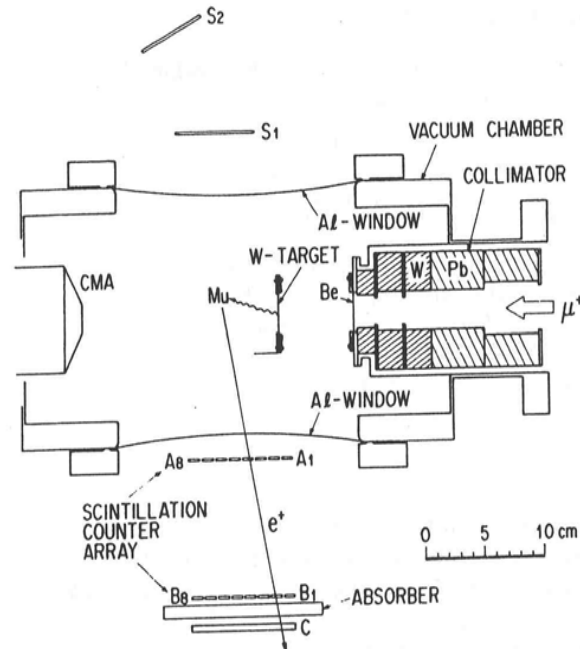
# THERMAL MUONIUM PRODUCTION IN VACUUM

— Activities at KEK-MSL —

Original  
Mills et al. (1986)

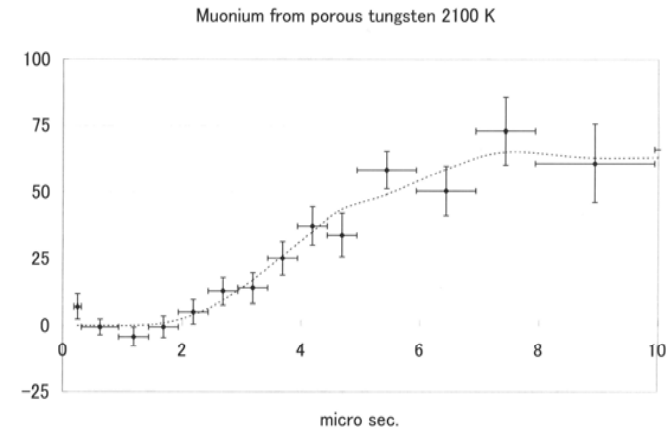
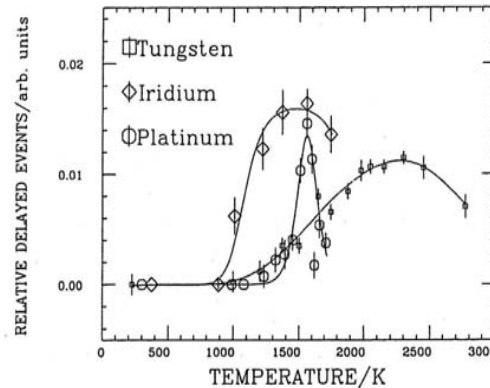
Development  
Matsushita et al. (1998)

Recent Development  
Miyadera et al. (2004)



$$N_{\text{Mu}}/N_{\mu^+} \simeq 0.04$$

$$T_{\text{Mu}} \simeq T_{\text{W}}$$



$$N_{\text{Mu}} (\text{Porus W}) \simeq 2 \times N_{\text{Mu}} (\text{W})$$

Physical parameters of thermal Mu [9,18].

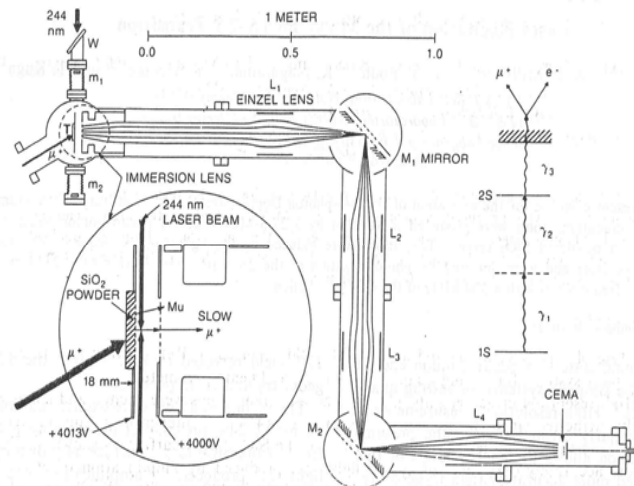
Metal	$E_{\text{Mu}}$ (eV)	$E_{\text{ad}}$ (eV)	$\phi_{\text{H}}$ (eV)	Facility
W	0.66(4)	2.9	1.6	KEKMSL
W	1.72(5)	2.9	1.6	KEKMSL
W	1.3(1)	2.9	1.6	RIKEN-RAL
Re	2.62(3)	2.8	2.0	RIKEN-RAL
Ir	1.4(1)	2.7	1.5	KEKMSL
Pt	2.9(1)	2.5	2.2	KEKMSL

