

円筒容器中の超流動ヘリウム3-B相 における準粒子状態

理研

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B-phase in cylinder

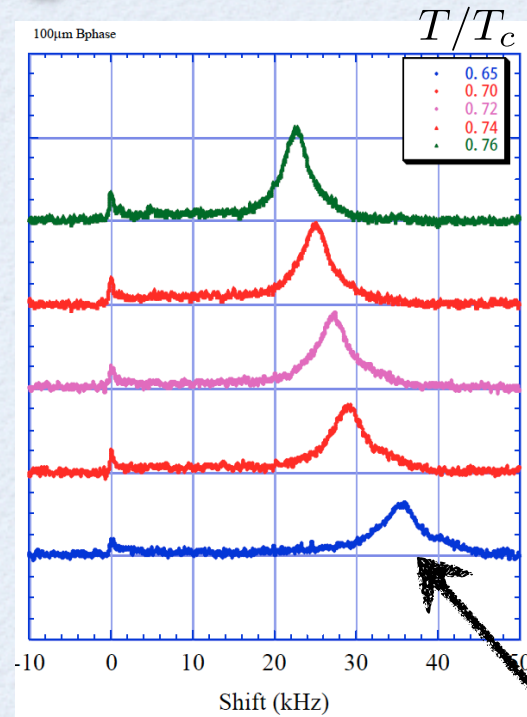
Rotating cryostat in ISSP



最高回転速度~12rad/s
試料半径 50 μ m, 100 μ m

数本の渦を侵入させる
ことが可能
マヨラナゼロモード

NMR spectra

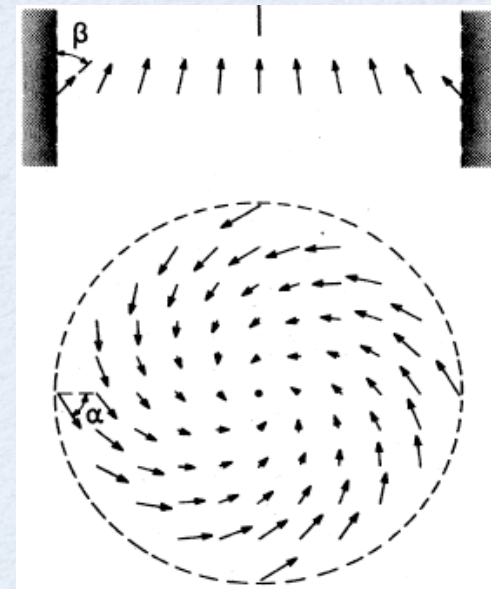


R. Ishiguro, Dr. Thesis (2003).

$$\Delta f_B^2 = \Omega_B^2 \sin^2 \beta \propto \frac{|\Delta_B|^2}{\chi_B} \sin^2 \beta$$

マヨラナエッジ状態
異方的スピン帯磁率

flare-out texture




M.M. Salomaa and G.E. Volovik,
Rev. Mod. Phys. **59**, 533 (1987).

$\beta = 63.4^\circ$
edge

Outline of research

 n-texture

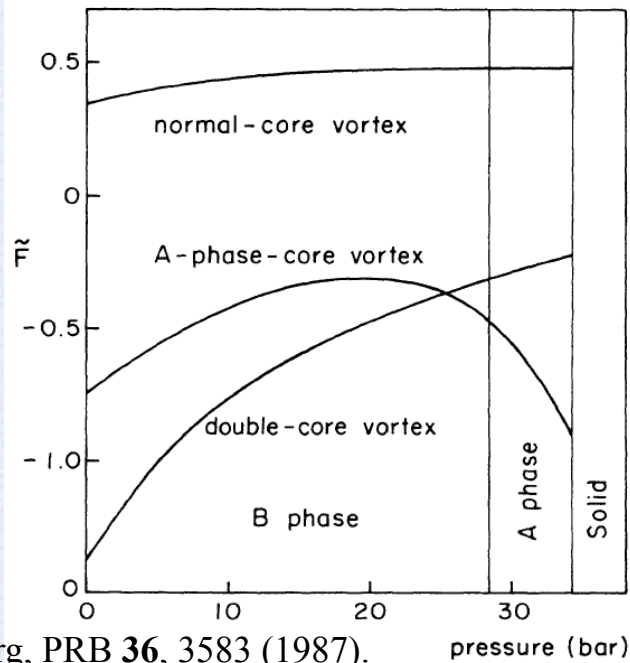
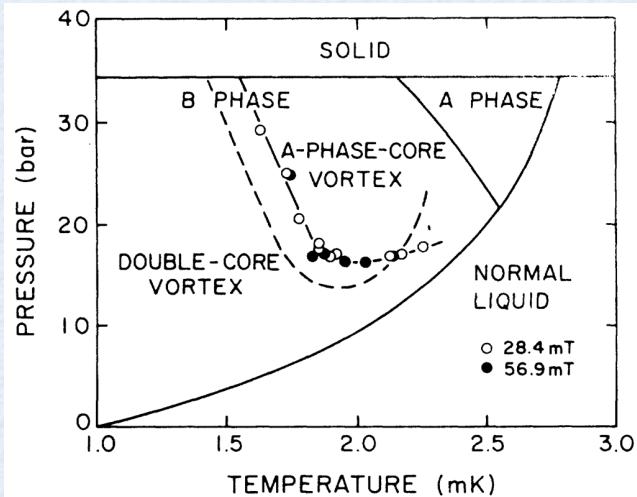
 Quasiparticle states
(vortex, edge)