# ULTRA SLOW $\mu^+$ PRODUCTION VIA LASER IONIZATION OF THERMAL Mu

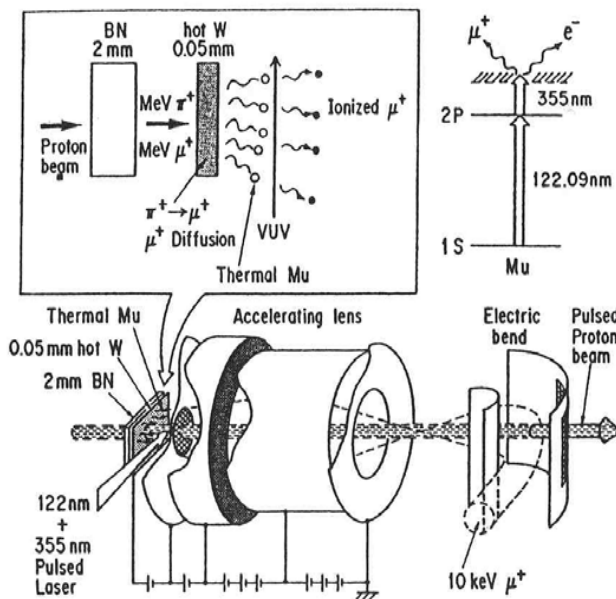
Original  
Chu et al. (1989)  
(KEK-MSL)

Hot W at Proton Beam  
Nagamine, Miyake et al.  
(1995)  
(KEK-MSL)

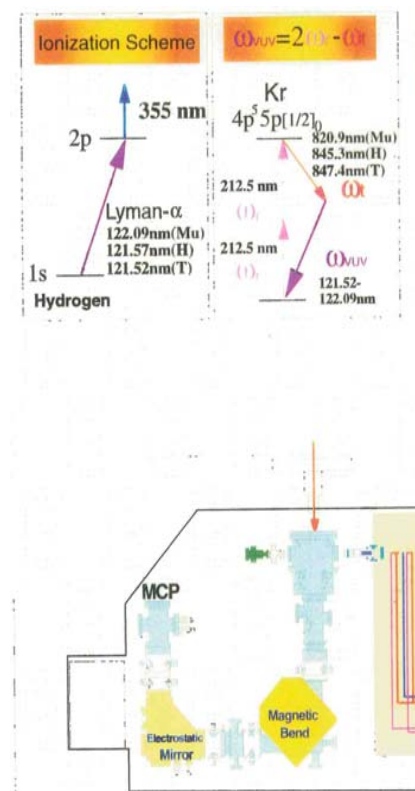
Hot W at 4 MeV  $\mu^+$  Beam  
Bakule, Matsuda et al. (2002)  
(RIKEN-RAL)



$1/h/10^3$  4 MeV  $\mu^+$



$1/\text{min}/2 \mu\text{A} 500 \text{ MeV } p$



$1/s/10^5$  4 MeV  $\mu^+$

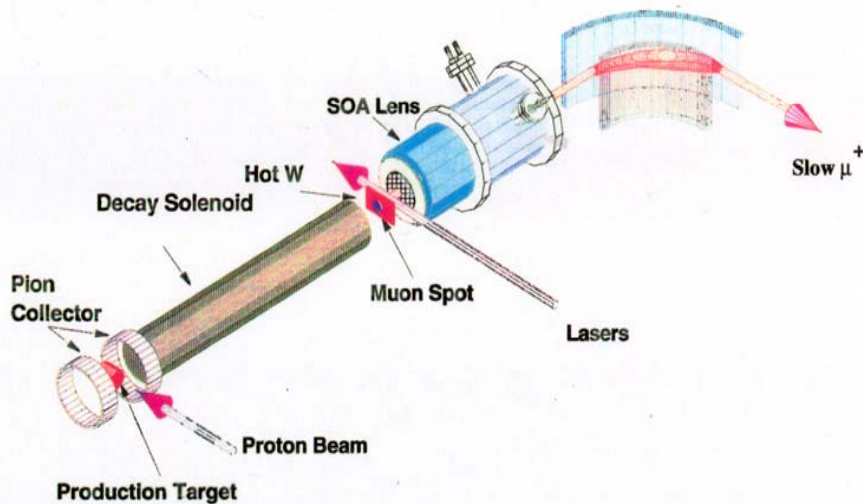
# INTENSE ULTRA SLOW $\mu^+$ IN THE NEAR FUTURE (1)

## EFFICIENT $\pi/\mu$ COLLECTOR

High Intensity Proton Driver  
(1 GeV  $\times$  mA  $\rightarrow$  MW)

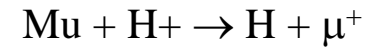
Full  $\pi/\mu$  Capture

$\mu^+$  Stopping & Zero-Energy  $\mu^+$  Production

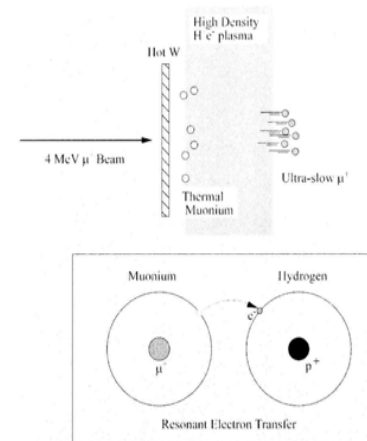


## EFFICIENT Mu IONIZATION

i) Resonant  $e^-$  Transfer in High Density H Plasma



$$\sigma_{\text{Tr}} \simeq 5 \times 10^{-15} \text{ cm}^2$$



ii) Multi-Photon Mu Ionization by femto-sec Laser Pulses

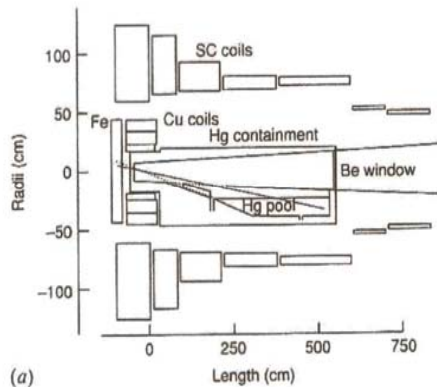
iii) Laser Impact Ionization of Mu at Surface



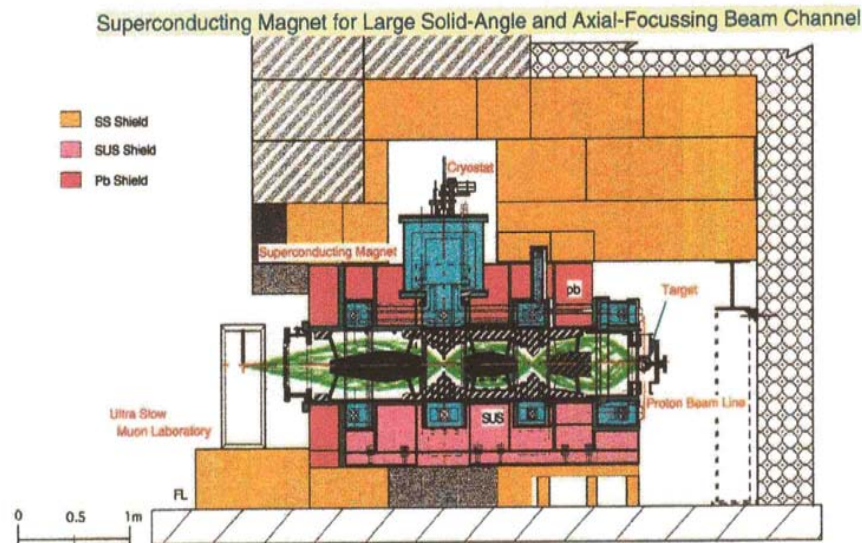
# $\pi/\mu$ COLLECTION AND MUON TRANSPORTATION

☆Based Upon Recent Progress in the Studies of Neutrino-Factor and  $\mu\mu$  Colliders