 Spin susceptibility

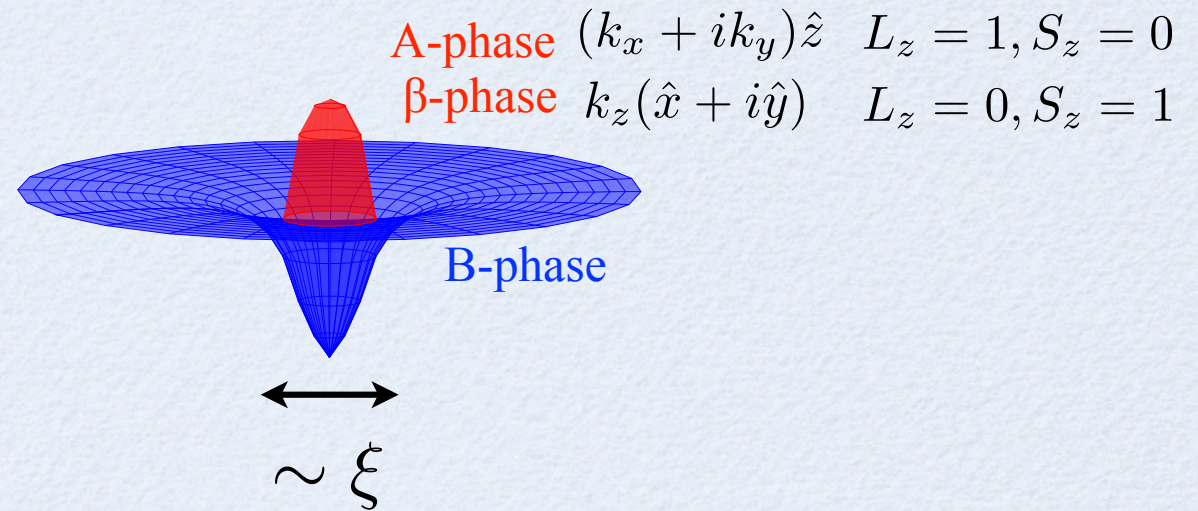
 NMR spectrum

Vortex in B-phase

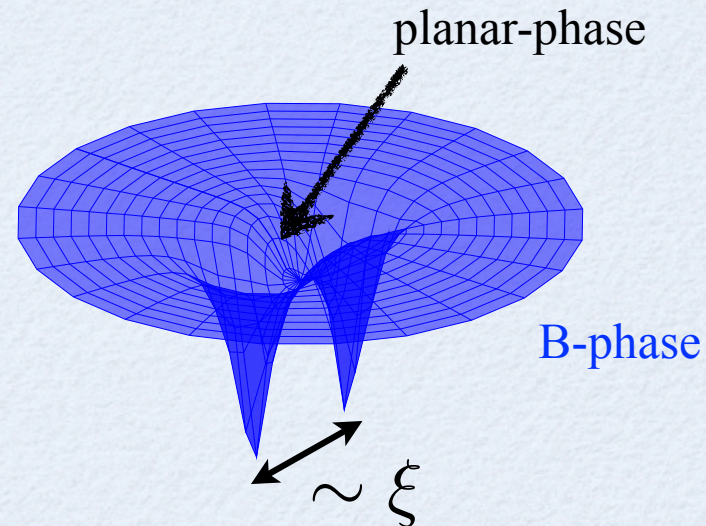
Phase diagram of vortex



A-phase-core vortex



double-core vortex



Quasi-classical Eilenberger theory

$$\Delta/E_F \ll 1 \quad \int d\xi_k \hat{\sigma}_z \hat{G}(\mathbf{k}, \mathbf{r}, \omega_n) \equiv \hat{g}(\mathbf{k}_F, \mathbf{r}, \omega_n) \equiv -i\pi \begin{pmatrix} \hat{g} & i\hat{f} \\ -i\hat{f} & -\hat{g} \end{pmatrix}$$

Eilenberger equation

$$-i\hbar \mathbf{v}_F \cdot \nabla \hat{g}(\mathbf{k}_F, \mathbf{r}, \omega_n) = \left[\begin{pmatrix} i\omega_n \hat{1} & -\hat{\Delta}(\mathbf{k}_F, \mathbf{r}) \\ \hat{\Delta}^\dagger(\mathbf{k}_F, \mathbf{r}) & -i\omega_n \hat{1} \end{pmatrix}, \hat{g}(\mathbf{k}_F, \mathbf{r}, \omega_n) \right]$$

$$\hat{g} \downarrow \quad \uparrow \hat{\Delta}$$

Gap equation

$$\hat{\Delta}(\mathbf{k}_F, \mathbf{r}) = N_0 \pi k_B T \sum_{-\omega_c \leq \omega_n \leq \omega_c} \left\langle V(\mathbf{k}_F, \mathbf{k}'_F) \hat{f}(\mathbf{k}'_F, \mathbf{r}, \omega_n) \right\rangle_{\mathbf{k}'_F}$$

$$\text{pair potential : } V(\mathbf{k}_F, \mathbf{k}'_F) = 3g_1 \mathbf{k}_F \cdot \mathbf{k}'_F$$

Local density of states (LDOS)

$$\hat{g} = \begin{pmatrix} g_0 + g_z & g_x - ig_y \\ g_x + ig_y & g_0 - g_z \end{pmatrix}$$

$$N(\mathbf{r}, E) = \left\langle \underline{N}(\mathbf{k}_F, \mathbf{r}, E) \right\rangle_{\mathbf{k}_F} = N_0 \left\langle \text{Re}[g_0(\mathbf{k}_F, \mathbf{r}, \omega_n)|_{i\omega_n \rightarrow E+i\eta}] \right\rangle_{\mathbf{k}_F}$$

Dispersion

Riccati equations

$$-i\hbar\mathbf{v}_F \cdot \nabla \hat{g}(\mathbf{k}_F, \mathbf{r}, \omega_n) = \left[\begin{pmatrix} i\omega_n \hat{1} & -\hat{\Delta}(\mathbf{k}_F, \mathbf{r}) \\ \hat{\Delta}^\dagger(\mathbf{k}_F, \mathbf{r}) & -i\omega_n \hat{1} \end{pmatrix}, \hat{g}(\mathbf{k}_F, \mathbf{r}, \omega_n) \right]$$

$$\hat{g} \equiv -i\pi \begin{pmatrix} \hat{g} & i\hat{f} \\ -i\hat{f} & -\hat{g} \end{pmatrix} \quad \downarrow \quad \begin{pmatrix} \hat{g} & i\hat{f} \\ -i\hat{f} & -\hat{g} \end{pmatrix} = \begin{pmatrix} (\hat{1} + \hat{a}\hat{b})^{-1} & 0 \\ 0 & (\hat{1} + \hat{b}\hat{a})^{-1} \end{pmatrix} \begin{pmatrix} \hat{1} - \hat{a}\hat{b} & 2i\hat{a} \\ -2i\hat{b} & -(\hat{1} - \hat{b}\hat{a}) \end{pmatrix}$$

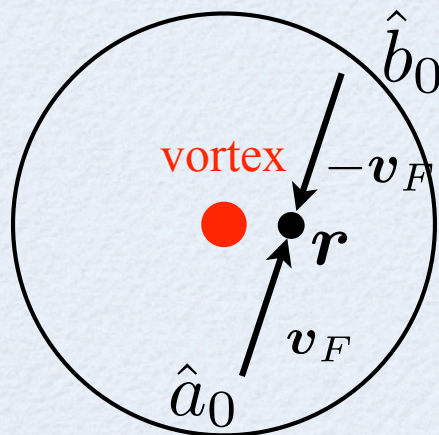
Riccati equations

toward \mathbf{v}_F

$$\hbar\mathbf{v}_F \cdot \nabla \hat{a}(\mathbf{k}_F, \mathbf{r}, \omega_n) = \hat{\Delta} - \hat{a}(\mathbf{k}_F, \mathbf{r}, \omega_n) \hat{\Delta}^\dagger \hat{a}(\mathbf{k}_F, \mathbf{r}, \omega_n) - 2\omega_n \hat{a}(\mathbf{k}_F, \mathbf{r}, \omega_n)$$