Full Solid Angle Capture

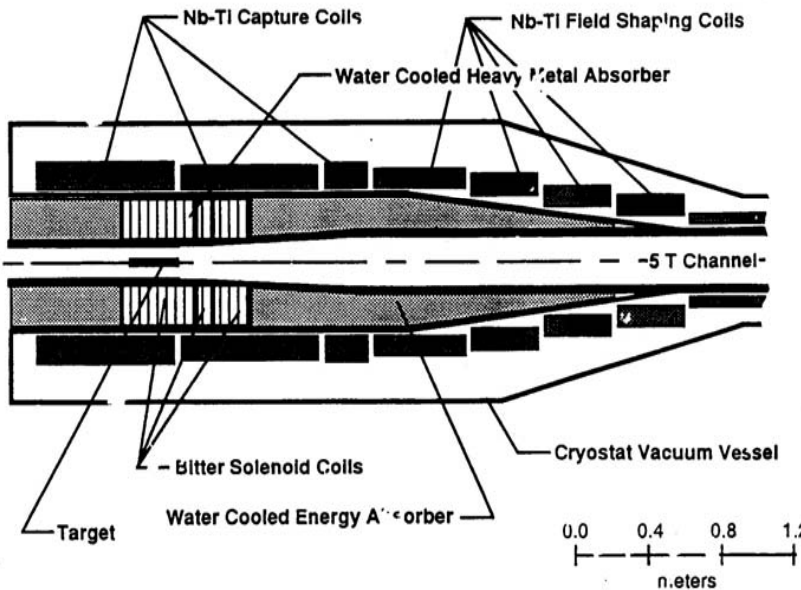


1 Str Acceptance for Surface  $\mu^+$ , DAI-OMEGA at KEK



# INTENSE ULTRA SLOW $\mu^+$ IN THE NEAR FUTURE (2)

Realization of more than  $10^{10}/s$  Ultra Slow  $\mu^+$



	Expected Numbers ( $s^{-1}$ )	Conditions & Remarks
$N_p$	$7.6 \times 10^{15}$	1 GeV $\times$ 1mA (1 Mw)
$N_{\pi^+}^{tot}$	$4.8 \times 10^{13}$	$\sigma_{\pi^+}^{tot} : 28mb$
$N_{\mu^+}$	$4.8 \times 10^{12}$	Pion Capture 2.9 T 20 cm Bore $\times$ 1.5m Pion Decay 3.0 T, 25 cm Bore $\times$ 10 m Full Reflection
$N_{Th\ \mu}$	$\simeq 10^{12}$	Full Stopping (100 $\times$ 10 $\mu m$ Poruns W) 20 % Conversion
$N_{us\mu^+}$	$\simeq 10^{12}$	Full Ionization

$$N_p = 7.6 \times 10^{15}$$

1 GeV  $\times$  1mA (1 Mw)

$$N_{\pi^+}^{tot} = 4.8 \times 10^{13}$$

$\sigma_{\pi^+}^{tot} : 28mb$

$$N_{\mu^+} = 4.8 \times 10^{12}$$

Pion Capture 2.9 T 20 cm Bore  $\times$  1.5m  
Pion Decay 3.0 T, 25 cm Bore  $\times$  10 m  
Full Reflection

$$N_{Th\ \mu} \simeq 10^{12}$$

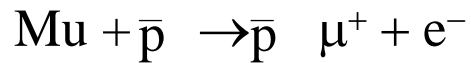
Full Stopping (100  $\times$  10  $\mu m$  Poruns W)  
20 % Conversion