toward $-\mathbf{v}_F$

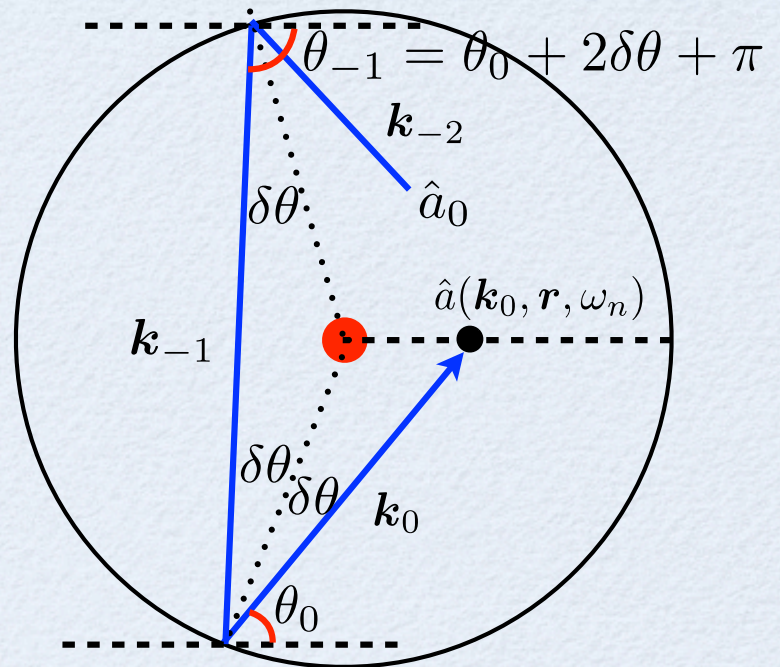
$$-\hbar\mathbf{v}_F \cdot \nabla \hat{b}(\mathbf{k}_F, \mathbf{r}, \omega_n) = \hat{\Delta}^\dagger - \hat{b}(\mathbf{k}_F, \mathbf{r}, \omega_n) \hat{\Delta} \hat{b}(\mathbf{k}_F, \mathbf{r}, \omega_n) - 2\omega_n \hat{b}(\mathbf{k}_F, \mathbf{r}, \omega_n)$$



Numerical method

オーダーパラメーターが空間変化しているため、 \mathbf{a} , \mathbf{b} の初期値を決定することができない。
 ただし、コヒーレンス長よりも十分長い積分経路をとれば初期値によらない解を得られる。

Y. Nagai *et al.*, arXiv:1202.2661.



$$k_{-1,x} = -k_{0,x} \cos[2(\theta_0 + \delta\theta)] - k_{0,y} \sin[2(\theta_0 + \delta\theta)]$$

$$k_{-1,y} = -k_{0,x} \sin[2(\theta_0 + \delta\theta)] + k_{0,y} \cos[2(\theta_0 + \delta\theta)]$$

$$\hbar \mathbf{v}_F(\mathbf{k}_{-1}) \cdot \nabla \hat{a}(\mathbf{k}_0, \mathbf{r}, \omega_n) = \hat{\Delta}(\mathbf{k}_0, \mathbf{r}) - \hat{a}(\mathbf{k}_0, \mathbf{r}, \omega_n) \hat{\Delta}^\dagger(\mathbf{k}_0, \mathbf{r}) \hat{a}(\mathbf{k}_0, \mathbf{r}, \omega_n) - 2\omega_n \hat{a}(\mathbf{k}_0, \mathbf{r}, \omega_n)$$



$$\hbar \mathbf{v}_F(\mathbf{k}_0) \cdot \nabla \hat{a}(\mathbf{k}_{-1}, \mathbf{r}, \omega_n) = \hat{\Delta}(\mathbf{k}_{-1}, \mathbf{r}) - \hat{a}(\mathbf{k}_{-1}, \mathbf{r}, \omega_n) \hat{\Delta}^\dagger(\mathbf{k}_{-1}, \mathbf{r}) \hat{a}(\mathbf{k}_{-1}, \mathbf{r}, \omega_n) - 2\omega_n \hat{a}(\mathbf{k}_{-1}, \mathbf{r}, \omega_n)$$

$$\hat{\Delta}(\mathbf{k}, \mathbf{r}) = iC_{\mu i}(\mathbf{r}) \hat{\sigma}_\mu \hat{\sigma}_y k_i$$

$$C_{\mu x}(\mathbf{r}) \rightarrow -C_{\mu x}(\mathbf{r}) \cos[2(\theta_0 + \delta\theta)] - C_{\mu y}(\mathbf{r}) \sin[2(\theta_0 + \delta\theta)]$$

$$C_{\mu y}(\mathbf{r}) \rightarrow -C_{\mu x}(\mathbf{r}) \sin[2(\theta_0 + \delta\theta)] + C_{\mu y}(\mathbf{r}) \cos[2(\theta_0 + \delta\theta)]$$

A-phase-core vortex

$$T = 0.2T_c, R = 40\xi_0$$

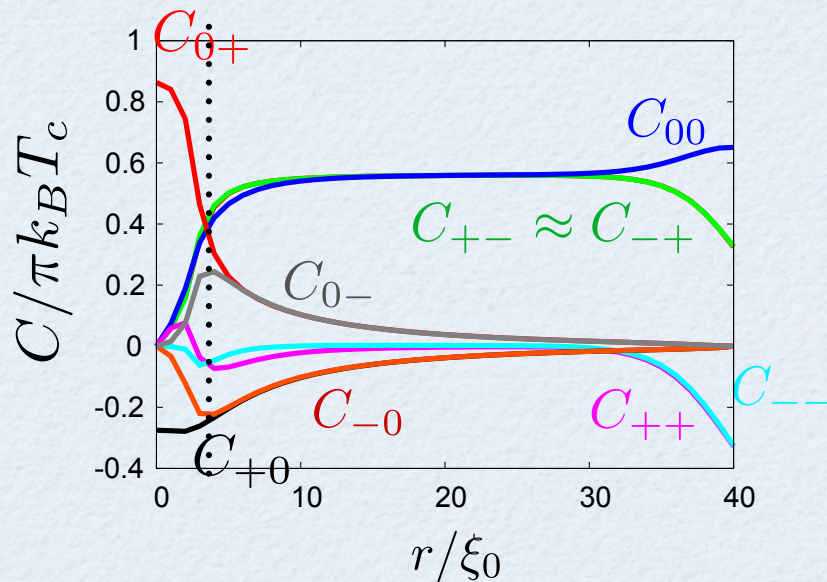
Order parameter

$$\hat{\Delta}(\mathbf{k}, \mathbf{r}) = iC_{\mu i}(\mathbf{r})\hat{\sigma}_\mu\hat{\sigma}_y k_i$$

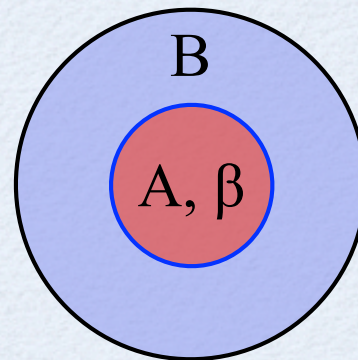
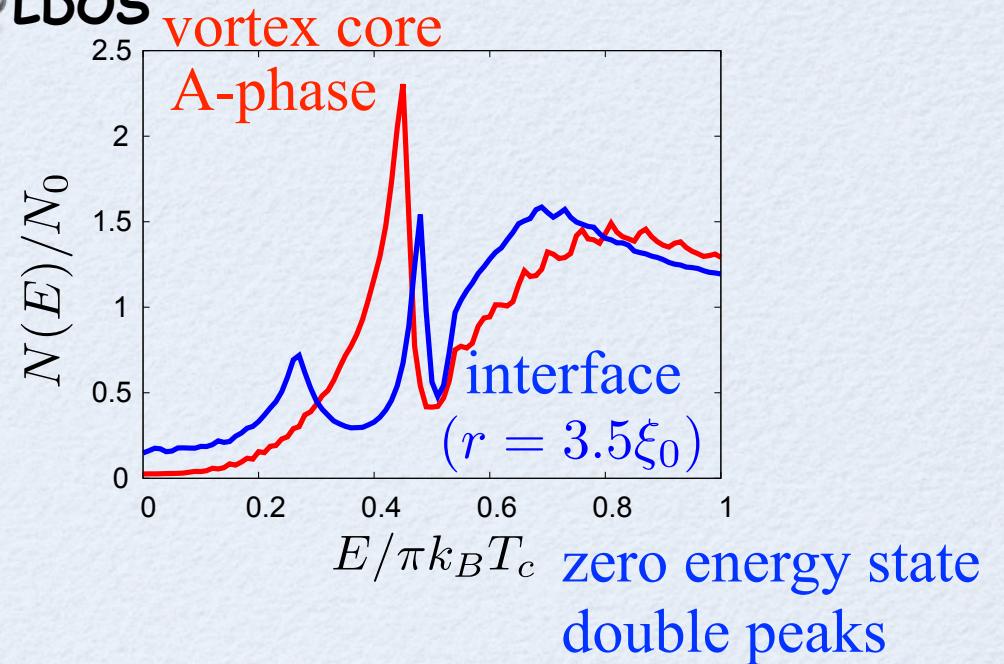
$$C = \begin{pmatrix} C_{++}e^{-i\phi} & C_{+0} & C_{+-}e^{i\phi} \\ C_{0+} & C_{00}e^{i\phi} & C_{0-}e^{2i\phi} \\ C_{-+}e^{i\phi} & C_{-0}e^{2i\phi} & C_{--}e^{3i\phi} \end{pmatrix}$$