$$N_{us\mu^+} \simeq 10^{12}$$

Full Ionization

# TOWARDS PRODUCTION OF MUONIC ANTI- HYDROGEN

## POSSIBLE CROSSED-BEAM EXPERIMENT

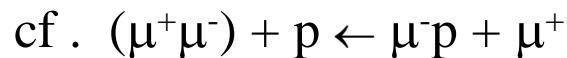


$$a_0 \quad \frac{1}{207} a_0$$

$$E_{1s}^e \quad 207 E_{1s}^e$$

$$\sigma_{\text{Tr}} \simeq 10^{-4} \pi a_0^2$$

$$\text{at } E_p \simeq 207 E_{1s}^e$$



$$\frac{2}{207} a_0 \quad \frac{1}{207} a_0$$

$$\frac{207}{2} E_{1s}^e \quad 207 E_{1s}^e$$

$$\sigma_{\text{Tr}} \simeq 10^{-4} \pi a_0^2$$

$$\text{at } E_{\mu^+} \sim 207 E_{1s}^e$$

Q.C. Ma et al. Phys. Rev. 32A (1985) 2645

# FURTHER EFFICIENCY INCREASE

— *Optimization of Time, Space, Character* —

☆ Time Compression/Bunching

☆ Acceleration & Micro-Beam

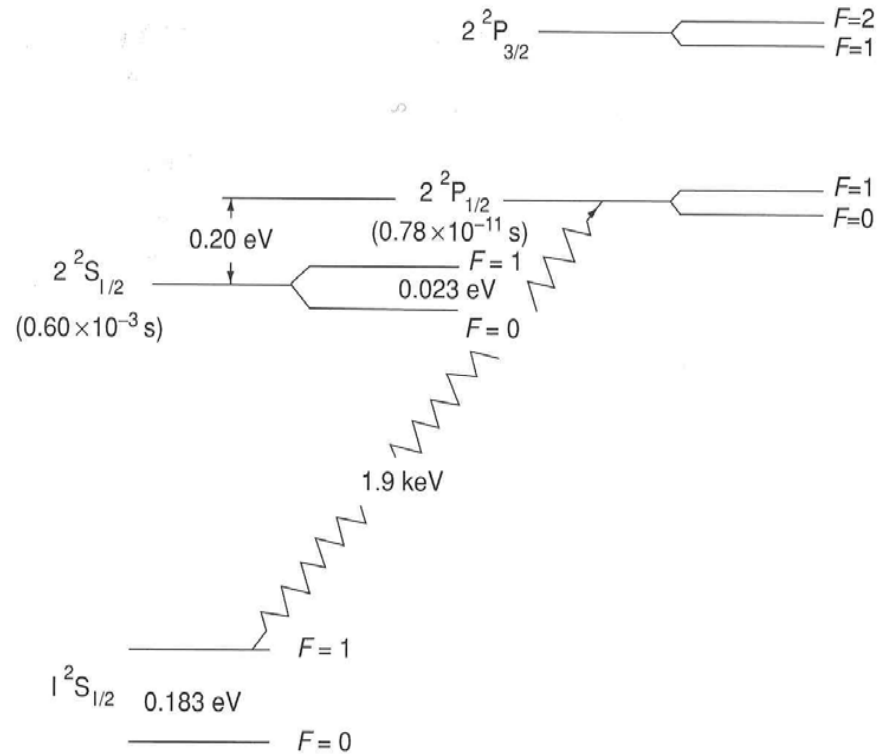
*Yield*

*Estimation*

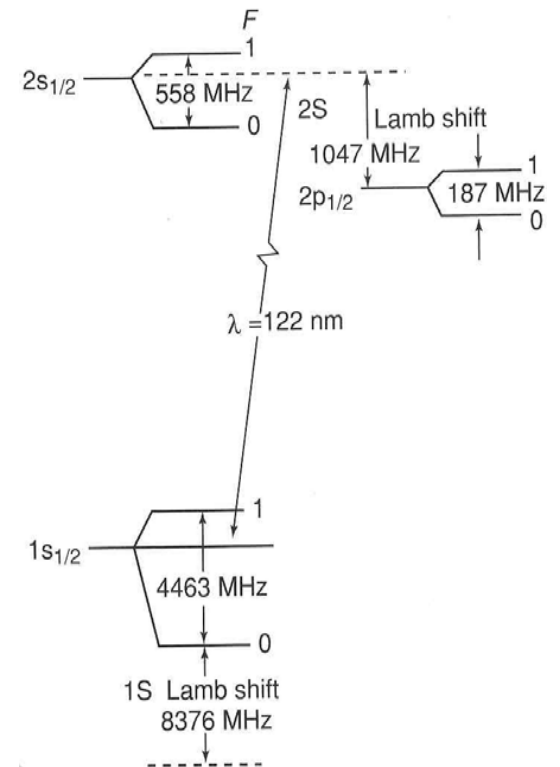
$$\frac{I_p}{p} \cdot N_{Mu} \cdot \sigma_{Tr} \simeq 1/s$$

$$10^{10}/s \quad 10^{10} \quad 10^{-20} \text{ (cm}^2\text{)}$$

# POSSIBLE HIGH-PRECISION SPECTROSCOPY FOR TEST OF CPT THEOREM BY USING MUONIC HYDROGEN/ANTI-HYDROGEN

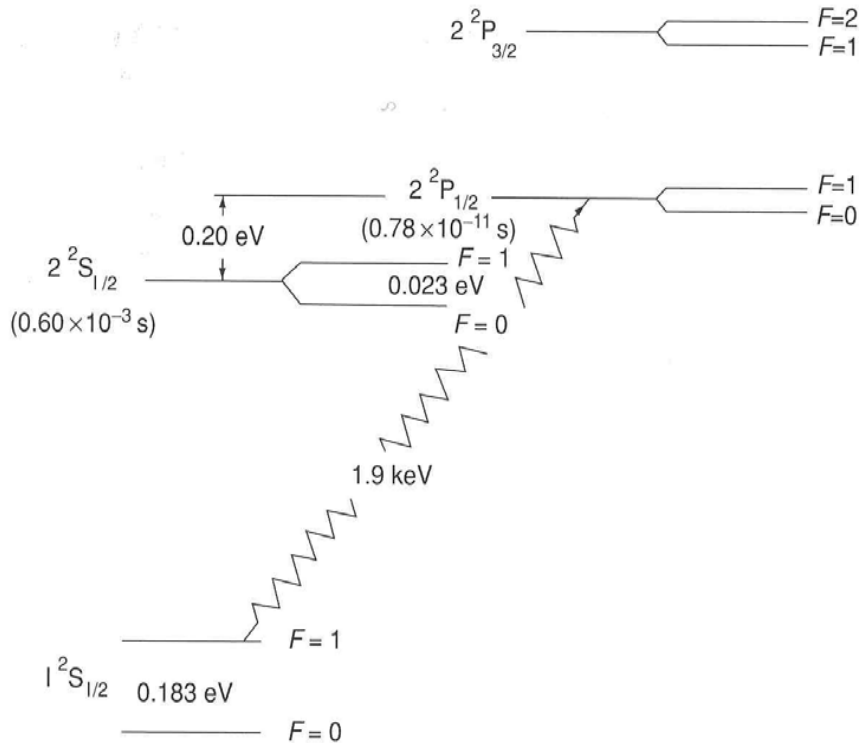


$\mu p$  and  $\mu^+ \bar{p}$  under CPT conservation



$e p$  and  $e^+ \bar{p}$

# POSSIBLE OBSERVABLES FOR HIGH PRECISION LASER SPECTROSCOPY



1. Hyperfine Splitting at the Ground State

$$\Delta E (n = 1, \text{ hfs}) = 0.18 \text{ eV} (6.89 \mu\text{m})$$

Resonance Signal Detection:

Range, Polarization, Transfer to H

2. Lamb Shift (Vacuum Polarization at  $n =$

$$\Delta E (2^2p_{1/2} - 2^2s_{1/2}) = 0.20 \text{ eV} (6.20 \mu\text{m})$$

Resonance Signal Detection:

Missing  $K_\alpha$  X-ray

Laser is available!

$\text{CdGeAs}_2$  (K. Kato et al.)

no ( $\mu\text{p}$ ) experiment So far!

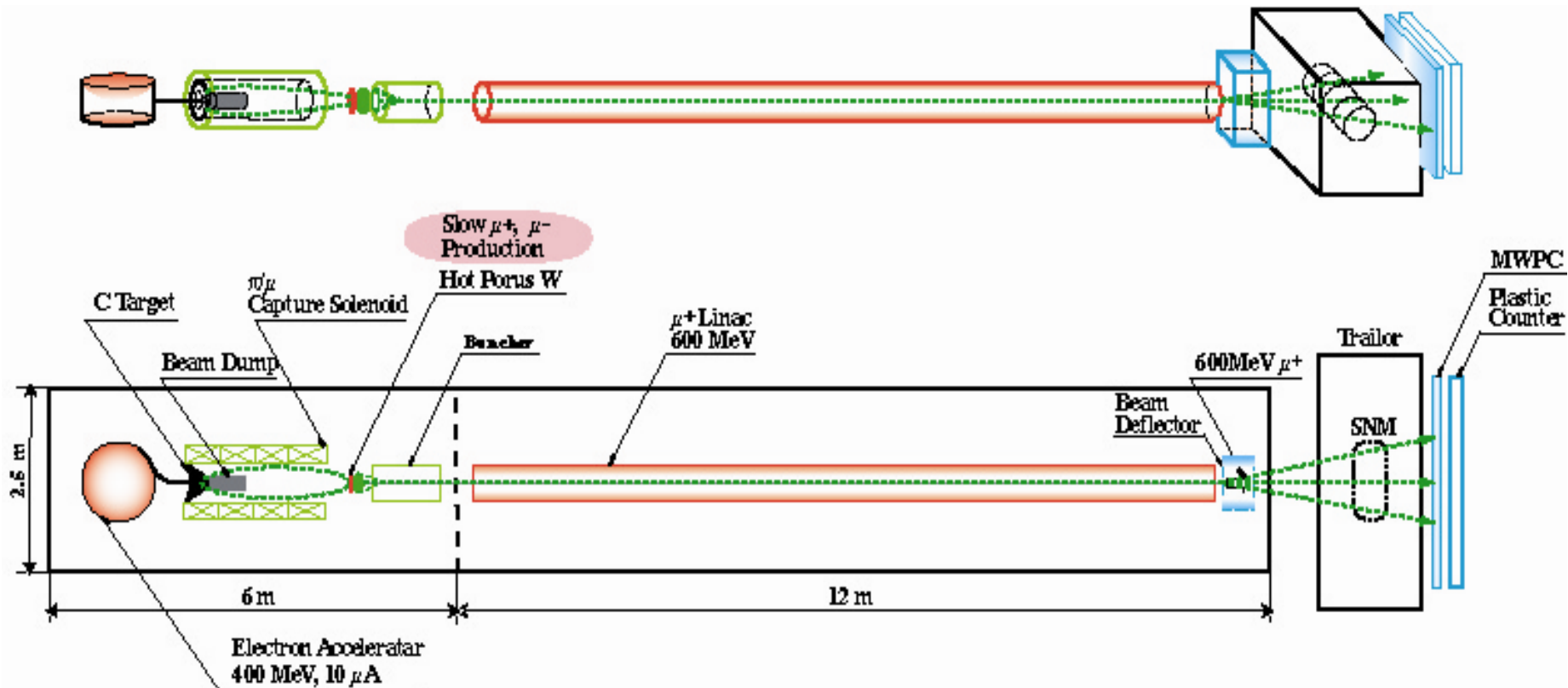
# CONCLUSION; FUTURE PERSPECTIVES

1. Muonic Anti-Hydrogen is not a Dream and to be realized in the 21<sup>st</sup> century

The technology of intense and high-quality  $\mu^+$  and  $\bar{p}$  beam will take a rapid development *independently*, because of the needs of each community.