β-phase

A-phase B-phase

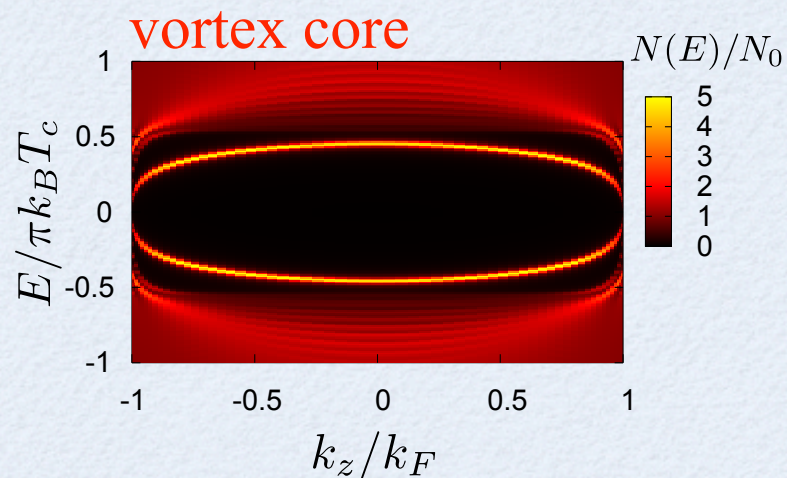


LDOS

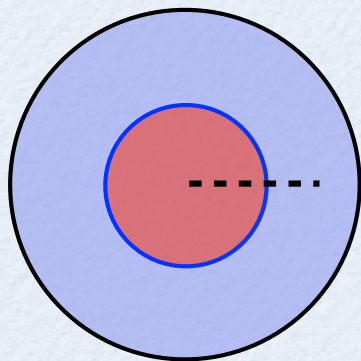


A-phase-core vortex

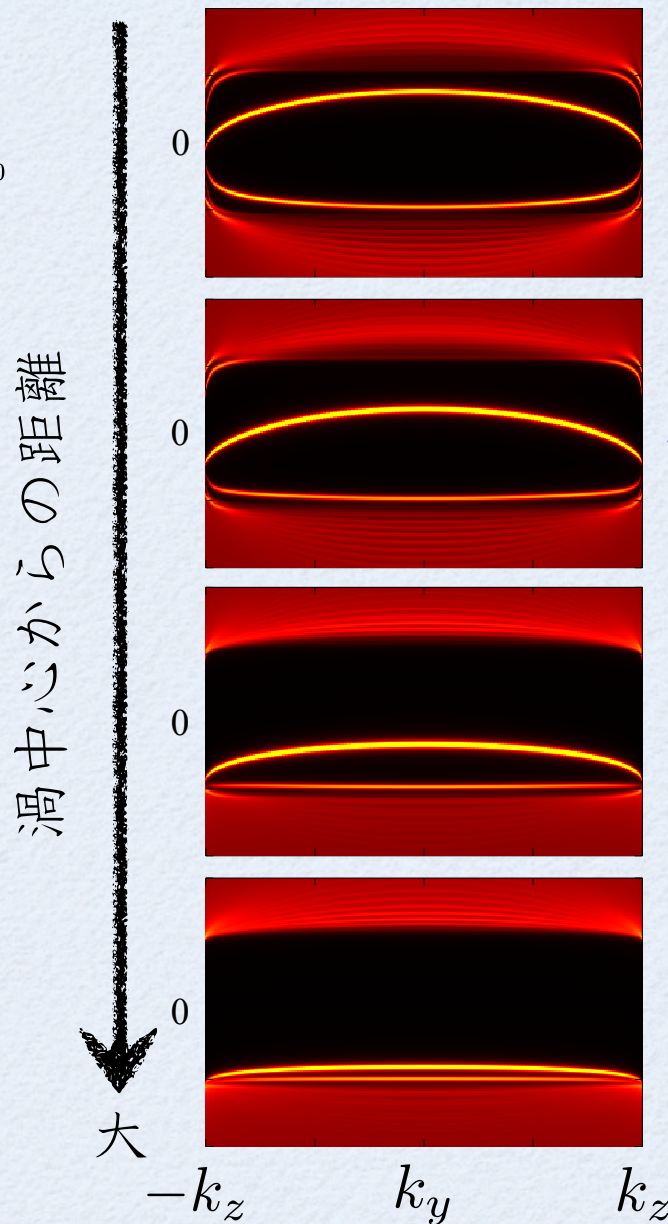
Dispersion



A相のギャップエッジ



トポロジカル超流動体間の
トポロジカル相転移



ブランチが
zero energyを横切る

→ zero energy state

2つのブランチ
→ double peaks

Double-core vortex

Order parameter

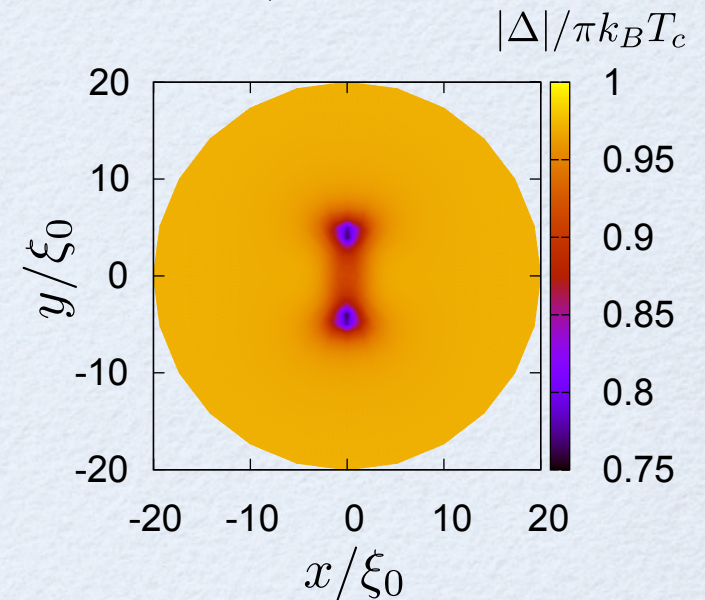
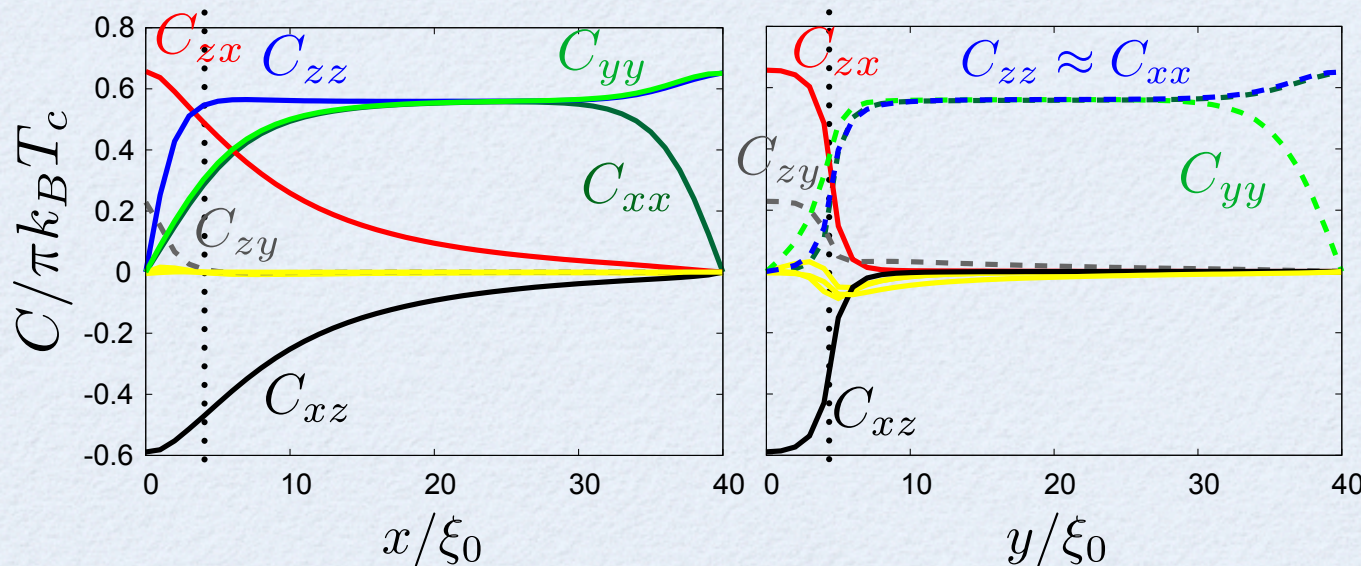
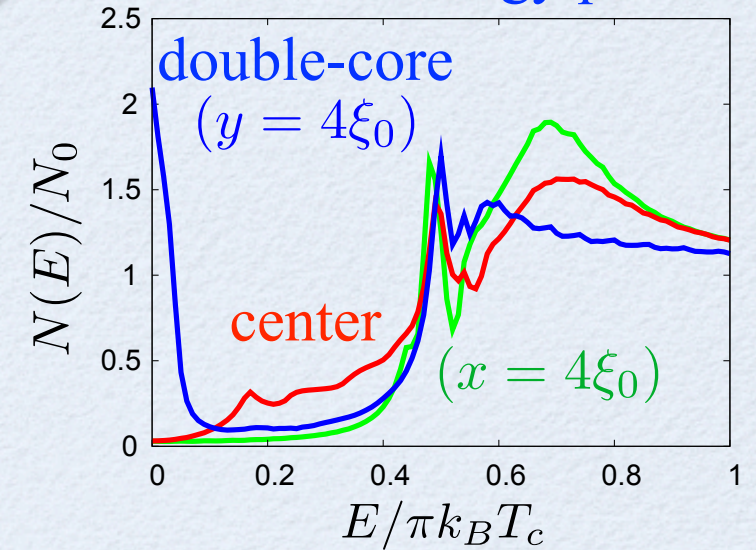
$$\hat{\Delta}(\mathbf{k}, \mathbf{r}) = iC_{\mu i}(\mathbf{r})\hat{\sigma}_{\mu}\hat{\sigma}_y k_i$$

$$C(r = R) = \begin{pmatrix} C_{++}e^{-i\phi} & \underline{C_{+0}} & C_{+-}e^{i\phi} \\ \underline{C_{0+}} & C_{00}e^{i\phi} & \underline{C_{0-}e^{2i\phi}} \\ C_{-+}e^{i\phi} & \underline{C_{-0}e^{2i\phi}} & C_{--}e^{3i\phi} \end{pmatrix}$$