Good communication between Low Energy Muon Science and Physics Community should be encouraged.

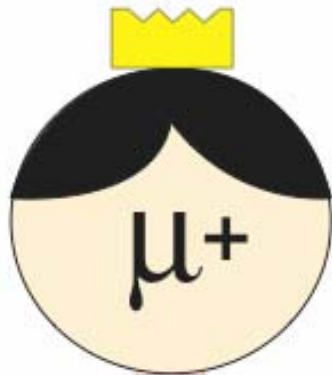
2. Need of theoretical works on CPT violation effect in Muonic Anti-Hydrogen



*Proposed accelerator systems for the advanced muon radiography*



# *Ultra-Slow*

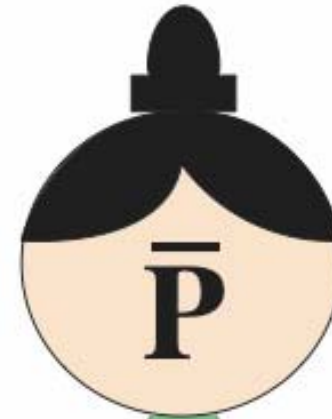


Surface Physics  
Inter-Surface Physics  
Nano Materials  
Life Science

Bunching & Re-Acceleration  
Radiography  
Neutrino Factories  
Muon Colliders



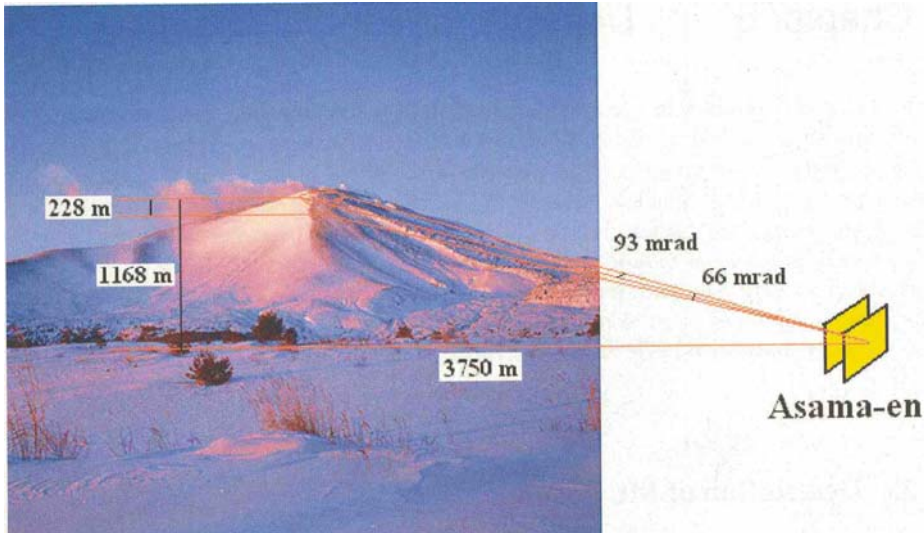
# *Ultra-Slow*



Ionization Dynamics  
Capture Process  
Anti-Hydrogen Production  
Anti-Hydrogen Spectroscopy  
Gravity