center: planar-like

LDOS

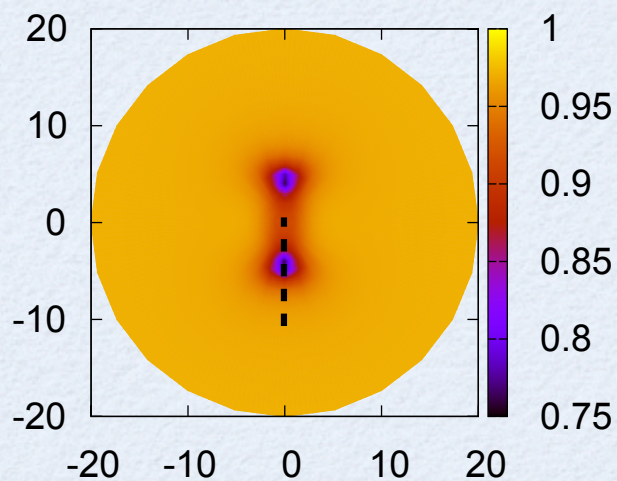
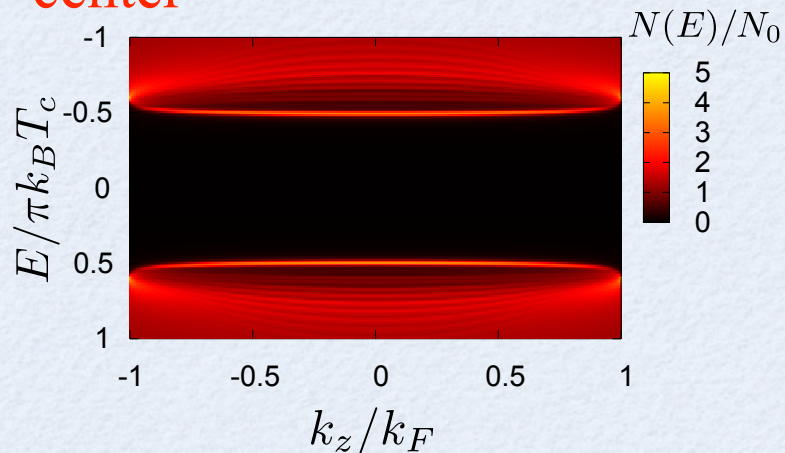
zero energy peak



Double-core vortex

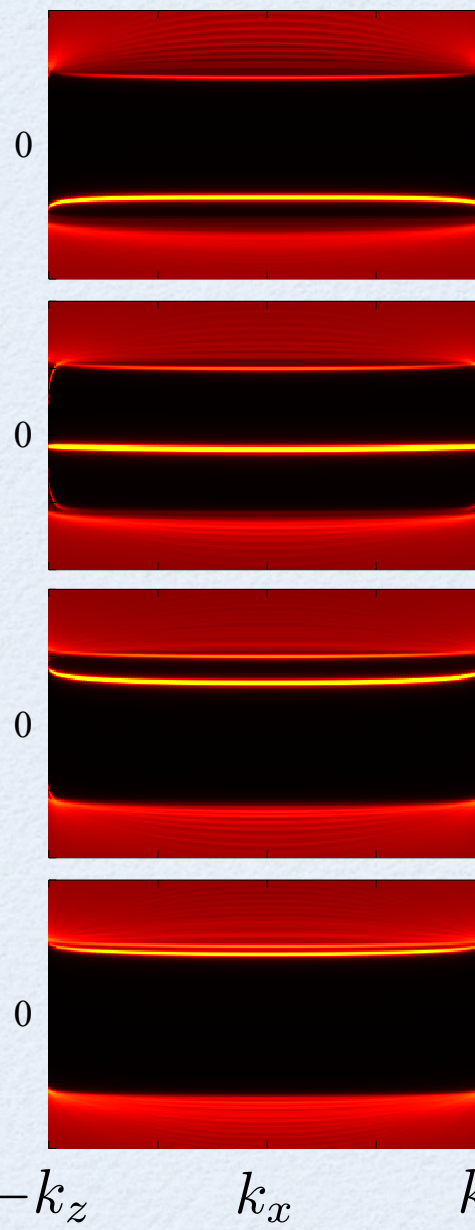
Dispersion

center

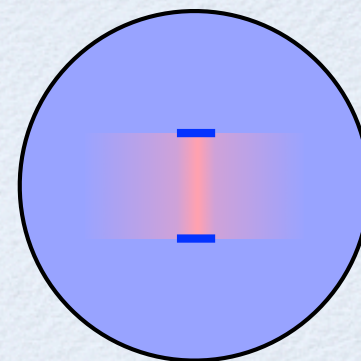


円筒中心からの距離

大



flat bandが
zero energyを横切る
→ zero energy peak




x方向: 連続変化
→ edge stateなし

y方向: 相変化
→ edge state

2D B-phase (planar-phase),
3D B-phase 間のトポロジカル相転移

Summary

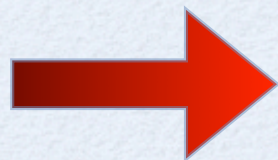
B相の渦周りに異なるトポロジカル超流動体間のトポロジカル相転移によるエッジ状態が存在

 **A-phase-core vortex**

A相 \Leftrightarrow B相

 **Double-core vortex**

2D B相 \Leftrightarrow 3D B相



ゼロエネルギー状態

Future prospects

 **n-texture**

 **Spin susceptibility**

 **NMR spectrum**