# LOOKING INNER-STRUCTURE FROM OUTSIDE

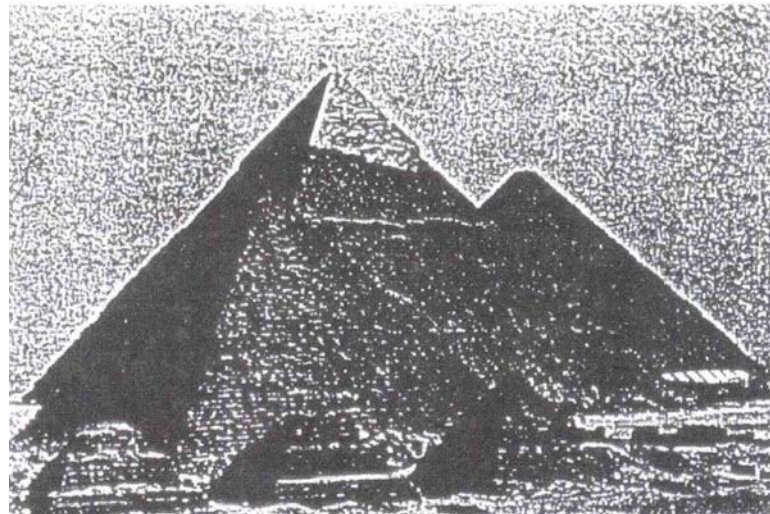
*— Keeping Objective as it is —*



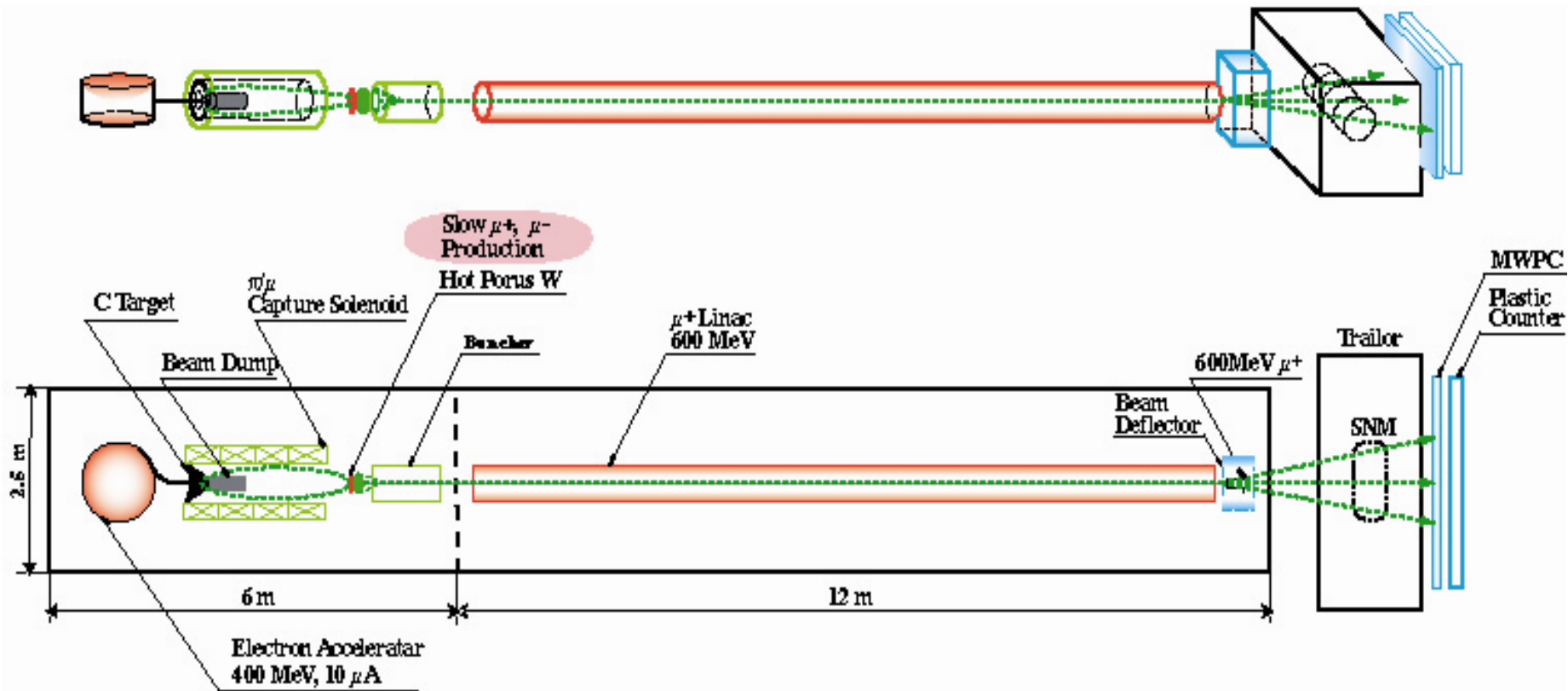
Volcano



Blast Furnace



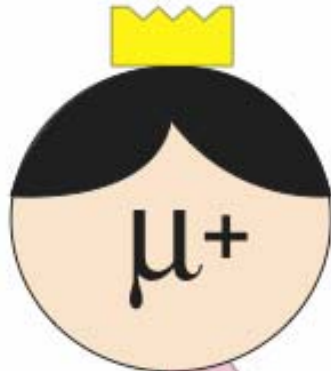
Pyramid



*Proposed accelerator systems for the advanced muon radiography*

*Ultra-Slow*

*Ultra-Slow*



*within  
21<sup>st</sup>  
Century*



Surface Physics  
Inter-Surface Physics  
Nano Materials  
Life Science

Ionization Dynamics  
Capture Process  
Anti-Hydrogen Production  
Anti-Hydrogen Spectroscopy  
Gravity

Bunching & Re-Acceleration  
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Neutrino Factories  
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